

Compiler

(1) LL(1)

- (a) $A \rightarrow \alpha_1 / \alpha_2$ then, if $first(\alpha_1) \cap first(\alpha_2) \neq \emptyset \Rightarrow$ Not LL(1)
- (b) $A \rightarrow \alpha_1 / \epsilon$ then if $First(\alpha) \cap Follow(A) \neq \emptyset \Rightarrow$ Not LL(1)

(2) LR(k)

If LR(0) then it is also SLR(1)

(a) SLR(1) :-

SR conflict

$A \rightarrow \alpha \cdot a \beta$
 $B \rightarrow \gamma \cdot$

if $\exists a \in Follow(B) \neq \emptyset$
= S/R conflict
= Not SLR(1)

RR conflict

$A \rightarrow \alpha \cdot$
 $B \rightarrow \gamma \cdot$

if $Follow(A) \cap Follow(B) \neq \emptyset$
= R/R conflict
= Not SLR(1)

(b) LR(0) :-

same rule
Not LR(0)

	a	b	c	\$
i	S/R	R	R	R

same rule
Not LR(0)

	a	b	c	\$
i	R ₁ /R ₂	R ₁ /R ₂	R ₁ /R ₂	R ₁ /R ₂

(c) CLR(1) or LRC(1) :-

$A \rightarrow \alpha \cdot a \beta, b$
 $B \rightarrow \gamma \cdot, a$

\Rightarrow SR conflict
 \Rightarrow Not CLR(1)

$A \rightarrow \alpha \cdot, a$
 $B \rightarrow \gamma \cdot, a$

\Rightarrow RR conflict
 \Rightarrow Not CLR(1)

(d) LALR(1) :-

"

Not LR conflict

"

Not LR conflict
still you have to check
yes/no are conflict

LL(1) is always LR(1)

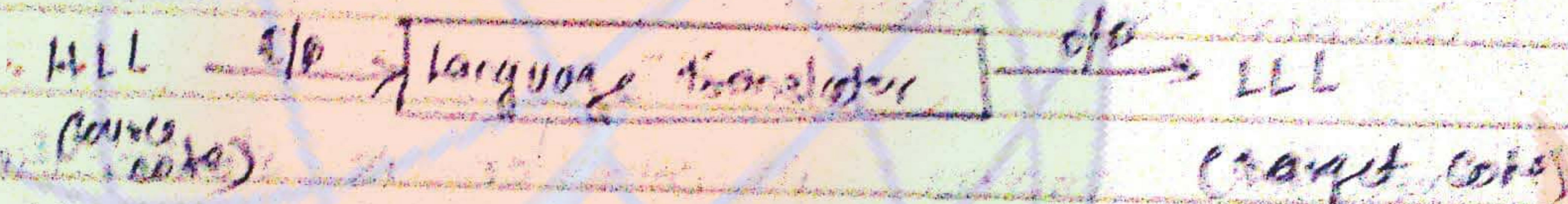
Every LR(0) is SLR(1) but every SLR(1) is not LR(0)

Compiler

{ CO = 4-6 }
{ TOC = 8-11 }

- Phases of a compiler
- Lexical Analysis
- Syntax Analysis
- Semantic Analysis
- Intermediate Code Generation
- Code Optimization
- Code Generation

1) Language Translator:

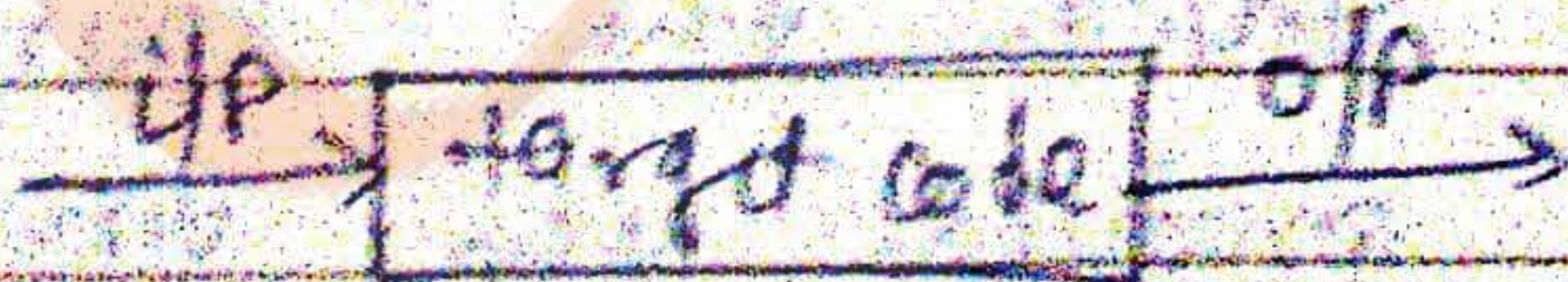
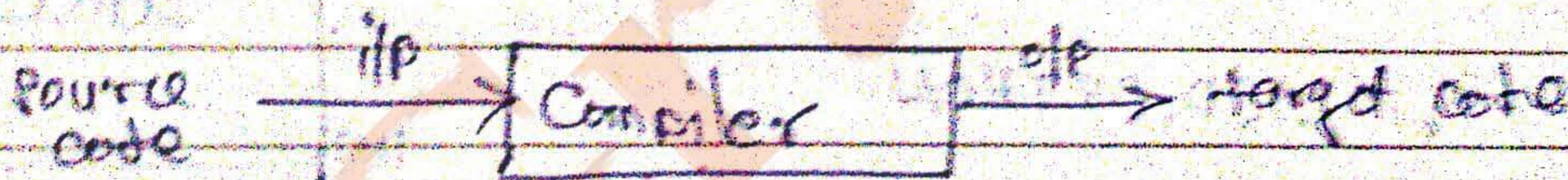


Language translator takes source code as input and produces target code as output.

2) The types of language translators -

- Compiler
- Interpreter
- Assembler

3) a) Compiler



C, C++

executed
all
at a
time

Compiler takes the source code as input and produces the target code as output.

then the target code will be called by the user to process the inputs for producing the output.

A compiler execute the entire code at a time, if any error occurs at any line, all of them will be given at a time.

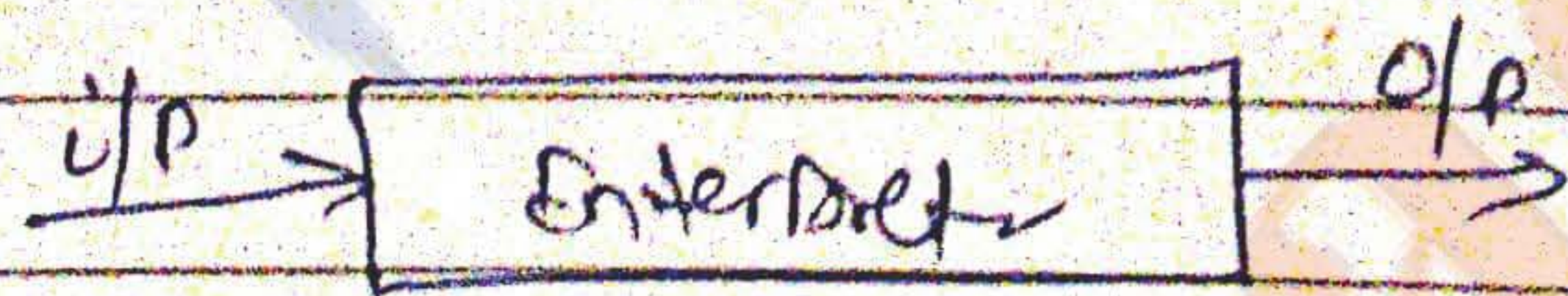
• Error diagnosis is not that much easy as compare to others.

• Execution process in compiler is slower than others.

But output generation by compiler is faster.

eg. C, C++

b) Interpreter.



eg. LISP, PYTHON

Interpreter takes the source code as input and produces the direct outputs - it will not produce any intermediate language

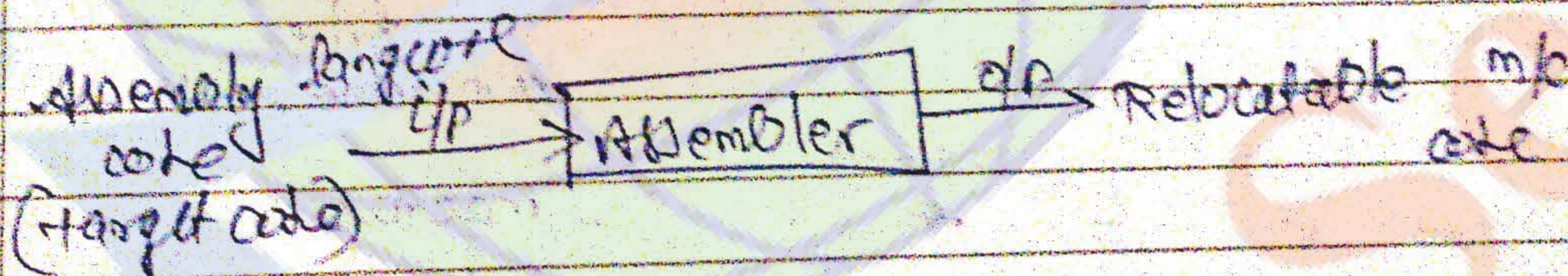
- Interpreter - execute the code line by line
 if any error occurs at any line, immediately that error will be produced.
 Until we resolve that error, the interpreter will not move to the next line.

- Error diagnosis in interpreter is easy.

- Execution process in interpreter is faster but output generation is slower than the compiler.

eg. LISP, PYTHON

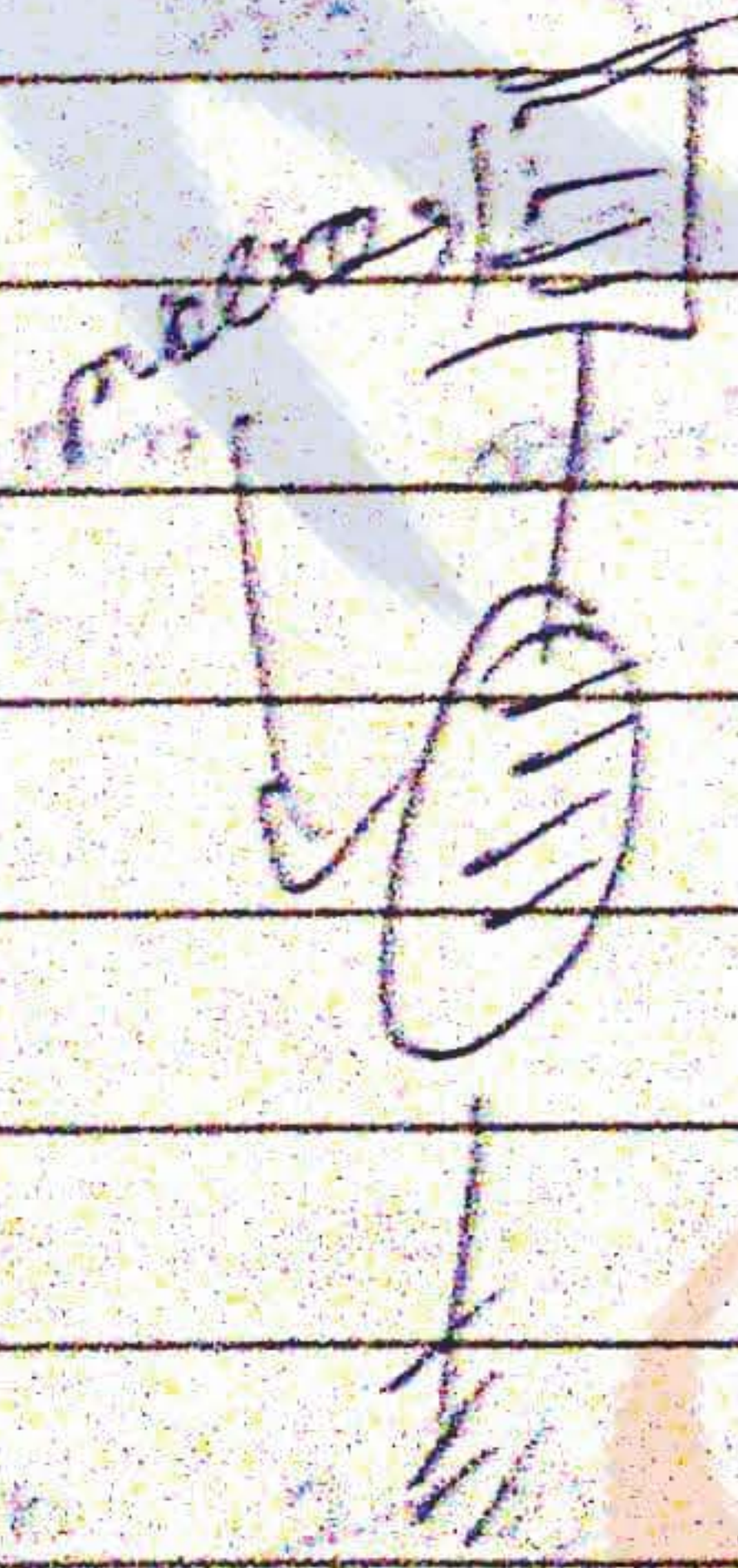
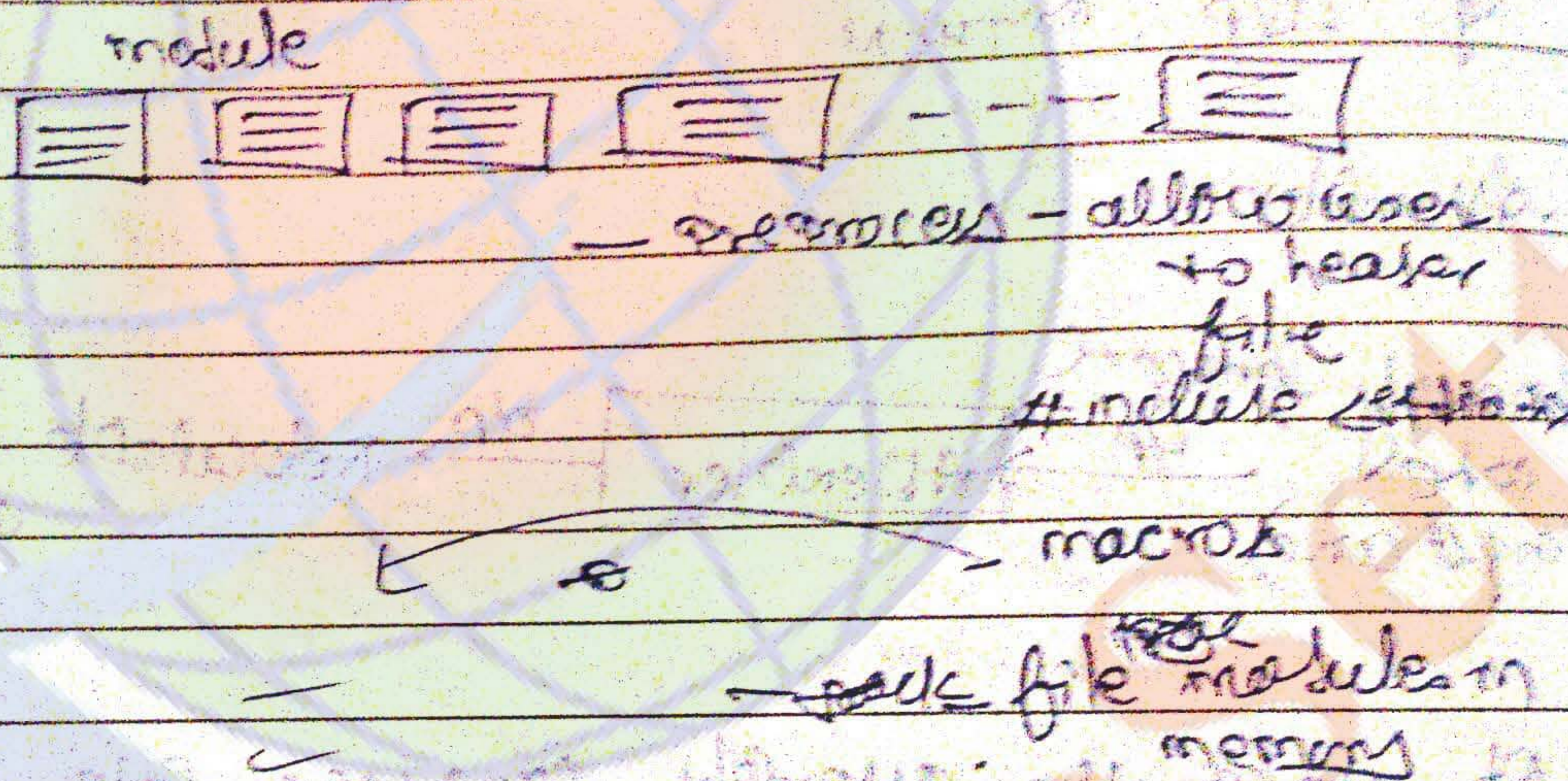
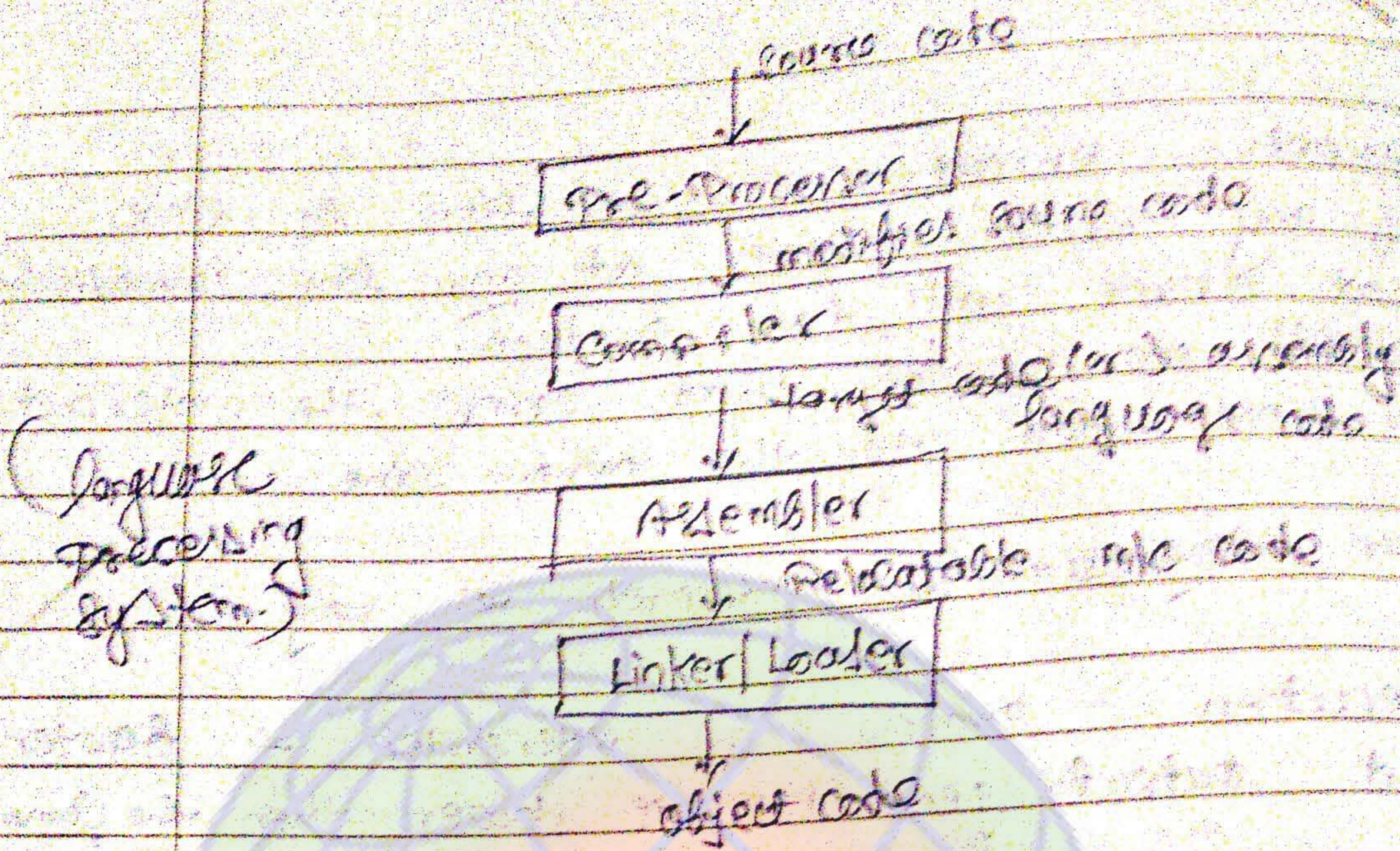
c) Assembler:-



It takes the assembly language code as input and produces relocatable machine code as output which has to be loaded into main memory ready for execution.

4) Language processing system

Pre-processor - takes the source code as input and produces modified source code as output.



• Preprocessor - Preprocessor takes the source code as input and produces modified source code as input

- If the program is too large it may

be divided into small pieces and they will be stored in different files.

- The pre-processor will take care of all these modules.

- Pre-processor allow the user to use header files and macros.

- A macro is a set of instructions which are repeatedly used in the program.

- Pre-Processing is an optional
eg. the language ~~is~~ which do not support #include < > they do not require Pre-Processing -

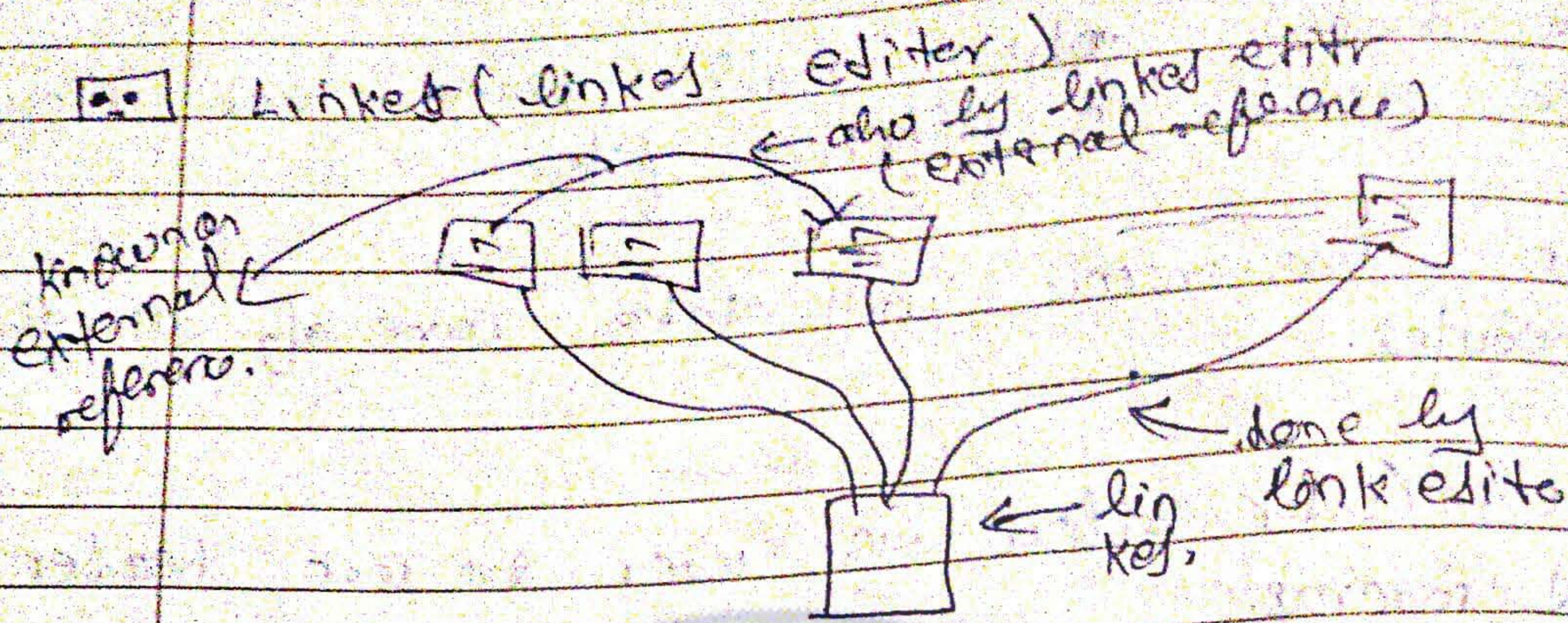
● Compiler - compiler takes the modified source code as input and produces the target code as output.

● - Compilation is also an optional
eg. script languages like Java script.

HTML
Assembly language
like 8085, 8086

they not require compile

● Assemble -



Phase 2

linker editor - If the program is too large, it may be divided into small pieces and will be stored in different files.

The linker links all these modules as a single module.

The linker editor resolves external references.

If a code in one file refers to allocation in another file is called as external reference.



loader:-

To execute the program, it must be loaded in main memory.

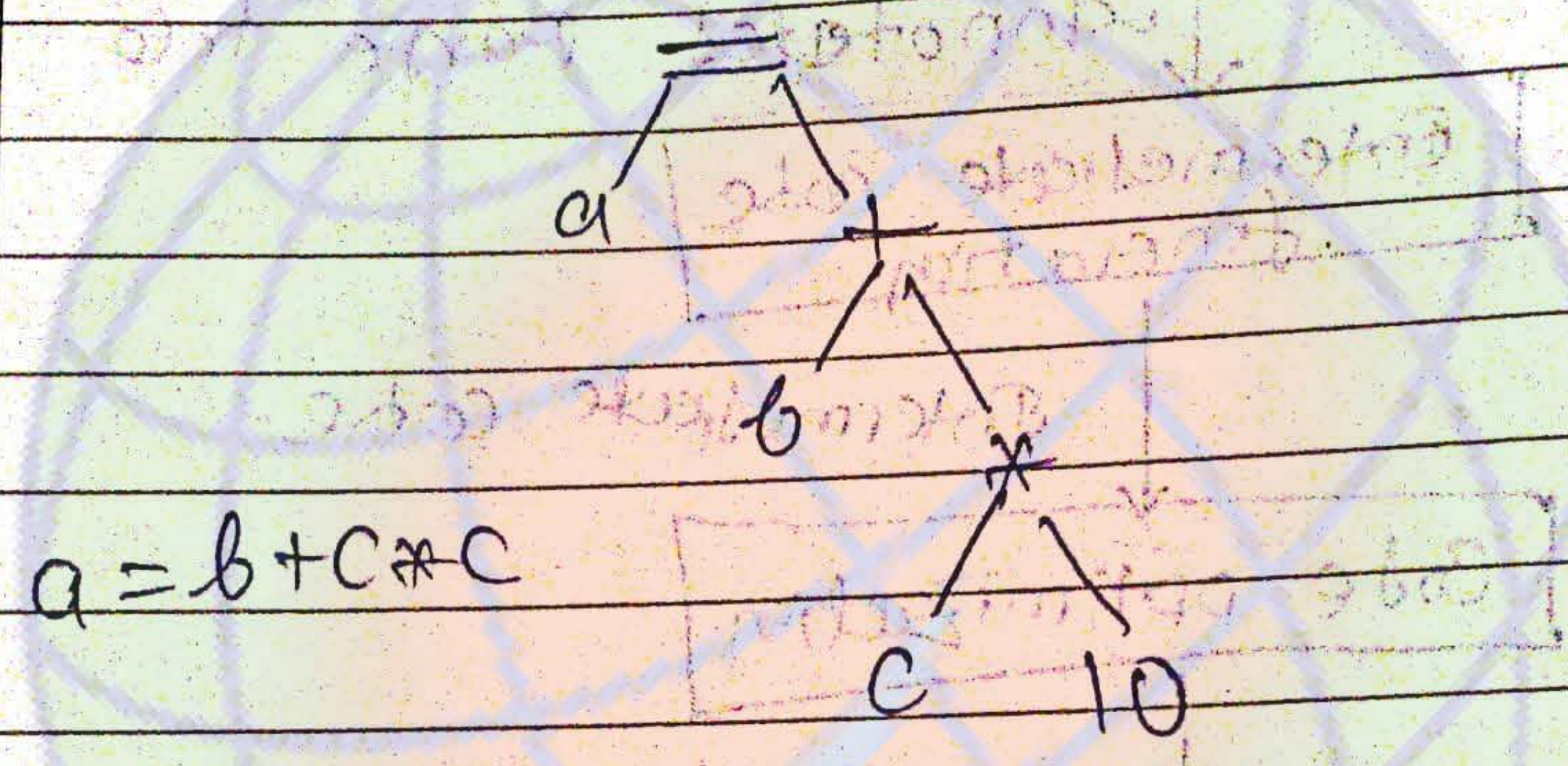
This will be done by loader.

a)

b) Syntax Analysis:-

CFG rule production is applied

The tokens generated by lexical analyser will be grouped together in syntax analyser to make a parse tree.

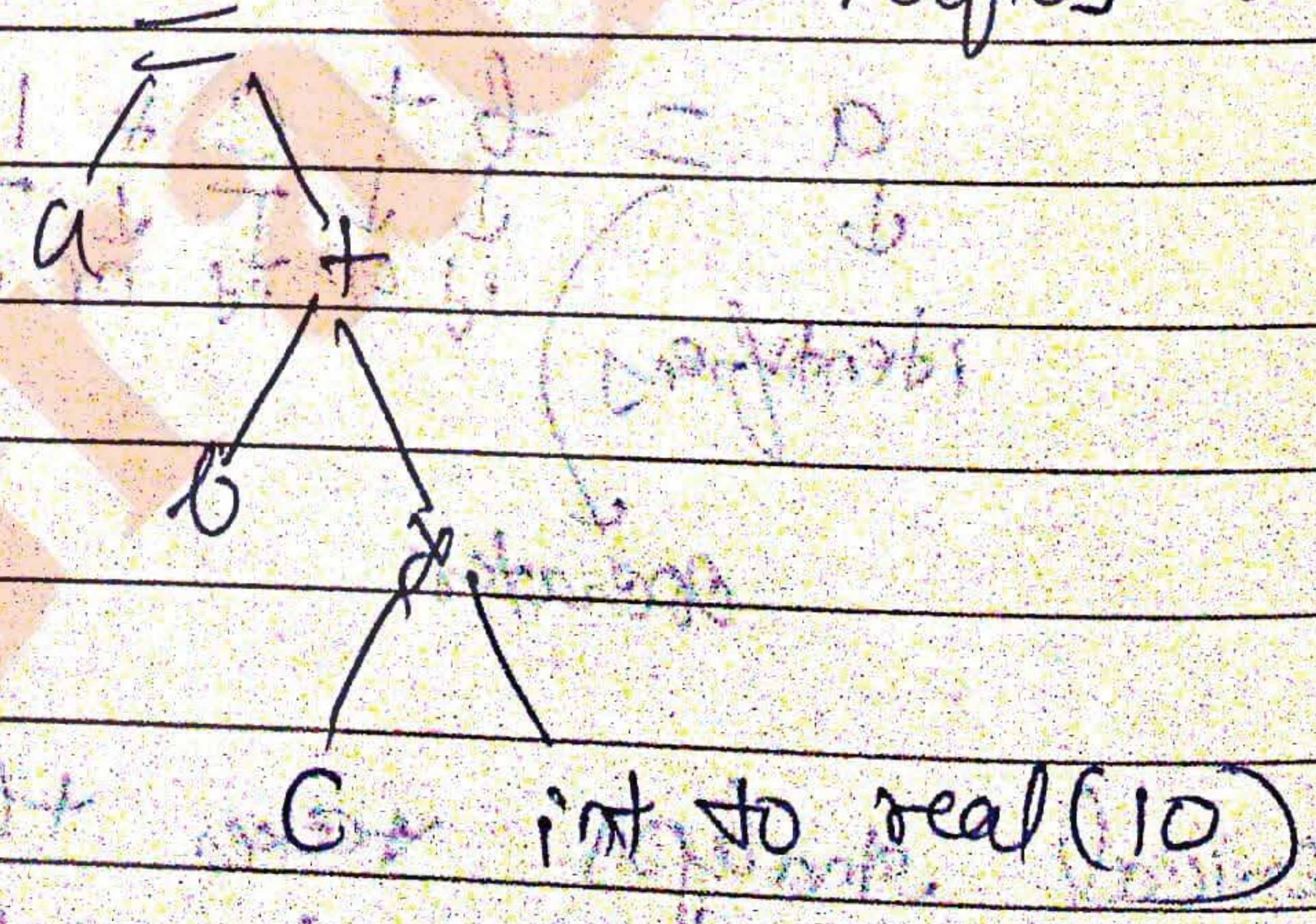


The meaning of the source code will be verified in semantic analysis

c) ~~Semantic Analysis~~ e) Semantic Analysis

meaning will be verified

meaning will be verified



Performs type checking, i.e. type compatible or not

of semantic analysis =
d) Intermediate code generation -

• various types of Intermediate code generated.

3-address code $\rightarrow a = b \text{ op } c$

• 3-address code:

$$a = b + c \times 10.00$$

$$t_1 = \text{int} \text{ to real } (10)$$

$$t_2 = c$$

$$t_3 = t_2 \times t_1$$

$$t_4 = b$$

$$t_5 = t_4 + t_3$$

$$a = t_5$$

inefficient code

Now,

$$t_1 = \text{int to real } (10)$$

$$t_2 = c \times t_1$$

$$t_3 = b + t_2$$

$$a = t_3$$

efficient code

- intermediate code makes the code generation

of semantic analysis
d) Intermediate code generation -

• various types of Intermediate code generation -

1- address code $\rightarrow a = b \text{ op } c$
 \uparrow
 reg

2- address code:

$$a = b + c \times \frac{10.00}{t_2 \times t_1}$$

$$t_1 = \text{int to real}(10)$$

$$t_2 = c$$

$$t_3 = t_2 \times t_1$$

$$t_4 = b$$

$$t_5 = t_4 + t_3$$

$$a = t_5$$

inefficient code

now:

$$t_1 = \text{int to real}(10)$$

$$t_2 = c \times t_1$$

$$t_3 = b + t_2$$

$$a = t_3$$

efficient code

- intermediate code makes the code generation

and easy

- mostly we use ~~of a given code~~
 representation in intermediate code.

e) Code optimization:

It is process of reducing the no. of instructions, without affecting the outcome of the source code.

$$t_1 = \text{int to real}(10)$$

$$t_2 = C * t_1$$

$$a = b + t_2$$

d) code generation:

```
(C) MOV R1, #10.00
```

```
MUL R1, C
```

```
ADD R1, b
```

```
MOV a, R1
```


Lexical Analysis

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The lexical analyzer scans every character of a source and the following will be done.

- Divides into tokens
- Ignore blank space/white space
- Ignore comments.
- Create a symbol table
- Produce lexical errors

a) Divides into tokens.

Tokens The terminologies used in the lexical analyzer are token

Token The set of rules which describes the token

tokens can be kw, op, punctuation mark,

tokens - which describe the category of the input string

eg - keyword (kw), operator (op), punctuation mark (pm), constant, identifier (id)

An identifier can be any combination of alphanumeric symbols. The first symbol of the identifier must be an alphabet or underscore.

- only special symbol allowed in identifier is underscore (_).

Patterns: The set of rules which describes the token.

Lexemes: The sequence of the characters in the source program that matches with patterns of the tokens.

b) Ignore blank space.

int a b
kw id pm id pm

int a b
kw id pm id pm

↓
Ignore space

c) Ignore comments.

/ * x / → will not be converted into tokens

d) create a symbol table

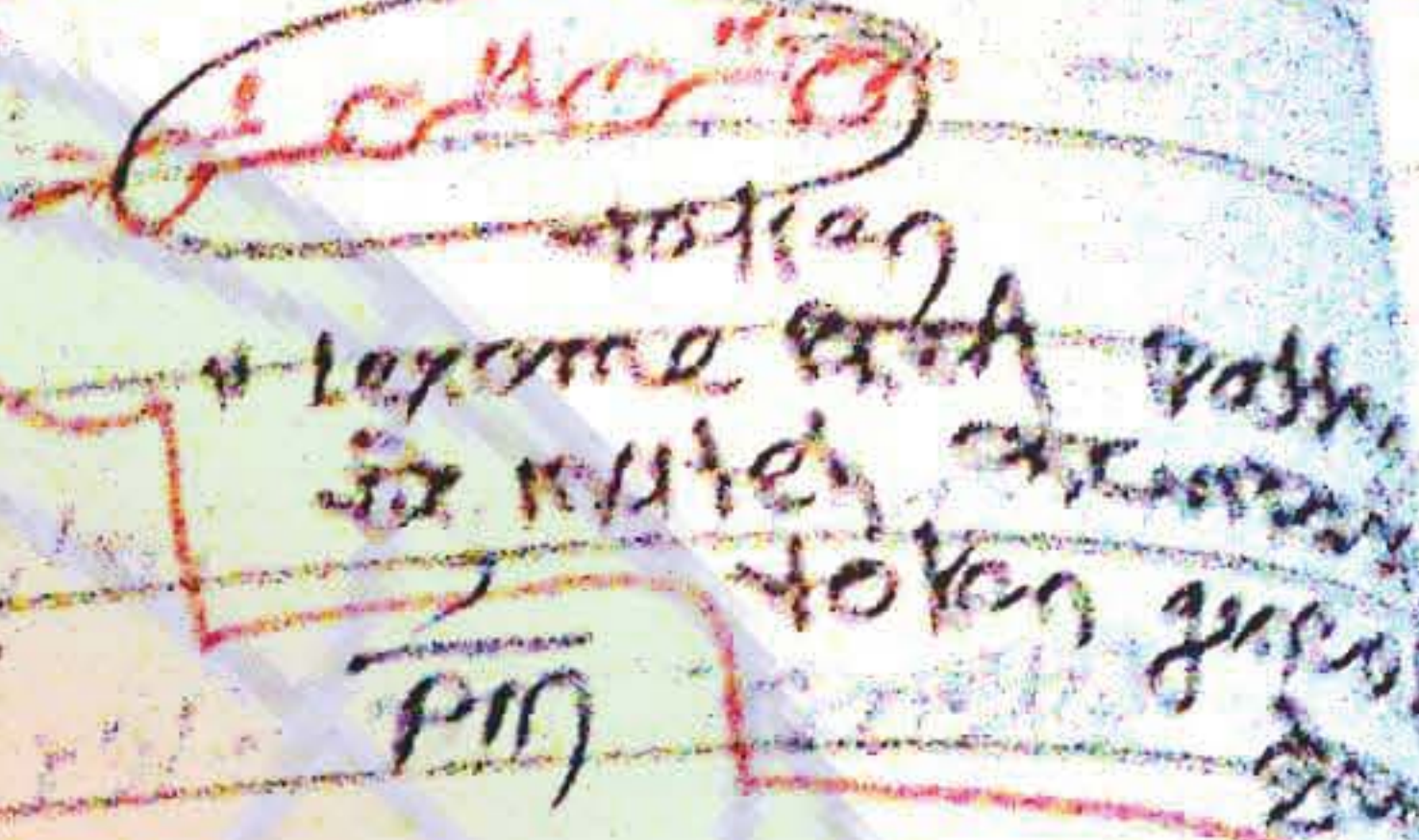
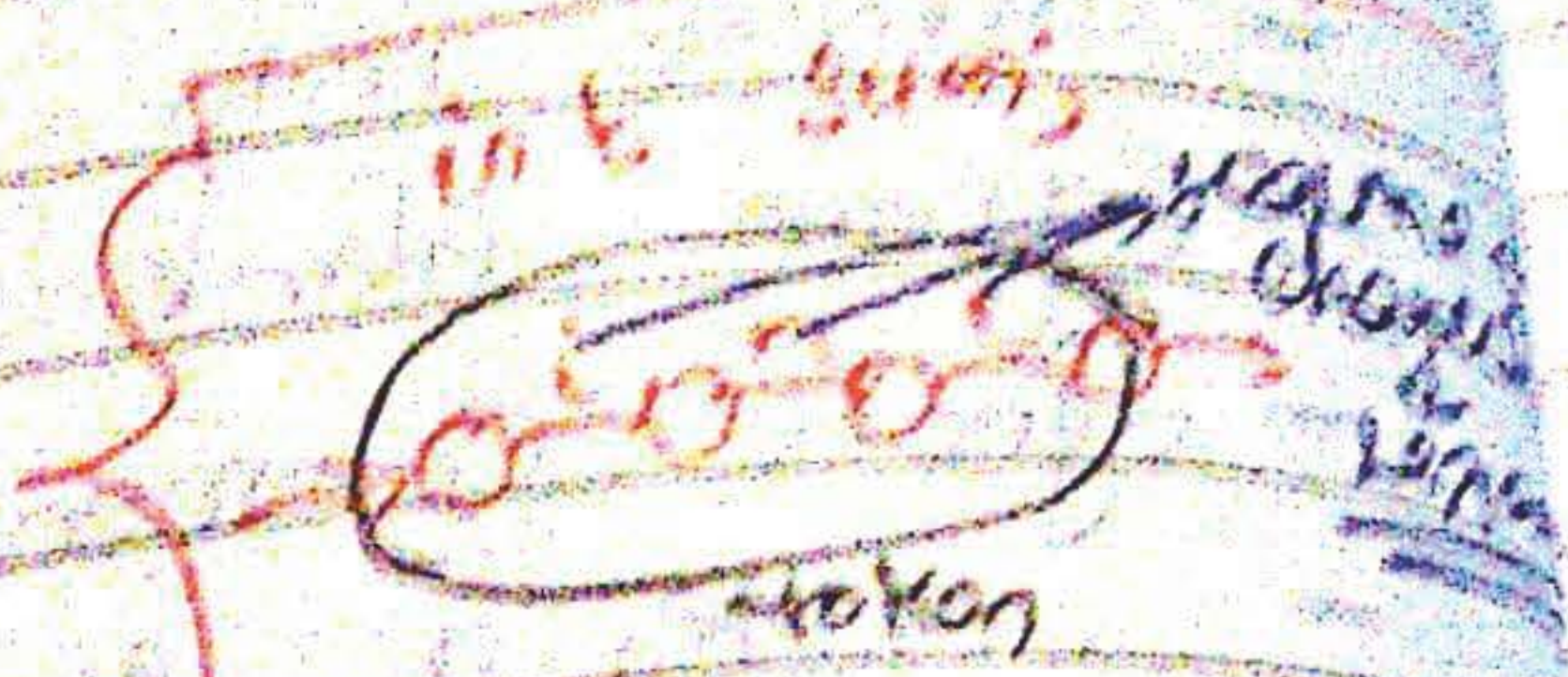
↓
is a data structure, which stores information

• Symbol table: A symbol table is a data-structure, which contain information about ~~the~~ variables and their attribute.
eg. → name of the variable, datatype, value, size, location.

e) produces lexical errors.

Lexical errors: → Unterminated comments /* -- (*)
→ Nested comments

↳ /* -- /* -- */



Lexemes - sequence

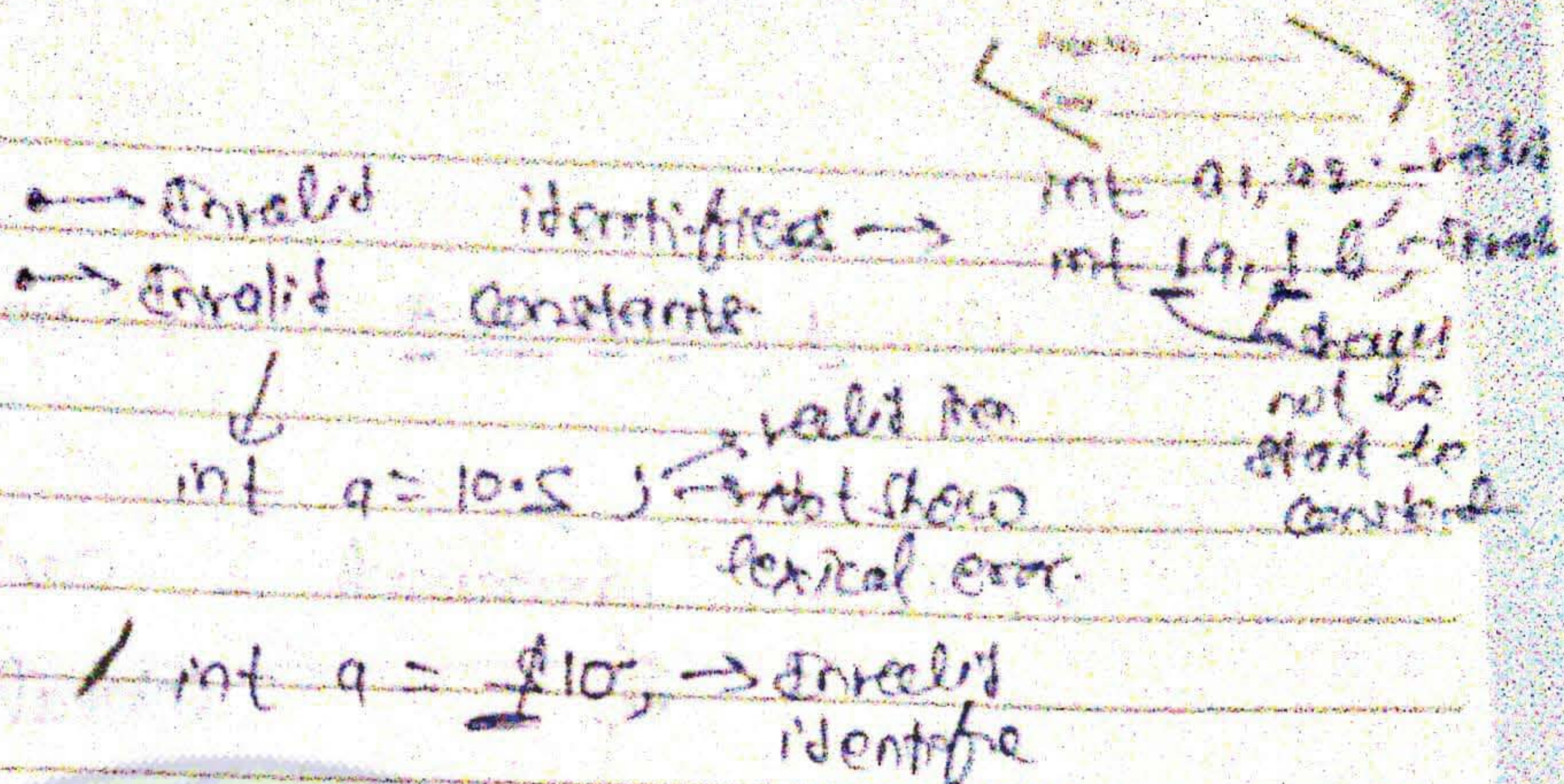
- Note:
- The ...
 - The ...
 - Hand ...

Token

check errors

a)

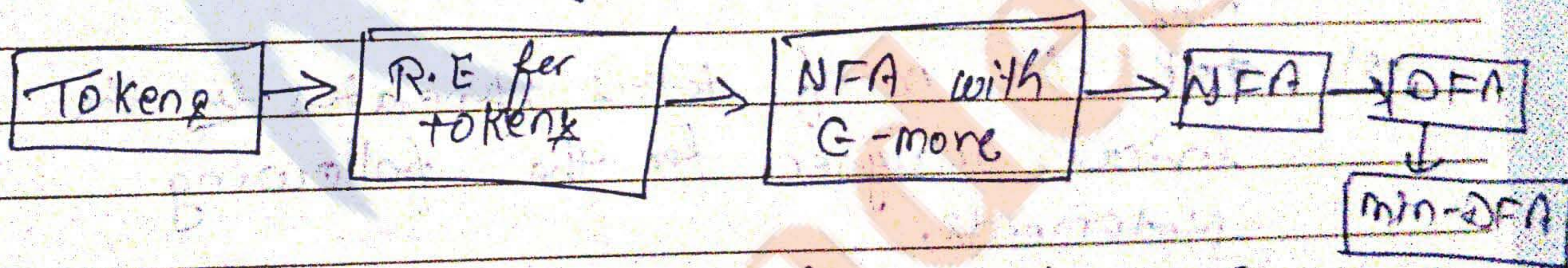
b)



Lexeme - sequence of character

int 'a1, a2' → ~~is~~ lexeme
 int 1a, 1 b → not a lexeme
 int a = \$10 → not a lexeme

- Note:
- The other name of the lexical analyser is scanner
 - The program used in lexical analysis is finite automata.
 - Hand code design



Q) Check whether lexical analyser can produce errors for the following statements.

a) $\frac{id}{id} \frac{id}{id} \frac{pm}{pm} \frac{id}{id} \frac{pm}{pm} \rightarrow$ No lexical errors.

b) $\frac{id}{id} (a > b)$
 $\frac{dse}{dse} a = a + 1$
 $b = b + 1 \rightarrow$ No lexical error

c) a = b + c * d ; \rightarrow no lexical error

d) Print ("Annavati is capital of Andhra");

lexical

\rightarrow Produces lexical error because

ब्रैकेटों की संख्या बराबर नहीं है
braces

e) int 1a, 1b;

\rightarrow lexical error

(invalid identifier)

f) int a = (a 10);

\rightarrow invalid constant

(lexical error)

Find

a) ~~check~~ the no. of tokens generated by the lexical analyser for the following statements.

a) a = b + c * d;

OP OP OP OP OP OP OP OP
id id id id id id id id
Ans = 8

b) if (a > b)

g = a + 1

else

b = b + 1

Ans = 17

Q) Consider the following C-Program and identify the compiler's module about object lines.

```

a) int main()
    {
    int i, n;
    for (i=0; i<=n; i++)
    {
    }
    }
    
```

- a) lexical error only
- b) syntactical error only
- c) both lexical & syntactical error
- d) No compiler error

Hint: If you don't know exactly, go for elimination

Q) An ideal compiler should be

- a) small in size
- b) takes less than compilation
- c) ~~produce~~ must produce an object code which executes faster
- d) all

Ti

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Q) In a compiler the keywords of a language will be recognized during

- lexical analysis
- syntax analysis
- code optimization
- code generation

Q) In a compiler the (module) grouping of characters into tokens will be done during

- scanner
- parser
- code optimizer
- all

Hint:

Ram

Ti Q) An instruction in programming language i.e. the sequence of instructions prior to compiling is known as

- literal
- procedure
- macro
- label

Ans: macro - it will copy the instruction

Q) The data structure in a compiler, used for storing ~~about~~ the information about the variables and their attributes is symbol table

Q) A link ~~editor~~ ^{editor} is a program that matches external names of one program with locations in another program

b) matches the parameters of macro definition with location



Syntax

The
be given
a par
to
some
will be

a) A system program, that sets up an executable program in main memory ready for execution is

- a) assembler
- b) loader
- c) compiler
- d) linker



Content

a) In lexical analysis, the modern computer language such as JAVA, need the power of which of the following machine model in necessary and sufficient sense -

- a) finite automata
- b) push down automata
- c) T.M
- d) All

Note: If not mention sufficient, the go for (d) all



Star

A

b) matches the parameters of the definition with the location

a) A system program, that sets up an executable program in main memory ready for execution is:

- a) Assembler
- b) loader
- c) compiler
- d) linker

a) In lexical analysis, the modern computer languages such as JAVA, need the power of which of the following machine model in necessary and sufficient sense -

- a) finite automata
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★ Sunday

The
he goes
a part
to
some
will

★ Content

of

★

★ Syntax Analysis:

The tokens generated by lexical analyser will be grouped together in syntax analysis to form a parse tree

To form such a tree there must be some rules and requires, and those rules will be supplied by context free grammar (CFG)

$$A \rightarrow \alpha$$

where $A \in V$, (only non terminal)

$\alpha \in (V \cup T)^*$ \rightarrow both

★ Context free grammar (CFG)

if every production of the grammar is of the form

$$A \rightarrow \alpha$$

where $A \in V$, $\alpha \in (V \cup T)^*$

★ Ambiguity:-

— more than one parse tree possible

A grammar is said to be ambiguous, if it can derive at least one string, which is ambiguous.

$$L(G_1) = \{ w_1, w_2, \dots \}$$

if one string is ambiguous, then the grammar is ambiguous.

Q3

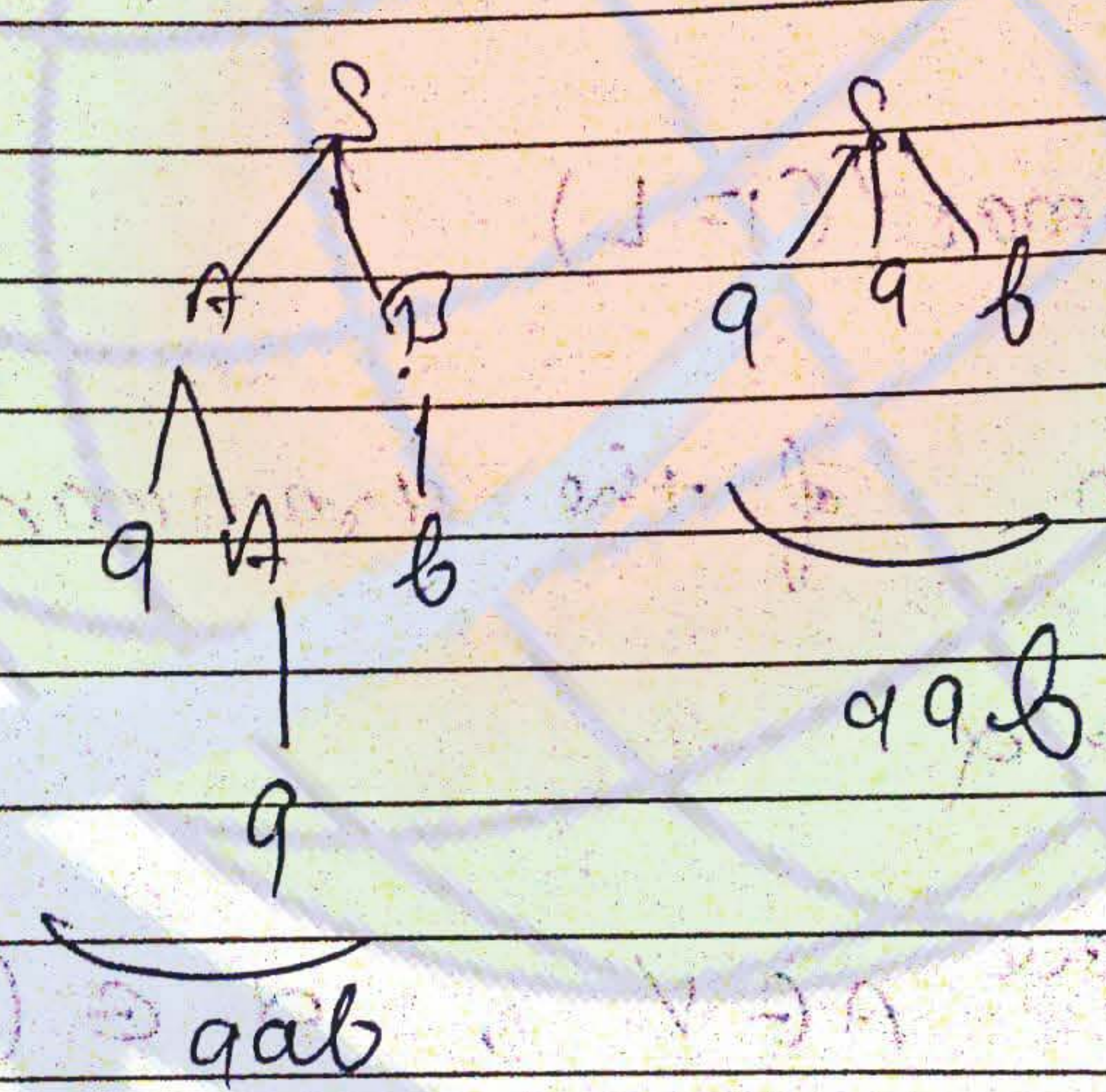
A string $w \in T^*$ is said to be ambiguous, if it has more than one different parse tree.

a) Is this grammar ambiguous?

$$G = \{ S \rightarrow AB/aab, A \rightarrow aA/a, B \rightarrow bB/b \}$$

soln

$$S \rightarrow \underline{AB}$$



So, ambiguous

G is ambig

Q4 N-VI

Note:

An ambiguous grammar is not suitable for any kind of parsing, except backtracking, shift-reduce and operator precedence parsing.

* Elimination of Ambiguity! -

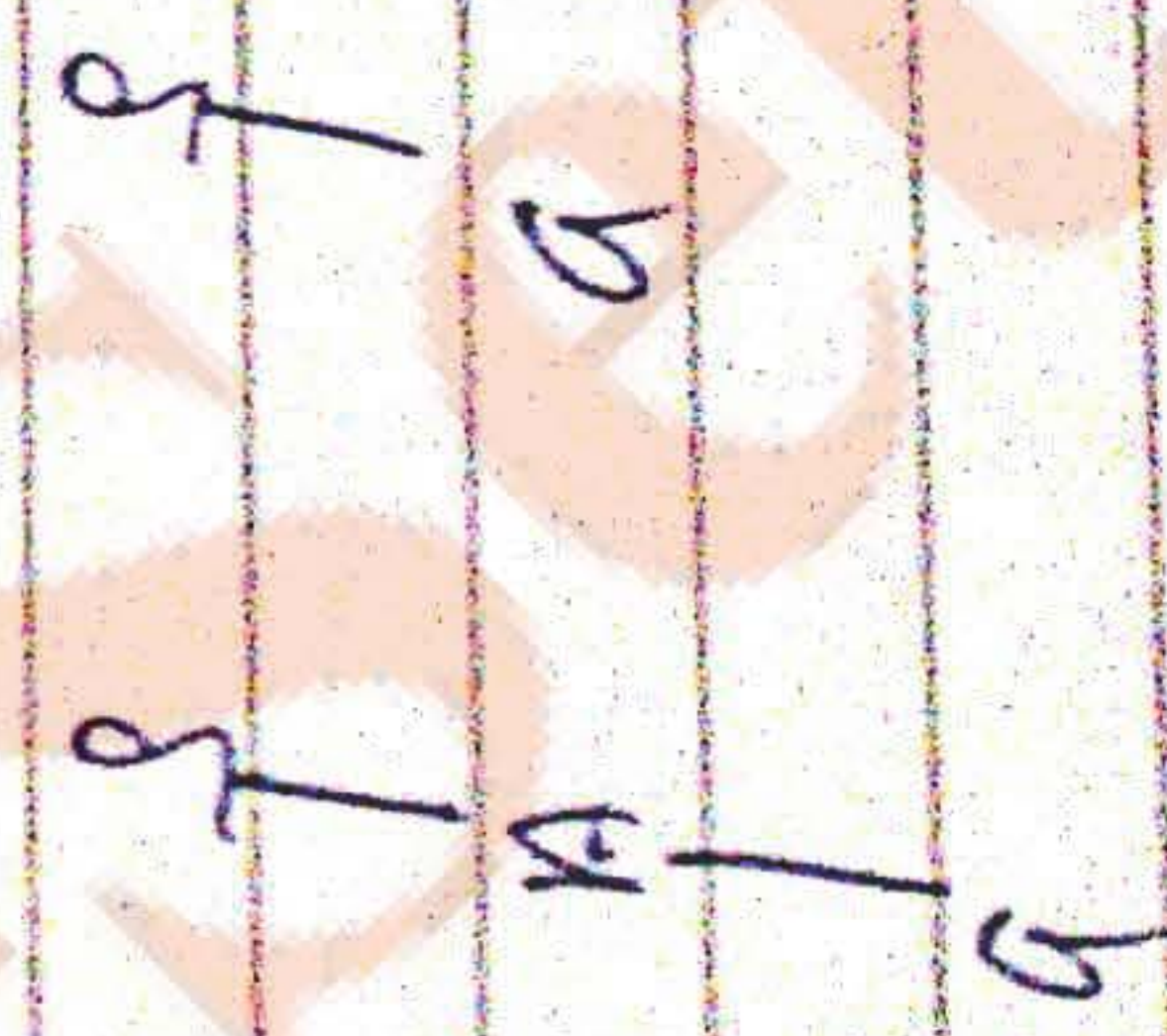
Therefore, we must eliminate the ambiguity from a grammar, but there is no procedure to eliminate the ambiguity from a grammar.

That's why elimination of Ambiguity from a grammar is undecidable.

eg1) $G = \{ S \rightarrow A \cup (aab), A \rightarrow aA/a, B \rightarrow aB/b \}$
i.e. ambiguous grammar
to eliminate.

$G' = \{ S \rightarrow AB, A \rightarrow aA/a, B \rightarrow bB/b \}$
i.e. unambiguous grammar

eg2) $G = \{ S \rightarrow A/a, A \rightarrow aA \}$



So, this is ambiguous

or, $G' = \{ S \rightarrow a \}$

↳ This is unambiguous



* Elimination of Ambiguity! -

Therefore, we must eliminate the ambiguity from a grammar.

But there is no procedure to eliminate the ambiguity from a grammar.

That's why, elimination of ambiguity from a grammar is undecidable.

eg1)

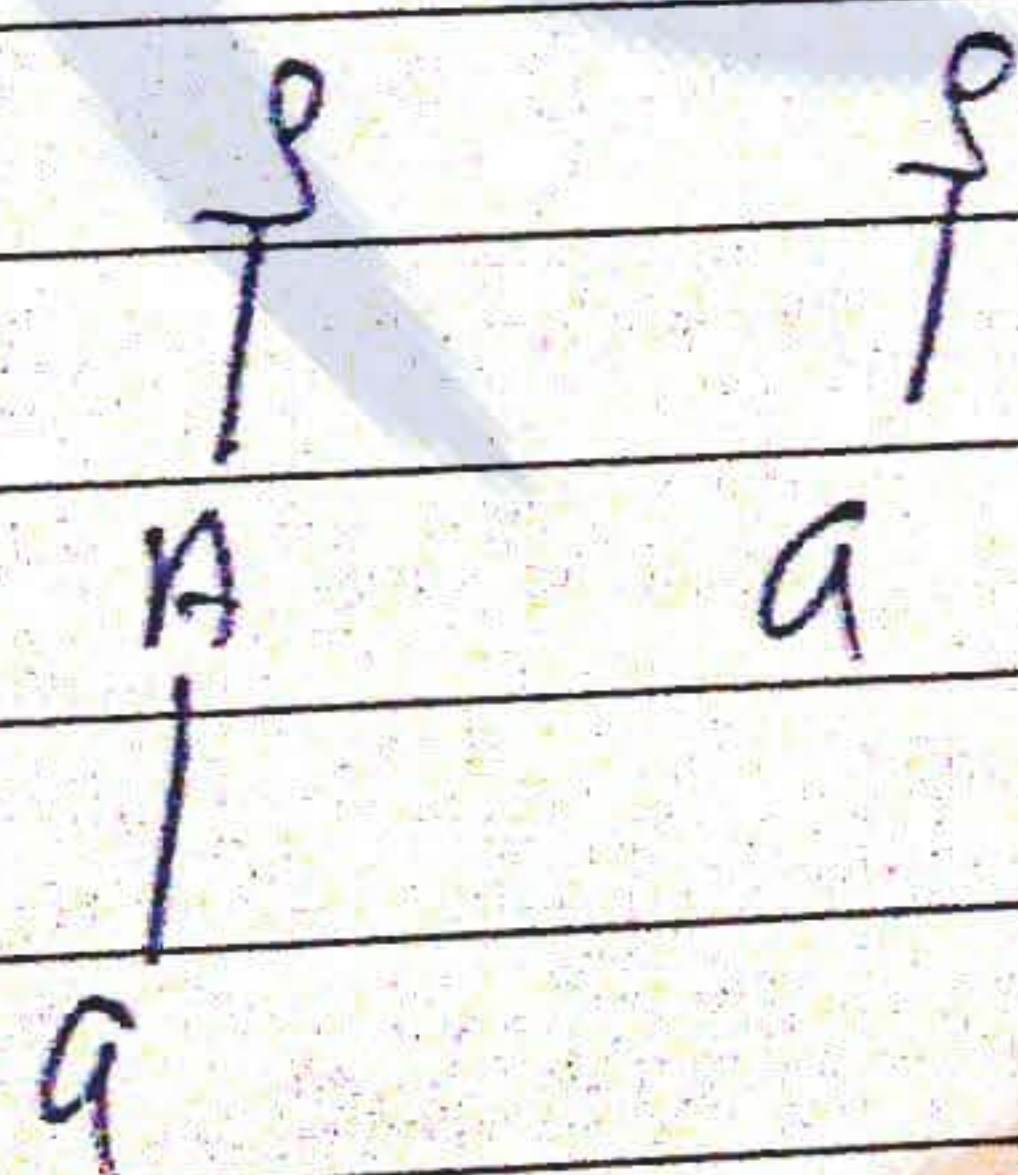
$G = \{ S \rightarrow AB / aab, A \rightarrow aA/a, B \rightarrow bB/b \}$
is ambiguous grammar

to eliminate.

$G' = \{ S \rightarrow AB, A \rightarrow aA/a, B \rightarrow bB/b \}$
is unambiguous grammar

eg2)

$G = \{ S \rightarrow A/a, A \rightarrow a \}$



So, this is ambiguous

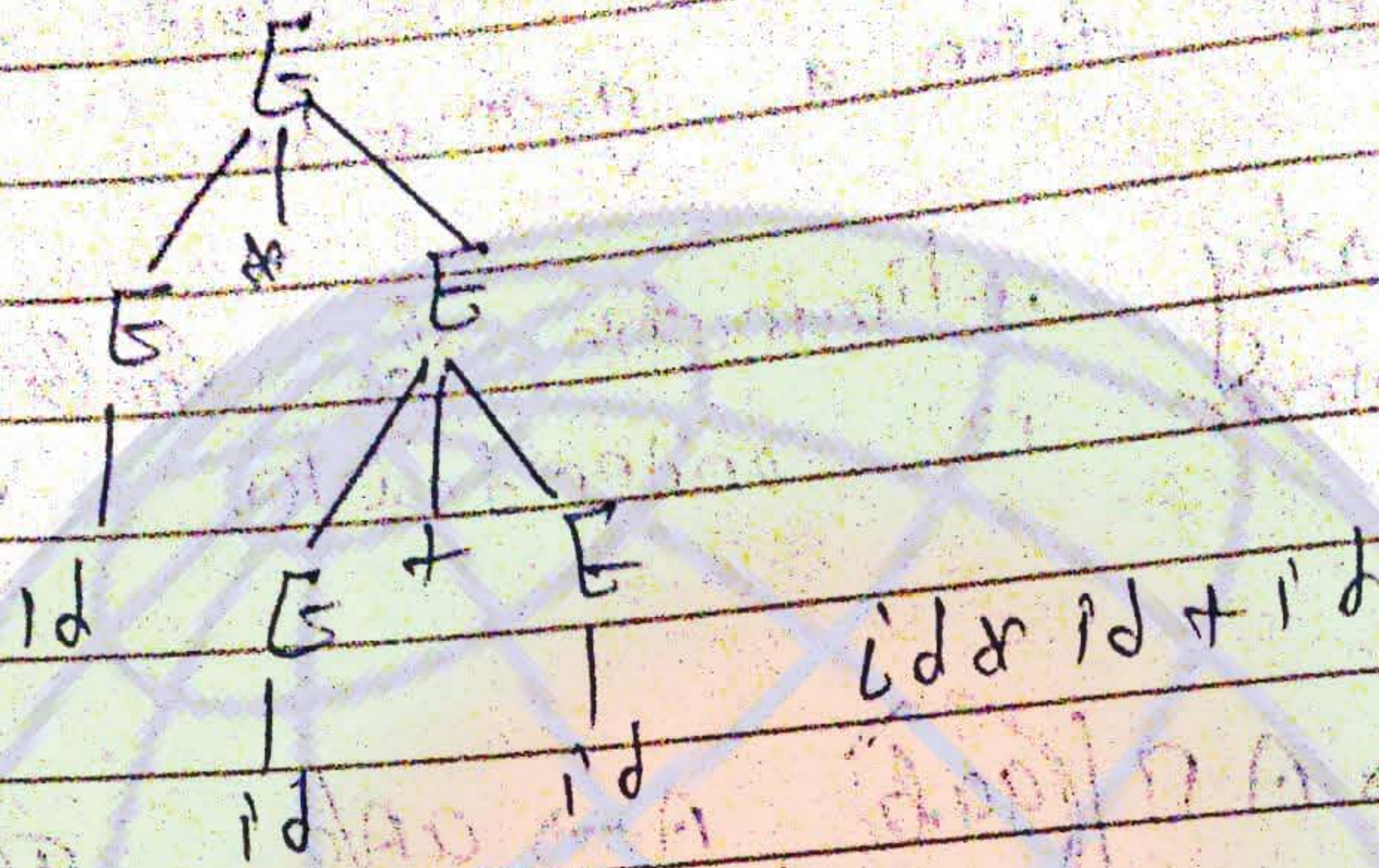
&

$G' = \{ S \rightarrow a \}$

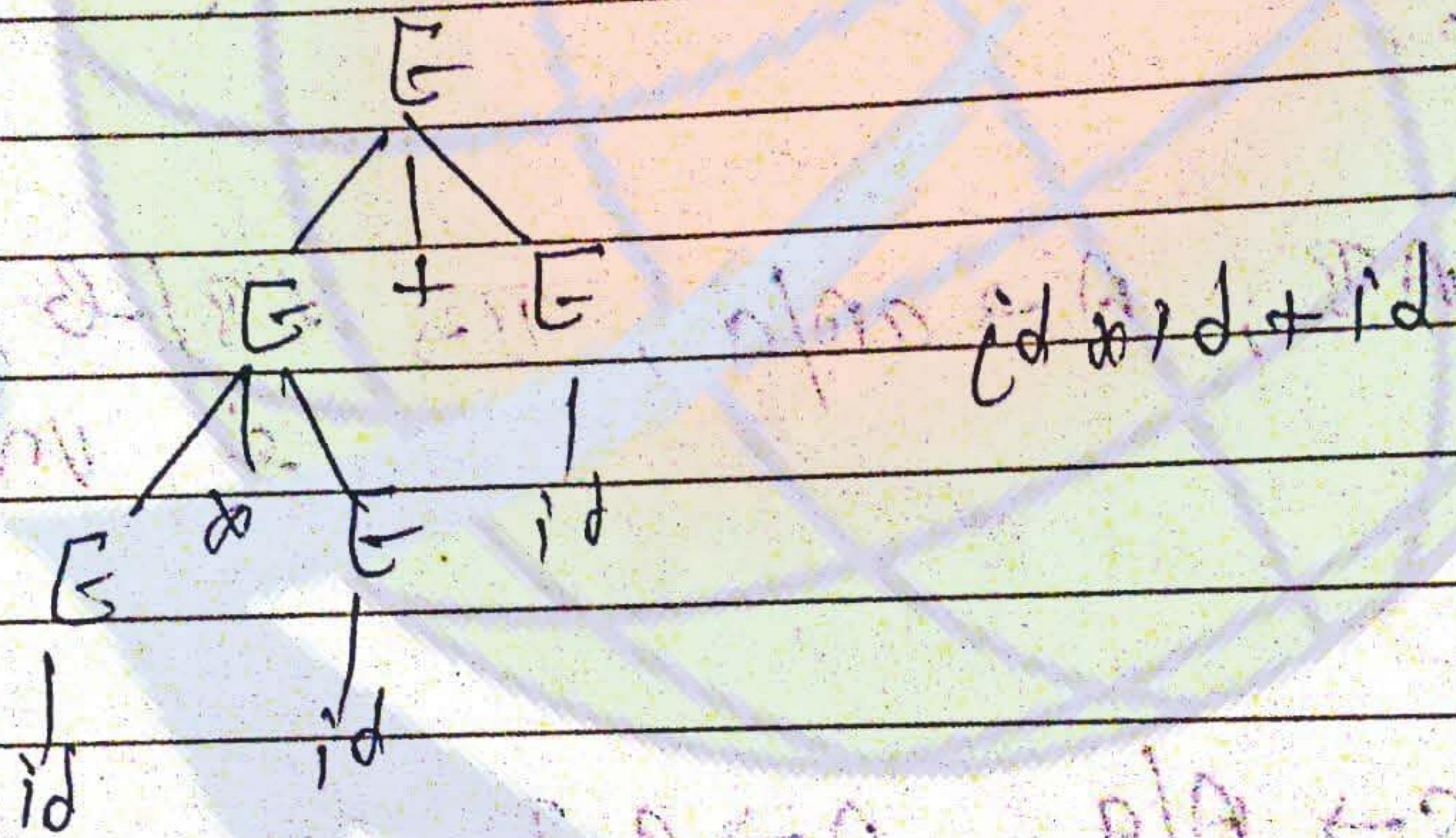
↳ This is unambiguous

Note: If rule is $E \rightarrow E + E / E * E / id$

eg.) $G = \{ E \rightarrow E + E / E * E / id \}$



id + id + id



id + id + id

So, the grammar is ambiguous

Now

$G = \{ E \rightarrow E + T / T$

$T \rightarrow T * F / F$

$F \rightarrow id \}$

This is unambiguous grammar

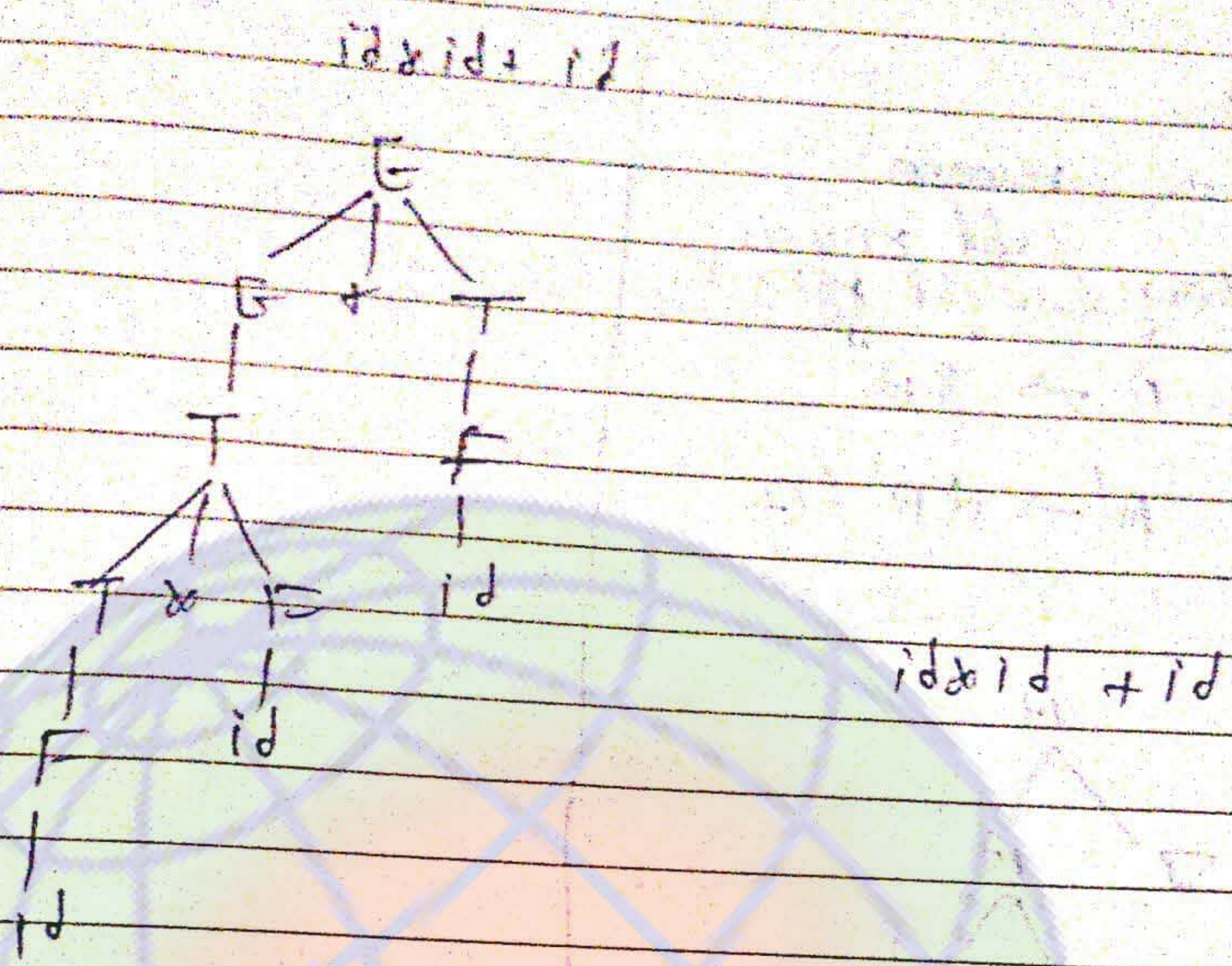
which gives all the string as above.

#

left

A

the part may not be possible to put



Recursion Context free grammar

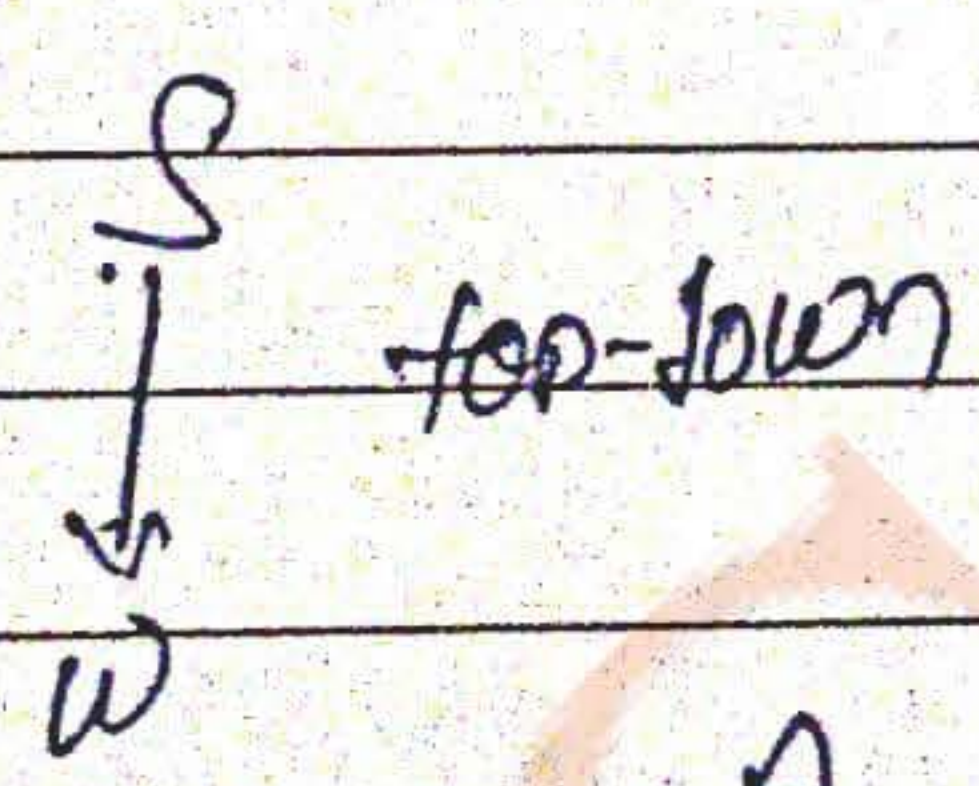
Left recursive CFG

Right recursive CFG

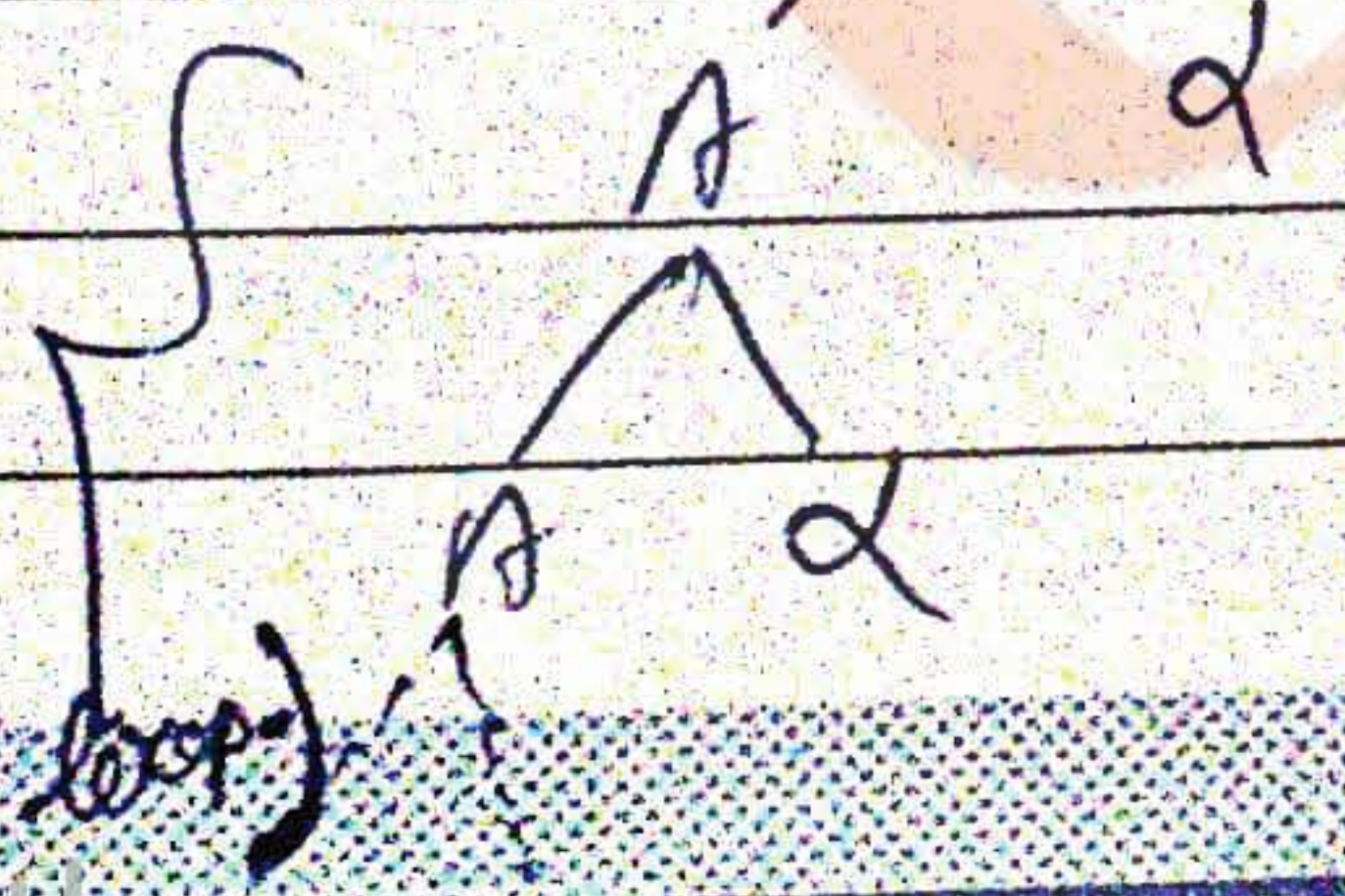
$$A \rightarrow A\alpha / \beta$$

$$A \rightarrow \alpha A / \beta$$

$$\begin{aligned}
 A &\rightarrow A\alpha \\
 &\rightarrow A\alpha A \\
 &\rightarrow \beta\alpha\alpha
 \end{aligned}$$



The parser may not decide where to put β and go into infinite loop.



eg.) $G_1 = \{ A \rightarrow AA_1 / AA_2 \dots / A A_n / \epsilon, / A_1, / A_2, \dots, / A_n \}$
 This is left recursive

To eliminate this
 The formulas:-
 $G_1 = \{ A \rightarrow \nabla A' / \nabla_2 A' / \nabla_3 A' / \dots / \nabla_n A \}$
 $A' \rightarrow \alpha_1 A' / \alpha_2 A' / \dots / \alpha_n A' / \epsilon \}$
 Left recursion removed

a) eliminate the left recursion from the following grammar

$$G_1 = \{ S \rightarrow Sa | Sb | a | b \}$$

S/1

$$G_1 = \{ S \rightarrow \underbrace{Sa}_{A \alpha_1} / \underbrace{Sb}_{A \alpha_2} / \underbrace{a}_{\nabla_1} / \underbrace{b}_{\nabla_2} \}$$

$$G_1' = \{ S \rightarrow aS' / bS' \}$$

$$S' \rightarrow aS' / bS' / \epsilon \}$$

a) eliminate the left recursion from the

$$G_1 = \{ S \rightarrow AaS / b, A \rightarrow ABA / SB S / a \}$$

$$G_1' = \{ S \rightarrow AaS / b, A \rightarrow \underbrace{ABA}_{A \alpha_1} / \underbrace{AaS}_{A \alpha_2} / \underbrace{bS}_{\nabla_1} / \underbrace{a}_{\nabla_2} \}$$

$$G_1'' = \{ S \rightarrow AaS / b, A \rightarrow bBA' / aA', A' \rightarrow bBA' / aSBA' / \epsilon \}$$

* Left factor :-

$$G = \{ A \rightarrow \alpha P_1 / \alpha P_2 / \dots / \alpha P_n \}$$

- same prefix common,



Now, remove left ~~prefix~~ common factors,

$$G' = \{ A \rightarrow \alpha A' \}$$

$$A' \rightarrow P_1 / P_2 / \dots / P_n \}$$

Note The above was problem with top-down parser.

$$* G = \{ S \rightarrow \alpha A \beta / \alpha A \gamma / \beta, A \rightarrow a \}$$

~~$$G' = \{ S \rightarrow \alpha A' \}$$

$$A' \rightarrow \beta / \gamma$$~~

$$G' = \{ S \rightarrow \alpha A \beta' / \beta, A' \rightarrow \alpha / \beta, A \rightarrow a \}$$

$$* G = \{ S \rightarrow \alpha A \beta / \alpha A \gamma / \alpha A \delta, A \rightarrow \alpha A / 1 \}$$

$$G' = \{ S \rightarrow \alpha S' / \alpha A \beta / \alpha A \gamma / \alpha A \delta, A \rightarrow \alpha A / 1 \}$$

$$S' \rightarrow \alpha A \beta / \alpha A \gamma / \alpha A \delta$$



Par

Top-down parsing

with Backtrack

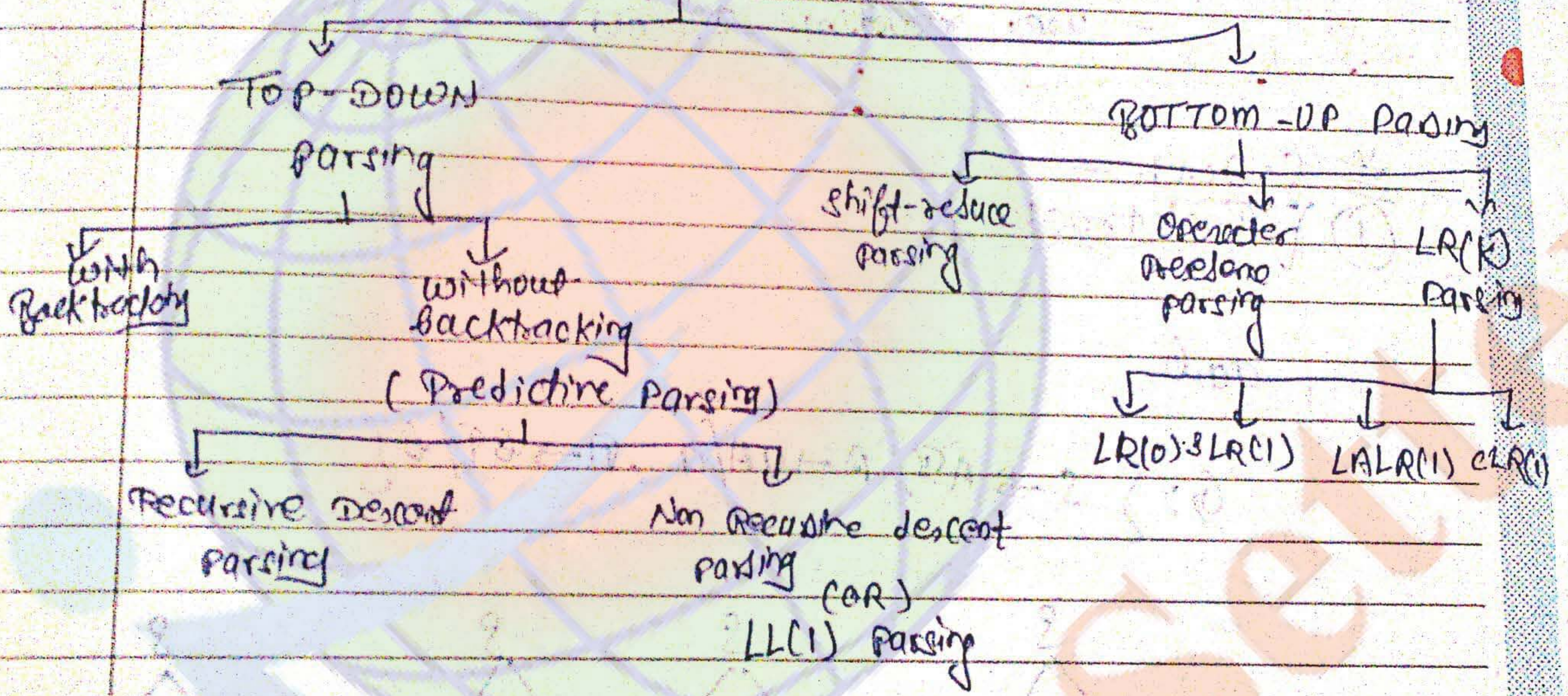
Recursive Descent parsing

① TOP

$$G'' = \{ S \rightarrow OS', A \rightarrow OA, \\ S' \rightarrow IS' \mid \emptyset \\ S'' \rightarrow AS'' \mid \emptyset \}$$



Parsing:-



① ● Top-down parsing : (from root to leaf)

- uses left most derivation (LMD)

$$G = \{ S \rightarrow AB \\ A \rightarrow AA/a \\ B \rightarrow BB/b \}$$

$$\begin{array}{c} S \\ \hline AB \\ \hline aAB \\ \hline aaB \\ \hline aab \end{array}$$

- uses derivation process.

(ii) Bottom-up parser (also known as LR parser)

~~aaab~~
~~oAb~~
~~A~~
~~AD~~
~~S~~

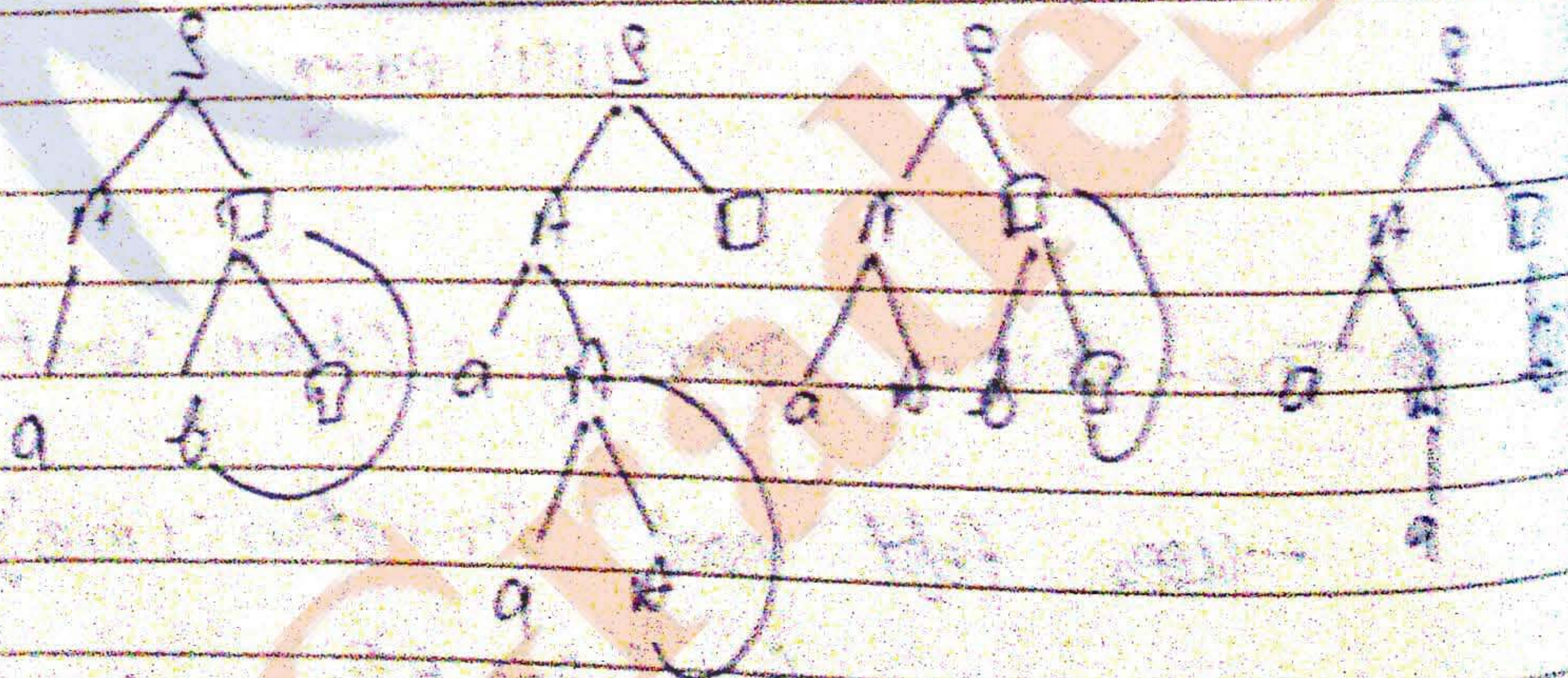
- Uses right most derivation (RMD) in reverse

- Uses reduction process

* (ii) Breadth-First Search (BFS) -
 (1) Backtracking:-

aaab

G: $\{ S \rightarrow AB, A \rightarrow aA/a, B \rightarrow bB/b \}$



Backtracking is a process of trying different productions until it gets the required string. If the grammar is having too many productions and if the string is also too long...

large, then the parser has to ~~try~~ try, so many productions.

because of these several tries the parser will become slow. that is why we don't prefer backtracking.

* FIRST set :-

~~First~~ FIRST(A) - the set of ~~FIRST~~ "FIRST" is the set of ~~FIRST~~

$A \rightarrow \ominus - / \ominus - / \ominus - / \ominus - / \ominus -$

$A \rightarrow \underline{a} a / \underline{a}$ $\text{first}(A) = a$

ab / a $\text{first}(A) = a$

ab / c a, c

aA / c a, c

aA a

$A \rightarrow \underline{a} A / c$

$A \rightarrow B C$

$B \rightarrow b D / b$

$\text{first}(A) = \text{set of } \text{first}(B)$
(it should not be ϵ)
 $= \{b\}$

$A \rightarrow sBC$

$D \rightarrow bD/\epsilon$
 $First(D) = \{b, \epsilon\}$

$First(A) = First(D)$

~~$= \{b, \epsilon\} \cup First(C)$~~

Procedure - "FIRST" निकालने का तरीका

1. $First(a) = \{a\}$
- 2) If $A \rightarrow a \Rightarrow First(A) = \{a\}$
- 3) If $A \rightarrow \epsilon \Rightarrow First(A) = \{\epsilon\}$
- 4) If $A \rightarrow BC \Rightarrow First(A) = First(B)$ if $First(B)$ does not contain ϵ .
- 5) If $A \rightarrow BC \Rightarrow First(A) = First(B) \cup \{\epsilon\} \cup First(C)$

If B also have ϵ

Q) * Find the first of each non-terminal of the following grammar

$S \rightarrow ABC$	$First$
$A \rightarrow aA/b$	$\{a, b\}$
$B \rightarrow BB/\epsilon$	$\{a, b\}$
$C \rightarrow CC/\epsilon$	$\{b, \epsilon\}$
	$\{\epsilon, \epsilon\}$

Note: Better to start from the bottom

R₁ (V₁)
R₂

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- FMN(S) = {a, b}
- FMN(W) = {a, b}
- FMN(M) = {b, c}
- FMN(C) = {c, d}

{a, b, c, d}

- (ii) G = { S → ABC
A → aA/e
B → bB/c
C → cC/d }

- FMN(S) = {a, b, c, d}
- FMN(A) = {a, e}
- FMN(B) = {b, c}
- FMN(C) = {c, d}

- 3) G = { E → TE'
E' → +TE'/e
T → FT'
T' → *FT'/e
F → [E]/id }

- FMN(E) = { [, id }
- FMN(E') = { +, e }
- FMN(T) = { [, id }
- FMN(T') = { *, e }
- FMN(F) = { [, id }

- 4) G = { S → ACB / eB / Ba
A → da / BC
B → g / e
C → h / e }

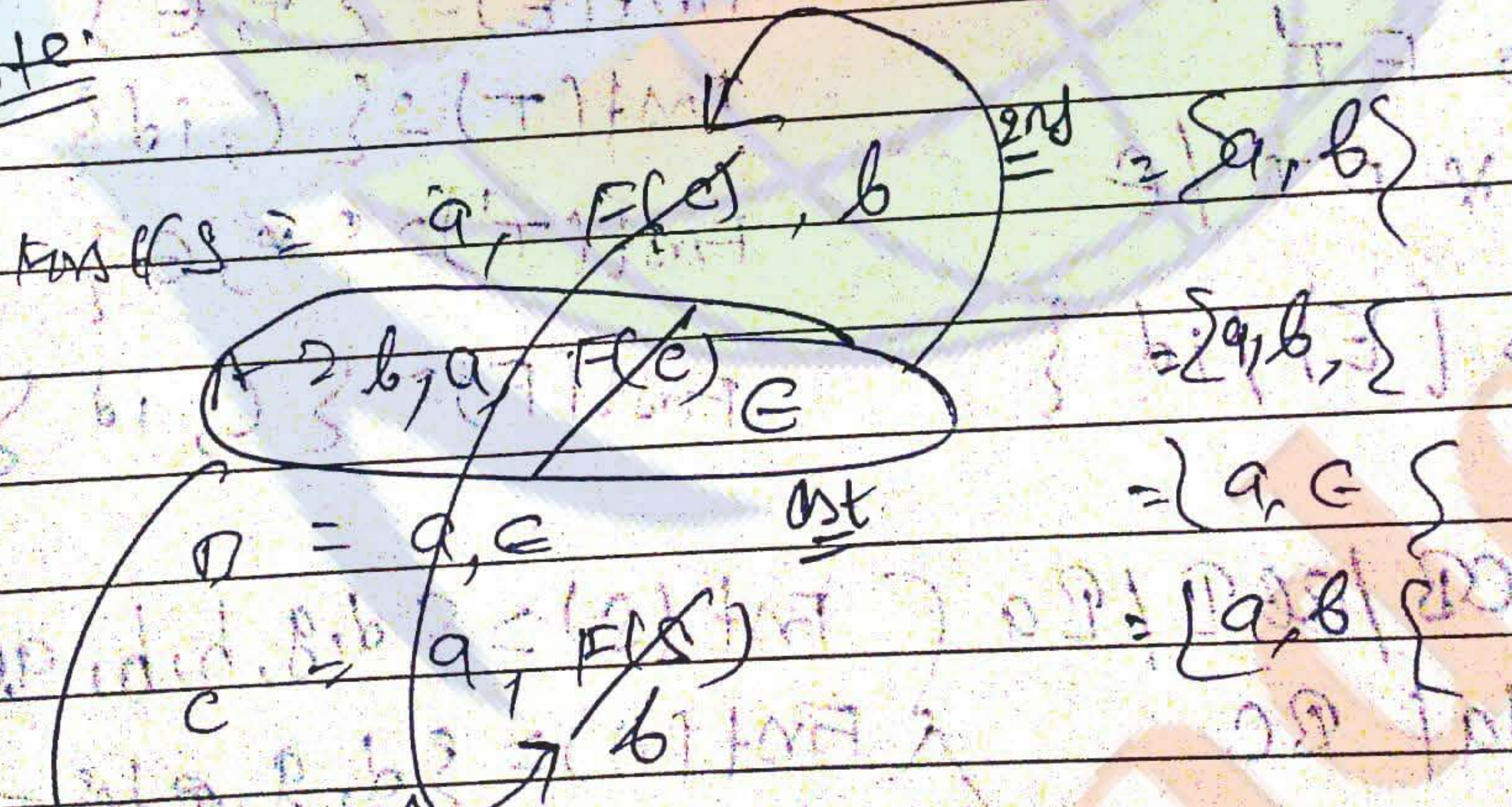
- FMN(S) = { d, g, h, b, a, e }
- FMN(A) = { d, g, h, e } = { g, h, e } ∪ {d}
- FMN(B) = { g, e }
- FMN(C) = { h, e }

R₂

$S \rightarrow AaB / bC$
 $A \rightarrow BC / bA$
 $B \rightarrow aB / \epsilon$
 $C \rightarrow a / SA$

$Final(S) = \{ \cancel{b}, \cancel{a}, \{a, b\} \}$
 $Final(A) = \{ \cancel{a}, \cancel{b}, \{a, b\} \}$
 $Final(B) = \{a, \epsilon\}$
 $Final(C) = \{ \cancel{a}, \cancel{b}, \{a, b\} \}$

Note



stack इन चयों पर केवल ϵ terminal
 के a, b इंग्रों ϵ ही अंकन है तो
 $Final(C)$ को ϵ से replace कर देवें
 कि इसके बाक सभी को ϵ कर लेंगे।

Q) $G = \{$
 $S \rightarrow abs / BA / e$
 $A \rightarrow BC$
 $D \rightarrow ab / Ac / e$
 $C \rightarrow cC / d$
 $\}$

$\{a, b, e\}$
 $\{First(S) = \{a, b, e\}\}$
 $\{a, c, d\}$
 $\{e, d\}$

$First(S) = \{a, b, e\}$
 $First(A) = \{a, c, d\}$

$First(D) = \{a, c\} \cup First(A) = \{a, c, d, e\}$
 $First(e) = \{e\}$

Q) Consider the following grammar
 $S \rightarrow ABC$

Let the no. of elements in $First(A)$, $F(D)$, $F(C)$ are 3, 4, 5 respectively.

~~All these~~ $First$ of all these contains ϵ , and the remaining all symbols are different then the no. of elements in $F(S)$ is

50/9

$S \rightarrow ABC$

$F(S) = \{a, b, c, d, e\}$
 $F(A) = \{a, b\}$
 $F(D) = \{a, b, c, d, e\}$
 $F(C) = \{c, d, e\}$
 $+ \epsilon = 10$ Any

Follow set:

(10)

$$S \rightarrow ABCD$$

$$\text{Follow}(A) = \text{First}$$

Follow of (A) is the set of terminals, that presents immediately to the right side of (A), whenever (A) is on the right side of the arrow

Procedure: "Follow निकालने का आसान तरीका"

1) $\text{Follow}(S) = \{ \$ \}$

2) If $A \rightarrow \alpha B \gamma \Rightarrow \text{Follow}(B) = \text{First}(\gamma)$ if $\text{First}(\gamma)$ does not contain ϵ .

3) If $A \rightarrow \alpha B \gamma \Rightarrow \text{Follow}(B) = \text{First}(\gamma) - \{ \epsilon \} \cup \text{Follow}(A)$

4) If $A \rightarrow \alpha B \Rightarrow \text{Follow}(B) = \text{Follow}(A)$

Ex) Find the follow of each non-terminal of the following grammar.

① $G_1 = \{ S \rightarrow \underline{A} \underline{a} \underline{A} \underline{b} \mid \underline{B} \underline{b} \underline{B} \underline{a} \}$

$A \rightarrow aA \mid \epsilon$

$B \rightarrow bB \mid \epsilon$

	First	Follow
$S \rightarrow$	$\{ a, b, \epsilon \}$	$\{ \$ \}$
$A \rightarrow$	$\{ a, \epsilon \}$	$\{ a, b \}$
$B \rightarrow$	$\{ b, \epsilon \}$	$\{ b, \epsilon \}$ or $\{ a, b \}$

2) $S \rightarrow ABC$
 $A \rightarrow aA/b$
 $B \rightarrow bB/c$
 $C \rightarrow a.cC/a$

$Follow(S) = \{ \$ \}$
 $Follow(A) = \{ b, a, c \}$
 $Follow(B) = \{ c, a \}$
 $Follow(C) = \{ \$ \}$

3) $E \rightarrow E+T$
 IT
 $T \rightarrow T * F$
 IF
 $F \rightarrow (E)$
 $/id$

$Follow(E) = \{ +,), \$ \}$
 $Follow(T) = \{ +, *,), \$ \}$
 $Follow(F) = \{ +, *,), \$ \}$

4) $S \rightarrow ACB/CB/CB$
 $A \rightarrow da/BOC$
 $D \rightarrow g/E$
 $E = h/E$

$Follow(S) = \{ \$ \}$
 $Follow(A) = \{ h, g, \$ \}$
 $Follow(B) = \{ \$, g, h, g \}$
 $Follow(C) = \{ g, \$, h, g \}$

$\{ g, \$ \} \cup \{ \$, h, g \}$
 $\{ h, \$ \} \cup \{ g, \$ \} \cup \{ \$ \}$
 $\{ \$ \} \cup \{ g \} \cup \{ h, \$ \}$

↓ work a head of
 ↓ uses LMD
 ↓ Left to right scan of the input string

Construction of LL(1) Parsing table:

1) we must consider every production of the form

$$A \rightarrow \alpha$$

and we proceed as follows

1) we write $A \rightarrow \alpha$ in

$M[A, x]$ where $x \in \text{First}(\alpha)$

2) If $\text{First}(\alpha) = \{ \epsilon \}$
 then

write $A \rightarrow \alpha$ in $M[A, y]$

where $y \in \text{Follow}(A)$

3) If all the entries in the table are single then the grammar LL(1)

* LL(1) :-
 was a head symbol of length 1
 uses LMD
 Left to right scan of the input string

Construction of LL(1) Parsing table :-

1) we must consider every production of the form

$$A \rightarrow \alpha$$

and we proceed as follows

1) we write $A \rightarrow \alpha$ in

$$M[A, x] \text{ where } x \in \text{First}(\alpha)$$

2) If $\text{First}(\alpha) = \{\epsilon\}$

then

$$\text{write } A \rightarrow \alpha \text{ in } M[A, y]$$

where $y \in \text{Follow}(A)$

3) If all the entries in the table are single then the grammar LL(1)

	a	b	ε
S	$S \rightarrow AA$	$S \rightarrow bA$	syntactical error
A	$A \rightarrow aA$	$A \rightarrow b$	syntactical error
ε	syntactical error	$\epsilon \rightarrow b\epsilon$	$\epsilon \rightarrow \epsilon$

Here, there are only single entries, so this is LLL(1).

In the above table, all the entries are single.

Q) Construct the LLL(1) parsing table for the following grammar

$$G = \{ E' \rightarrow TE' \\ E' \rightarrow +TE' / \epsilon \\ T \rightarrow FT' \\ T' \rightarrow *FT' / \epsilon \\ F \rightarrow (E) / id \}$$

	+	*	()	id	ε
E			$E \rightarrow TE'$			$E \rightarrow \epsilon$
E'	$E' \rightarrow +TE'$		$E' \rightarrow \epsilon$			
T			$T \rightarrow FT'$			$T \rightarrow \epsilon$
T'	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow)$		$T' \rightarrow \epsilon$
F			$F \rightarrow (E)$			$F \rightarrow id$

$$T' \rightarrow E$$

$$\text{Follow}(T) = \text{follow}(T)$$

$$= \text{FIRST}(E')$$

$$= \{+, *, \uparrow, \downarrow, \beta\}$$

$$= \{+, \uparrow, \beta\}$$

In the above table, all the entries are single, therefore the grammar is LL(1).

Stack	I/O Buffer	Action
\$ E	id + id * id #	Push by E → TE'
\$ E T'	id + id * id #	Push by T → FT'
\$ E T' F	id + id * id #	Push by F → id
\$ E T' id	id + id * id #	POP
\$ E T'	+ id * id #	Push by T' → G
\$ E'	+ id * id #	Push by E' → +TE'
\$ E T +	+ id * id #	POP
\$ E T	id * id #	Push by T → FT'
\$ E T F	id * id #	Push by F → id
\$ E T id	id * id #	POP
\$ E T	* id #	Push by T → FT'
\$ E T F *	* id #	POP
\$ E T F	id #	Push by F → id
\$ E T id	id #	POP

$$T' \rightarrow G$$

$$\text{Follow}(T) = \text{Follow}(T')$$

$$= \text{FIRST}(E')$$

$$= \{ +, *, \epsilon, \} \cup \{ \epsilon, \}$$

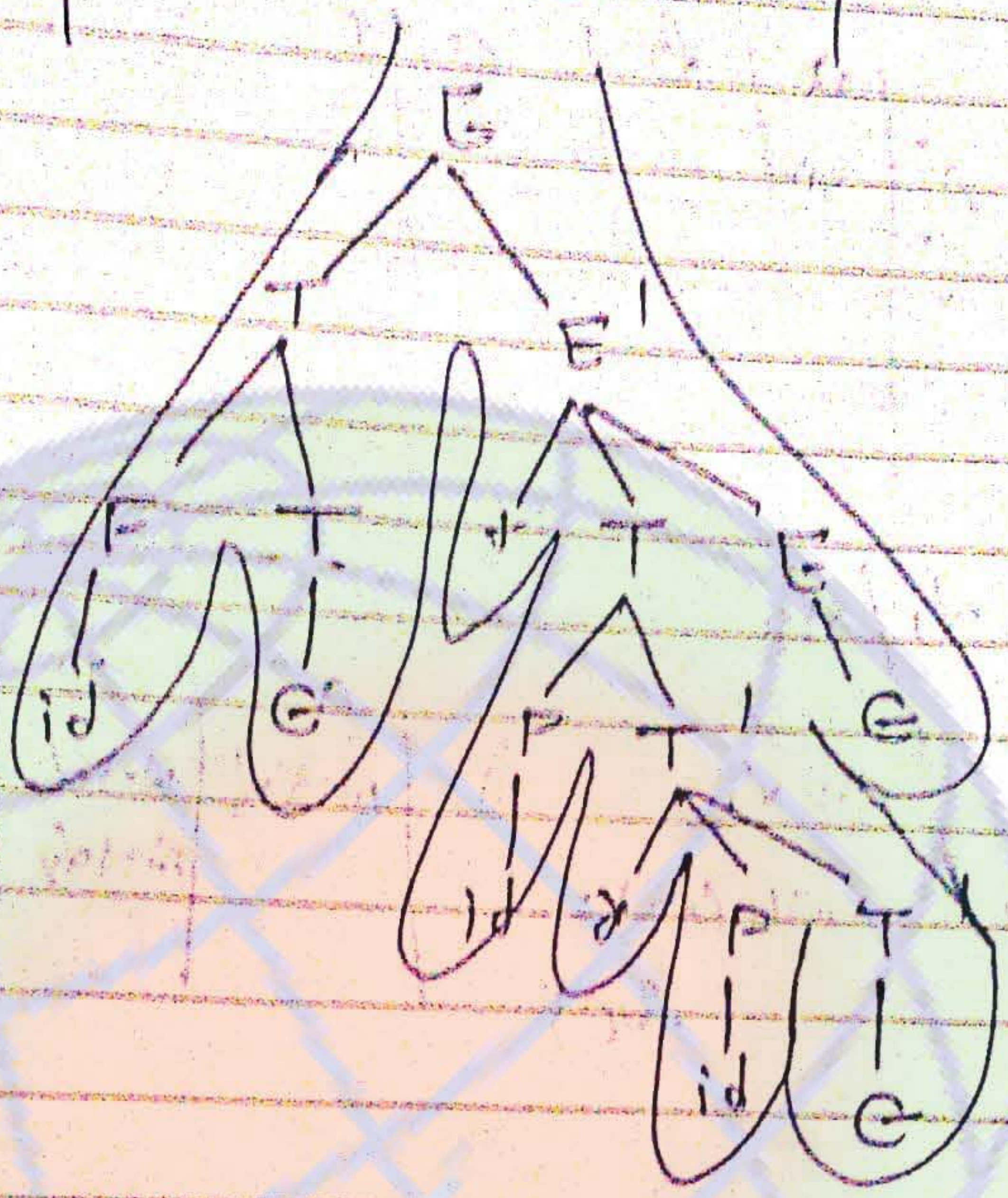
$$= \{ +, *, \epsilon \}$$

In the above table, all the entries are single, therefore the grammar is LL(1).

Stack	I/O Buffer	Action
\$ E	id + id * id \$	Push by $E \rightarrow TE'$
\$ E T'	id + id * id \$	Push by $T \rightarrow FT'$
\$ E T' F	id + id * id \$	Push by $F \rightarrow id$
\$ E T' id	id + id * id \$	POP
\$ E T'	+ id * id \$	Push by $T' \rightarrow G$
\$ E'	+ id * id \$	Push by $E' \rightarrow +TE'$
\$ E T +	+ id * id \$	POP
\$ E T	id * id \$	Push by $T \rightarrow FT'$
\$ E T F	id * id \$	Push by $F \rightarrow id$
\$ E T id	id * id \$	POP
\$ E T	* id \$	Push by $T \rightarrow FT'$
\$ E T F	* id \$	POP
\$ E T F	id \$	Push by $F \rightarrow id$
\$ E T id	id \$	POP

E' T'
E'
#

push by T L E
push by E L E
Accept



Properties of LL(1) grammar:-

1) A left recursive grammar is not LL(1).

$$\{ E \rightarrow E + E / id \}$$

↳ not LL(1) because left recursive

2) A left factor grammar is not LL(1)

eg. ↳ two or more prefix

$$S \rightarrow \underline{A} B / A \underline{C} \rightarrow \text{not LL(1)}$$

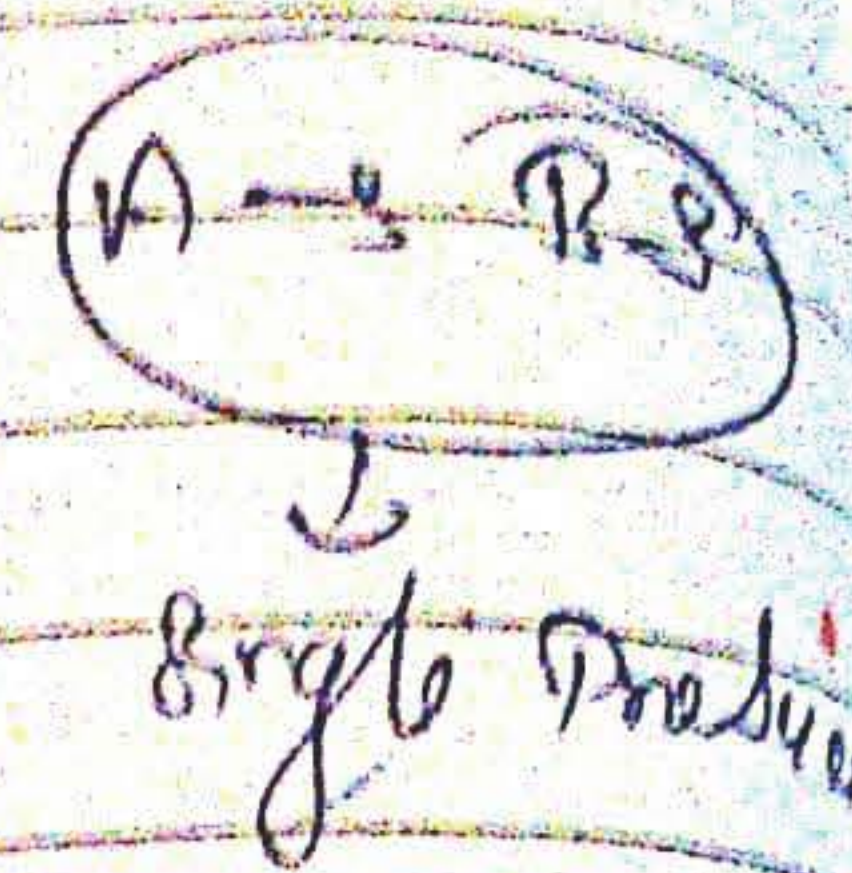
3) An Ambiguous grammar is not LL(1)

4) Every LL(1) grammar is Unambiguous.

but every Unambiguous grammar is not LL(1)

5) Every single production grammar is LL(1).

	a	b	c	f
A				
B				



6)

$A \rightarrow \alpha_1 / \alpha_2$

$A \rightarrow \alpha_1$ $A \rightarrow \alpha_2$

$First(\alpha_1) = \{a, b\}$ $First(\alpha_2) = \{ \epsilon, b, c \}$

	a	b	c	f
A	$A \rightarrow \alpha_1$	$A \rightarrow \alpha_1$ $A \rightarrow \alpha_2$	$A \rightarrow \alpha_2$	

If any productions are of the form

$A \rightarrow \alpha_1 / \alpha_2$ then

If $First(\alpha_1) \cap First(\alpha_2) \neq \emptyset$

\Rightarrow Not LL(1)

Note:

If any production are of the form

$A \rightarrow \alpha_1 / \alpha_2 / \alpha_3 / \dots / \alpha_n$

then

If any two have common elements then it is not LL(1)

if any productions are of the form

$$A \rightarrow \alpha / G$$

then

$$\text{if } \text{First}(\alpha) \cap \text{Follow}(A) \neq \phi$$

\Rightarrow Not LL(1)

e.g) $G = \{ S \rightarrow AA, A \rightarrow a \}$

sln $S \Rightarrow a/a$

$$\text{First}(A) \cap \text{First}(a)$$

$$= \{a\} \cap \{a\}$$

$$= \{a\}$$

$$= a$$

$=$ not empty

so not LL(1)

e.g) $G = \{ S \rightarrow aA / bB / a \}$

$$A \rightarrow G$$

$$B \rightarrow G$$

$$\cap \neq \emptyset$$

so not LL(1)

sln

not LL(1)

so Ambiguous

$$\text{First}(aA) \cap \text{First}(a)$$

$$\{a\} \cap \{a\}$$

$$\neq \phi$$

so, not LL(1)

Q3) $G = \{S \Rightarrow ABC$
 $A \rightarrow aA/e,$
 $B \rightarrow bB/e$
 $C \rightarrow cC/e\}$

Q4) $LL(1)$

$$FIRST(A) \cap FOLLOW(A)$$

$$= \{a\} \cap \{b, c, \epsilon\}$$

$$= \emptyset$$

(No common)

so $LL(1)$

$$FIRST(B) \cap FOLLOW(B)$$

$$= \{b\} \cap \{c, \epsilon\}$$

$$= \emptyset$$

$$FIRST(C) \cap FOLLOW(C)$$

$$= \{c\} \cap \{c\}$$

$$= \{c\}$$

Q4) $G = \{S \Rightarrow ABC$

10/17

Q5) check not

10/17

Q4) ~~Q3~~
 $G = \{ S \rightarrow aS / bA, A \rightarrow aSA / bA / \epsilon \}$

soln

$First(aS) \cap First(bA)$ $\{ a \} \cap \{ b \}$ $= \phi$	$= First(aSA) \cap First(bA)$ $\cap Follow(A)$ $= \{ a \} \cap \{ b \} \cap \{ a, b, \epsilon \}$ $\neq \phi$ $= \text{Not LL(1)}$
--	--

Q5) check whether the following grammar is LL(1) or not and also find the entries of

$m[s', e]$ & $m[E, a]$

in the corresponding parsing table

$G = \{ S \rightarrow i E \mid SS', a, S' \rightarrow eS / \epsilon, E \rightarrow b \}$

soln

$First(iE \mid SS') \cap First(a)$ $\{ i \} \cap \{ a \}$ $= \phi$	$First(eS) \cap Follow(S')$ $\{ e \} \cap \{ e, \epsilon \}$ $\neq \phi$
--	--

$Follow(S) \cup First(S')$
 $= \{ e, \epsilon, \epsilon \} \cup \{ a \}$
 $= \{ e, \epsilon, a \}$

\leftarrow Not LL(1)

Q4) ~~Q3~~

$$G = \{ S \rightarrow a^2 / bA, A \rightarrow a^2A / bA / \epsilon \}$$

soln

$$\text{First}(a^2) \cap \text{First}(bA)$$

$$\{ a^2 \} \cap \{ b \}$$

$$= \emptyset$$

$$= \text{First}(a^2A) \cap \text{First}(bA)$$

$$\cap \text{Follow}(A)$$

$$= \{ a^2 \} \cap \{ b \} \cap \{ a, b, \epsilon \}$$

$$\neq \emptyset$$

Not LL(1)

Q5) check whether the following grammar is LL(1) or not and also find the entries of

$$M[S', \epsilon] \text{ \& } M[E, a]$$

in the corresponding parsing table

$$G = \{ S \rightarrow i E \mid S S', S' \rightarrow \epsilon S / \epsilon, E \rightarrow b \}$$

soln

$$\text{First}(i E \mid S S') \cap \text{First}(a)$$

$$\{ i \} \cap \{ a \}$$

$$= \emptyset$$

$$\text{First}(\epsilon S) \cap \text{Follow}(S')$$

$$\{ \epsilon \} \cap \{ \epsilon, \$ \}$$

$$\neq \emptyset$$

$$\text{Follow}(S) \cap \text{First}(S')$$

$$= \{ \epsilon, \$ \} \cap \{ \epsilon, \$ \}$$

$$= \{ \epsilon, \$ \}$$

or

Not LL(1)

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	e	z
d	d e e e d e e	d e e e

Ex,

$$m[d, e] = \{d e e e, d e e\}$$

$$m[e, z] = p \quad \leftarrow [e, z]$$

Handle

* Bottom-up Parsing:-

Handle:- A handle is a substring of a string that matched with any of the right side of the productions.
then that handle will be reduced by its left side of the production.

$$G = \{ E \rightarrow E + E \mid E * E \mid id \}$$

Handle Pruning

Right Sentential Form	Handle	Production.
id + id * id	id	$E \rightarrow id$
$E + id * id$	id	$E \rightarrow id$
$E + E * id$	$E + E$	$E \rightarrow E + E$
$E * id$	id	$E \rightarrow id$
$E * E$	$E * E$	$E \rightarrow E * E$
E		

Handle Pruning:- Bottom-up parsing is a process of finding the handles, and using them in the reduction to get the start symbol.

The entire process is called handle pruning.

* Shift Reduce Parsing

In this parsing technique, we use two data structures.

- 1) stack - used to store the symbols of the grammar.

* Bottom-up Parsing:

Handle: - A handle is a substring of a string that matched with any of the right side of the productions.
- then that handle will be reduced by its left side of the production.

$$G = \{ E \rightarrow E + E \mid E * E \mid id \}$$

Handle Pruning

<u>Right Sentential Form</u>	<u>Handle</u>	<u>Production</u>
id + id * id	id	$E \rightarrow id$
$E + id * id$	id	$E \rightarrow id$
$E + E * id$	$E + E$	$E \rightarrow E + E$
$E * id$	id	$E \rightarrow id$
$E * E$	$E * E$	$E \rightarrow E * E$
E		

Handle Pruning: - Bottom-up parsing is a process of finding the handles, and using them in the reduction to get the start symbol.

The entire process is called handle pruning.

* Shift Reduce Parsing:

In this parsing techniques, we use two data structures.

1) Stack - used to store the symbols of the grammar.

The initial configuration of the stack is $\boxed{\$}$

2) Input buffer - used for storing the input string

The initial configuration of the input buffer is $\boxed{w | \$}$

In these techniques we perform four techniques:

- a) shift
- b) Reduce
- c) accept
- d) Error

*) Consider the following grammar and parse the input string $id + id \& id$ using shift reduce parsing

$$E \rightarrow E + E / E * E / id$$

Stack	Input Buffer	Action
$\$$	$id + id \& id \$$	shift
$\$ id$	$+ id \& id \$$	Reduce by $E \rightarrow id$
$\$ E$	$+ id \& id \$$	shift
$\$ E +$	$id \& id \$$	shift
$\$ E + id$	$\& id \$$	Reduce by $E \rightarrow id$
$\$ E + E$	$\& id \$$	shift

$\$ E + E \&$	id $\$$	shift
$\$ E + E \& id$	$\&$	Reduce by $E \rightarrow id$
$\$ E + E \& E$	$\&$	Reduce by $E \rightarrow E + E$
$\$ E + E$	$\&$	Reduce by $E \rightarrow E + E$
$\$ E$	$\&$	Accept

shift = 5
Reduce = 5
accept = 1

Total = 11

Operator Grammar:-

A Grammar is said to be operator grammar, if it satisfy the following two cond.

1) No production should contain adjacent non-terminals on the right side of the arrow.

2) There should not be any null production

eg) $G = \{ E \rightarrow E + E / E \& E / id \}$ is an operator grammar.

eg) $G = \{ S \rightarrow SAS / a, A \rightarrow + / - / \& / / \}$ is not operator grammar.

$G = \{ S \rightarrow S + S / S - S / S \& S / S / S / a \}$ is an operator grammar.

Consider the following grammar and priority relations of the following grammar

$$G = \{ E \rightarrow E + E / E * E / id \}$$

	id	*	+	\$
id	-	>	>	>
*	<	>	>	>
+	<	<	>	>
\$	<	<	<	-

Note: this dot is known as priority relation.

* Operator Precedence Parsing:-

Construction of operator precedence parsing table -

*) Let x is the top most symbol in the stack and y is the present input symbol in the input buffer, then we proceed as follows.

- 1) If $x < y$ then perform shift operation
- 2) If $x > y$ then there will be a handle in the stack

then perform reduce operation with a proper production.

a) Consider the following grammar

$$G = \{ E \rightarrow E - E / E * E / id \}$$

$$id \rightarrow id * id$$

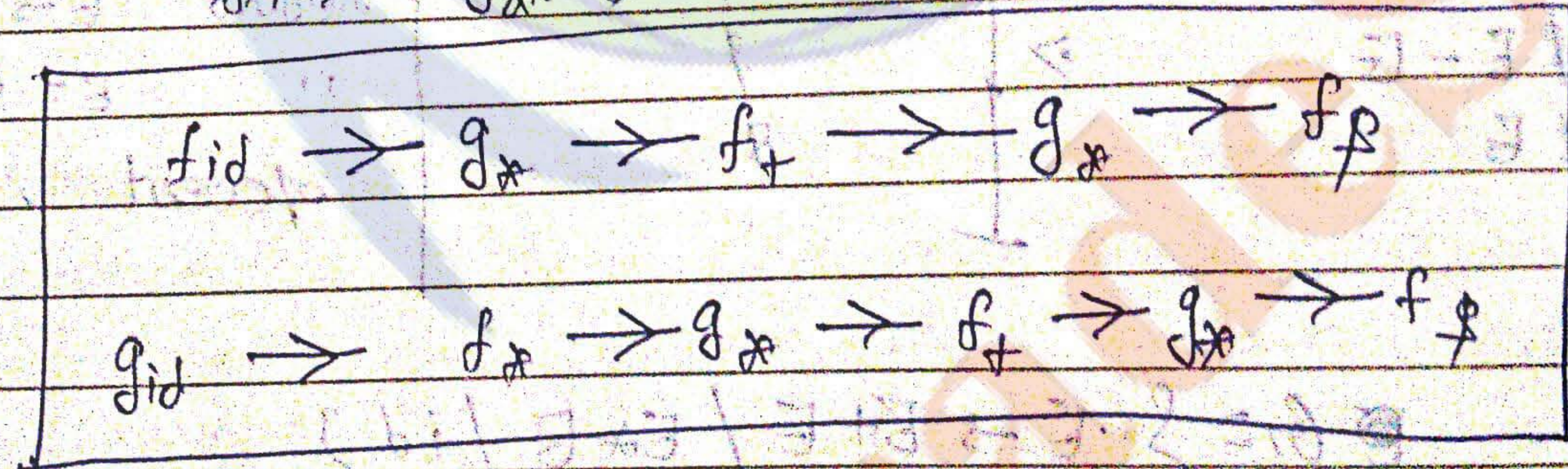
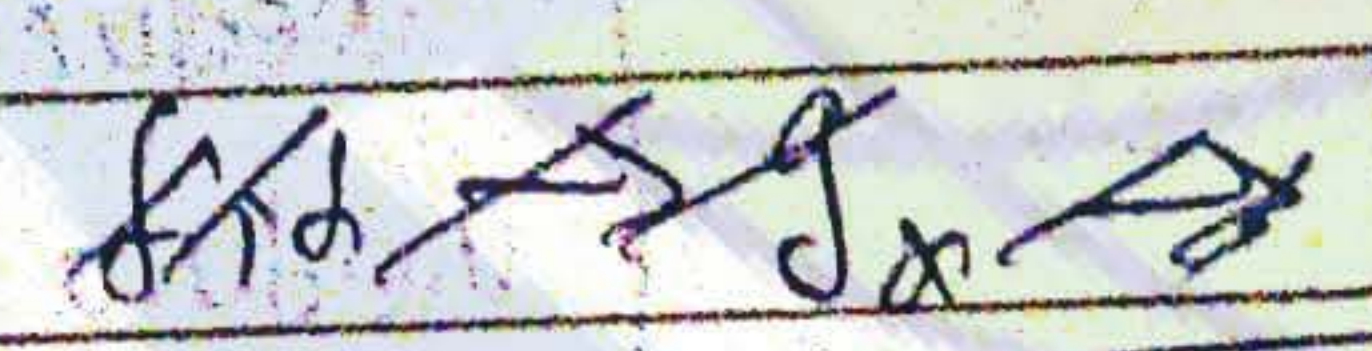
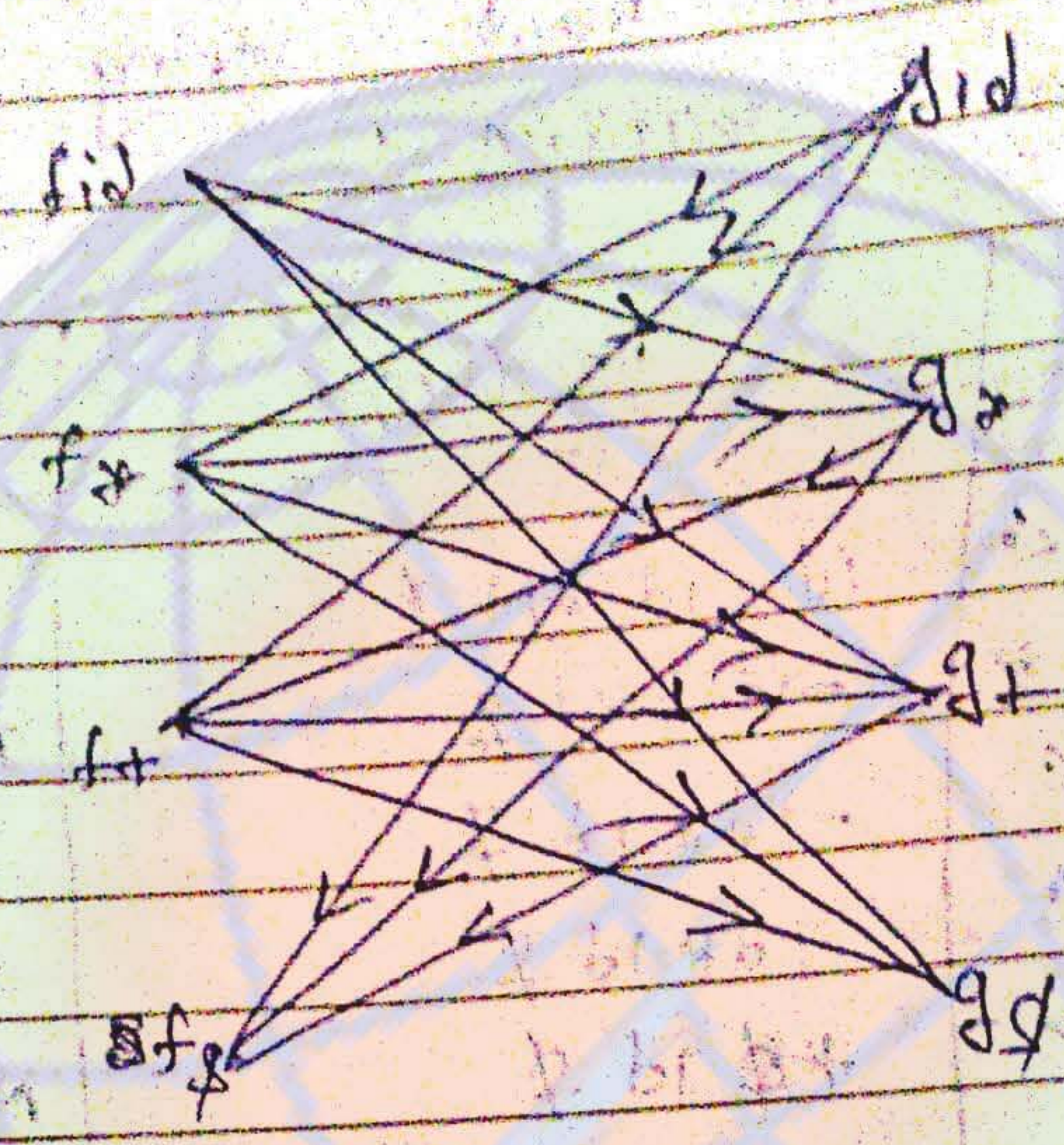
and parse the input string using operator precedence parsing

Stack		ifo buffer	Action
\$	<	id - id * id \$	shift
\$ id	>	- id * id \$	Reduce by $E \rightarrow id$
\$ E	<	- id * id \$	shift
\$ E -	<	id * id \$	shift
\$ E - id	>	* id \$	Reduce $E \rightarrow id$
\$ E - E	<	* id \$	shift
\$ E - E *	<	id \$	shift
\$ E - E * id	>	\$	Reduce $E \rightarrow id$
\$ E - E * E	>	\$	Reduce $E \rightarrow E * E$
\$ E - E	>	\$	" $E \rightarrow E - E$
\$ E		\$	accept

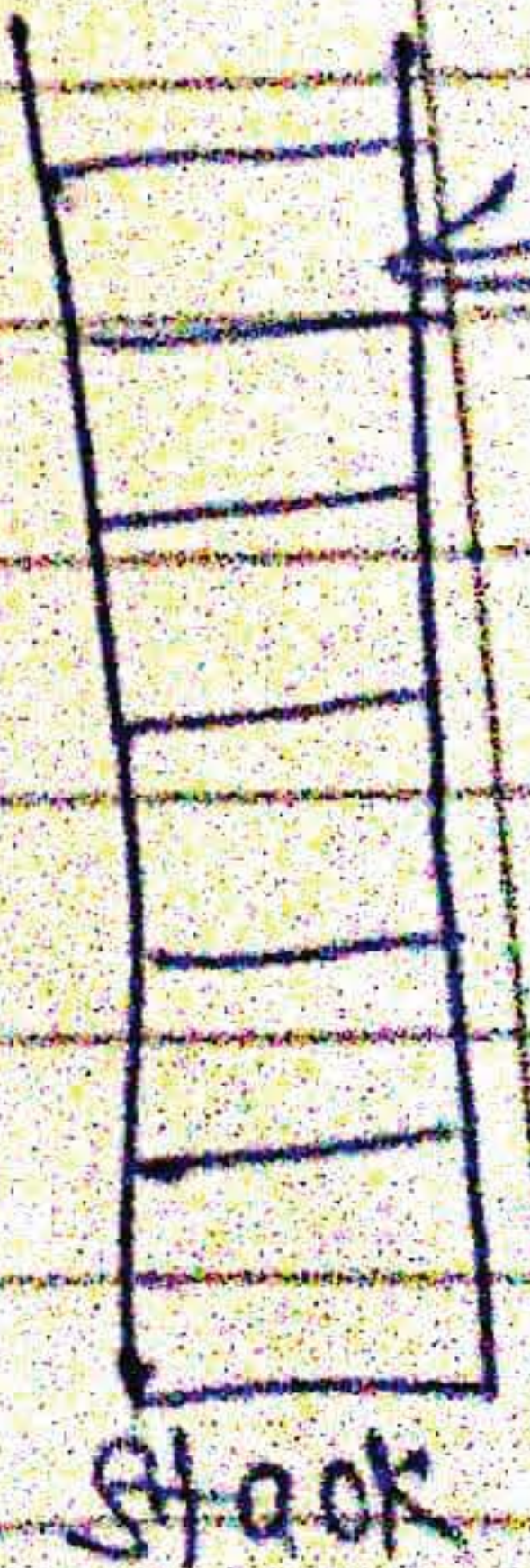
* $G = \{ E \rightarrow E + E / E * E / id \}$

\$	\$	id +	* *	+ +	\$
id	-	>	>	>	>
*	<	>	>	>	>
+	<	<	>	>	>
\$	<	<	<	<	-

The size of the operator relationship table
 is $O(n^2)$
 where n is number of operators.



	fid	*	+	\$
f	4	4	2	0
g	5	3	1	0



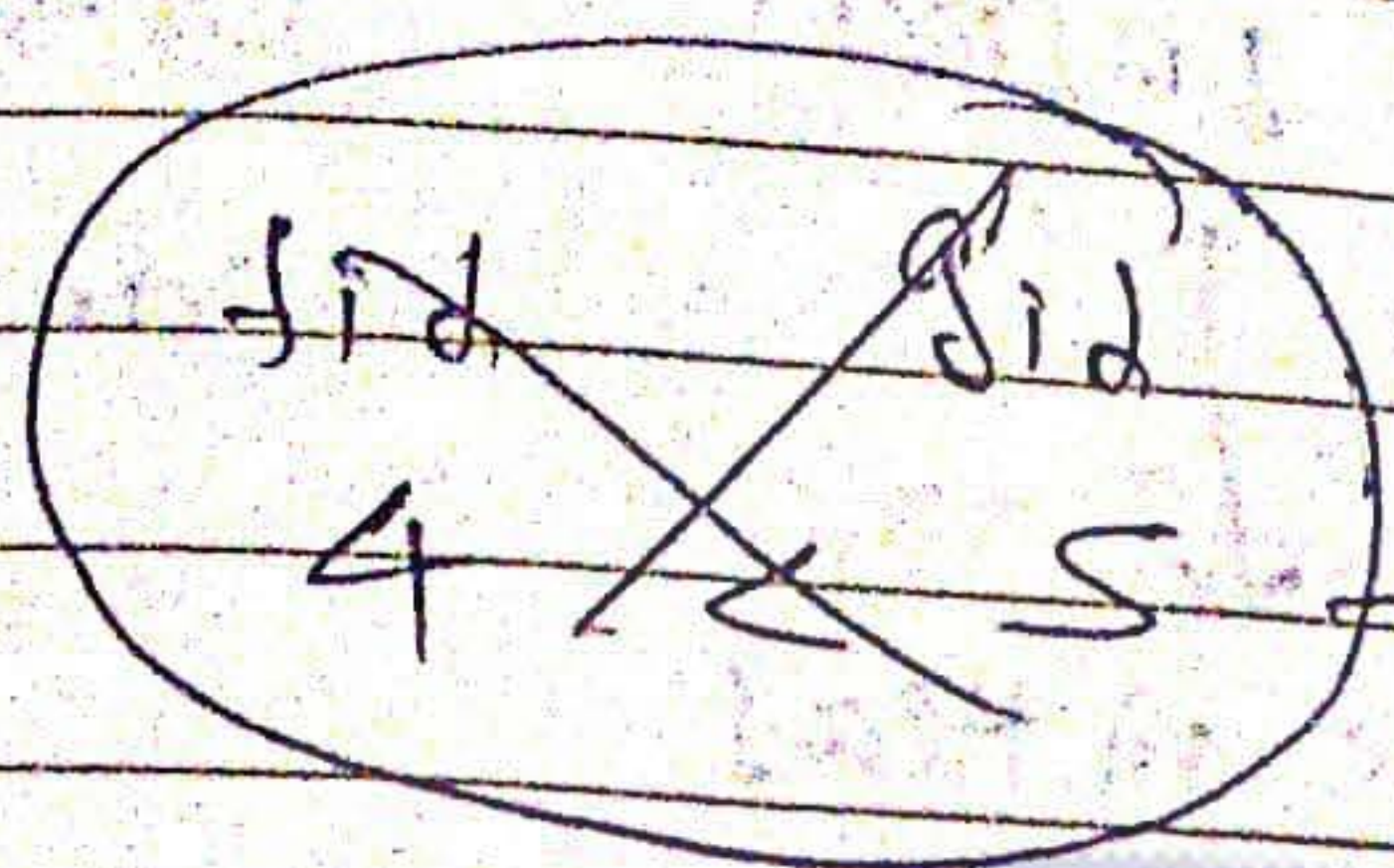
eg.)

$$f_x > g_x$$

$$4 > 3$$

$$f_x < g_x$$

$$2 < 3$$



This is Unwanted relation

Now the size of the table is $O(2n)$

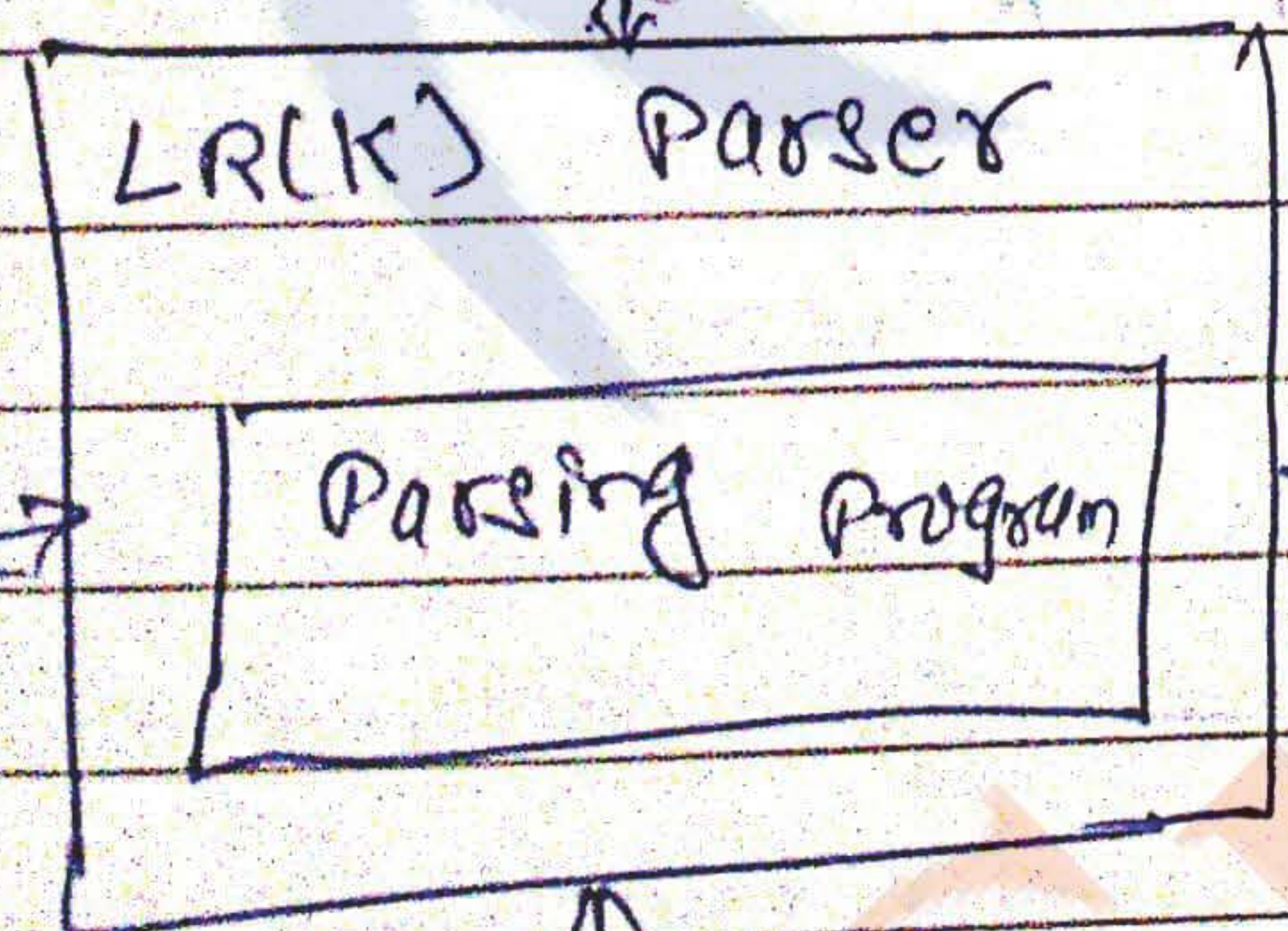
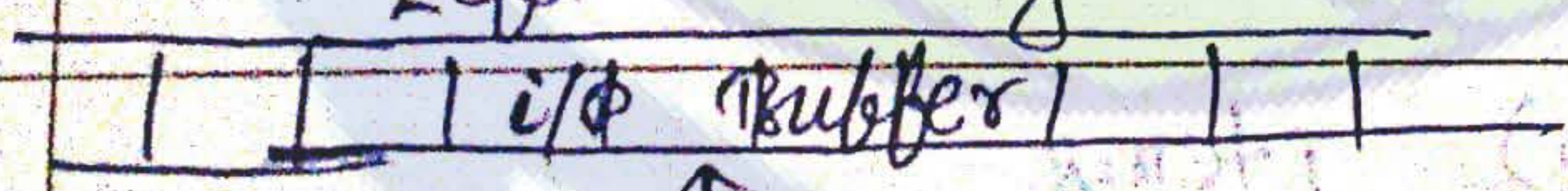


LR(K)

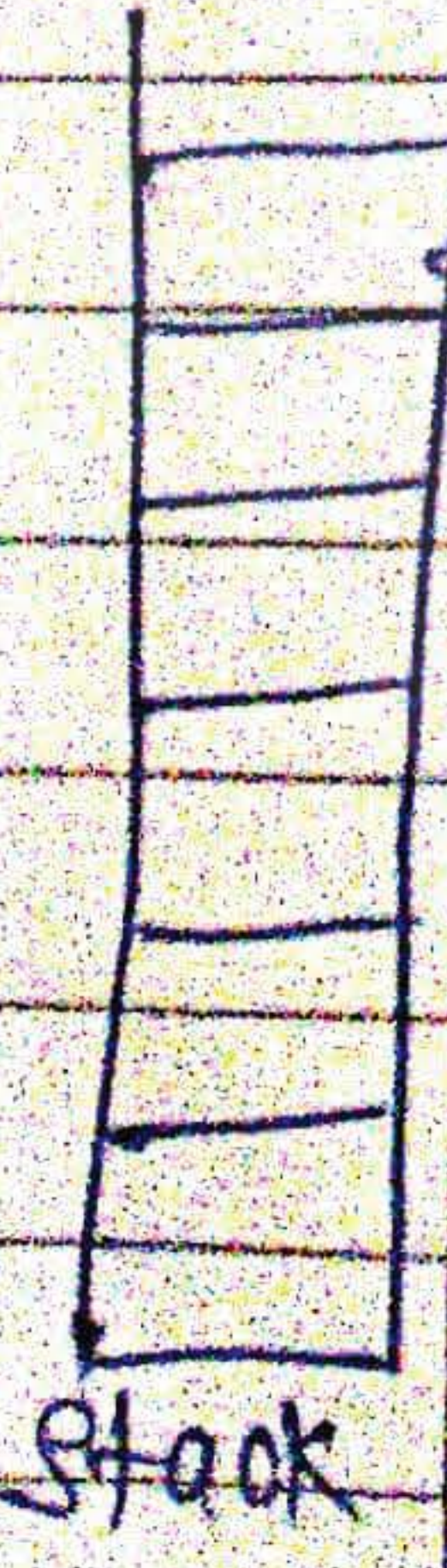
Look a head symbol of length 'k'.

uses RMD

Left to right scan of the i/p string

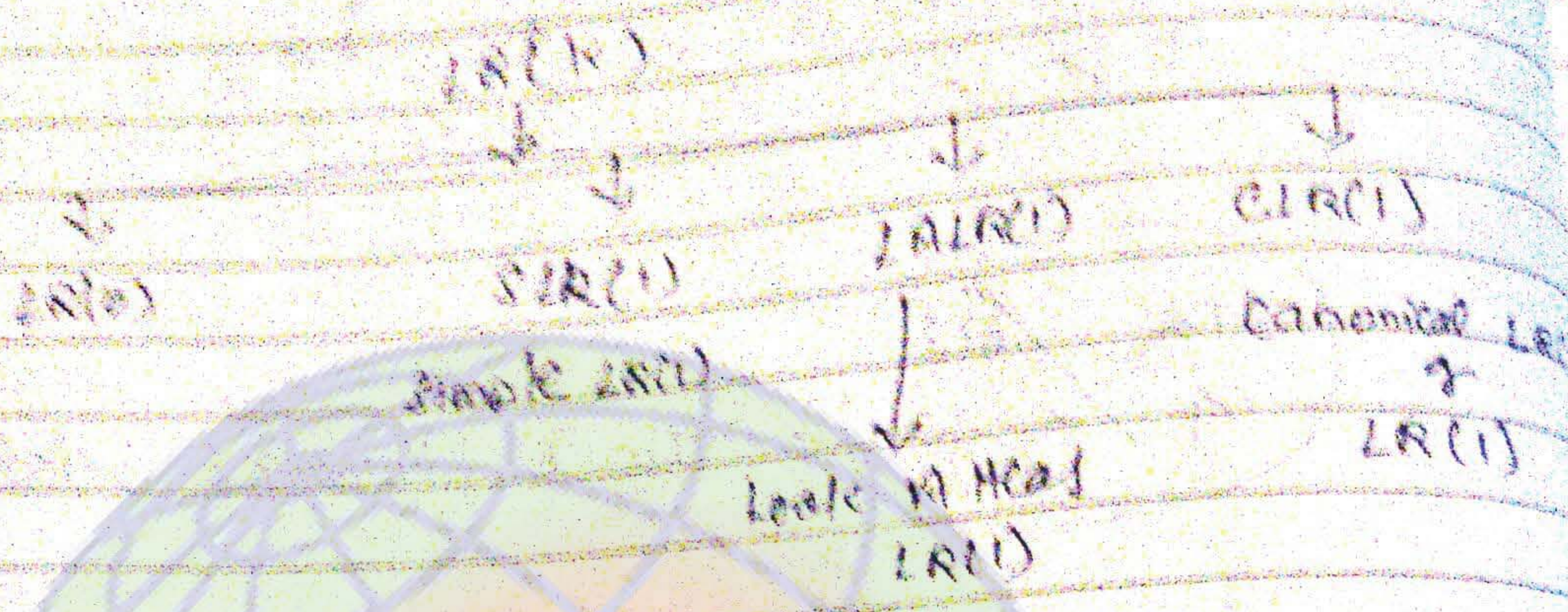


Block diagram of LR(K) Parser



Stack	Action	GOTO
a		
i		
n		

Stack



LR(1) parsing

LR(1) has three parts

- 1) Construct of Canonical item (or) LR(0) items
- 2) Construct of parsing table
- 3) Parsing the i/p string
- 4) Construction of LR(1) items

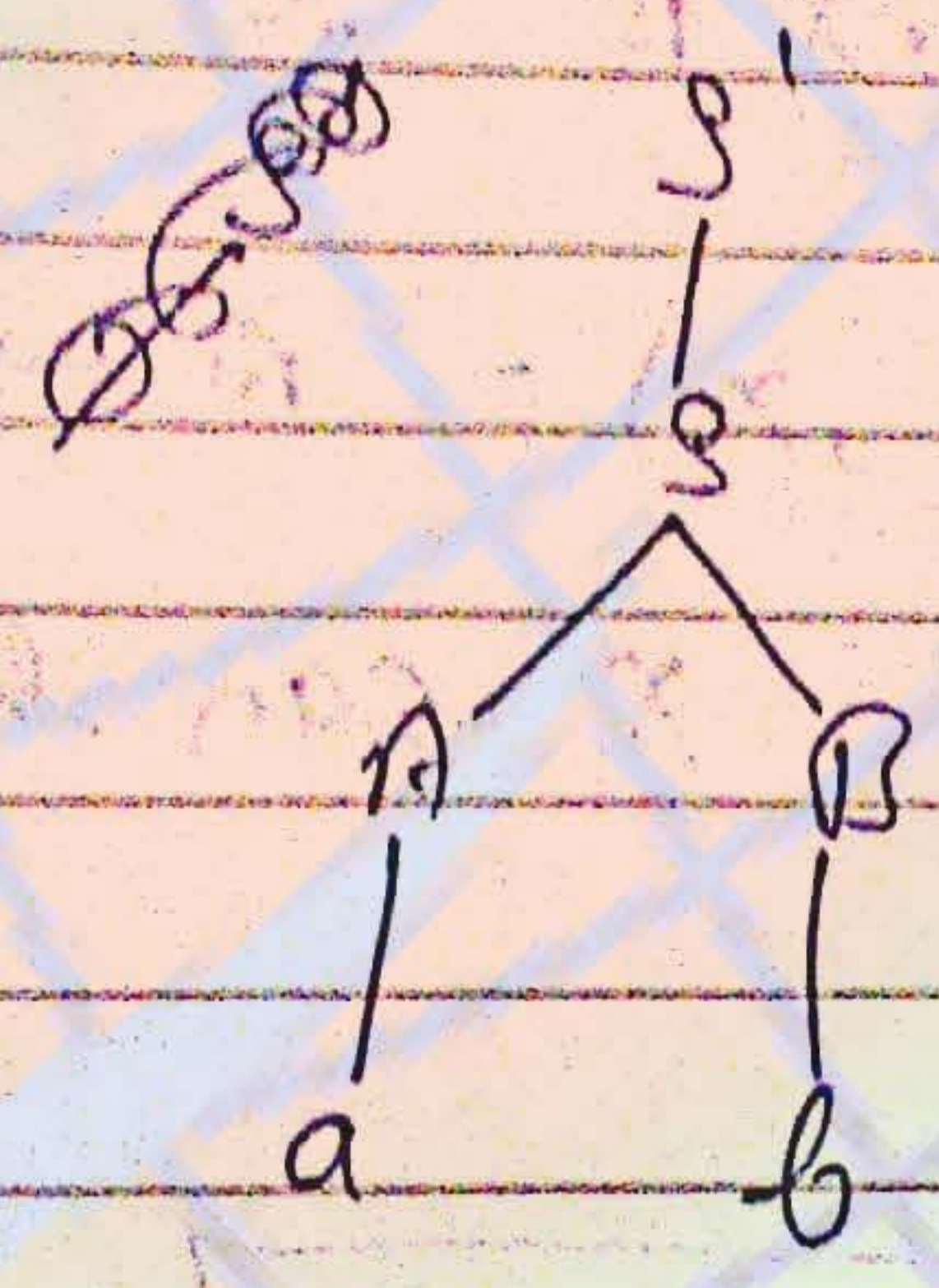
$S \rightarrow \cdot NY Z$
 $S \rightarrow NY \cdot Z$
 $S \rightarrow NY Z \cdot$
 $S \rightarrow NY Z$

Augmented grammar: - Augmented grammar is a new grammar with the new start symbol 's' such that

$s' \rightarrow s$ as a new production. The purpose of this production, the parser will get terminated after successful parsing of the input string.

$$G = \{ S \rightarrow AB, A \rightarrow a, B \rightarrow b \}$$

$$G' = \{ s' \rightarrow S, S \rightarrow AB, A \rightarrow a, B \rightarrow b \}$$



Construction of LR(0) Items:-

Construction on LR(0) items has two parts -

- (i) closure operation
- (ii) Goto operation.

1) Construction of closure operation -

a) Initially add $s' \rightarrow \bullet S$

$$G = \{ S \rightarrow AB, A \rightarrow a, B \rightarrow b \}$$

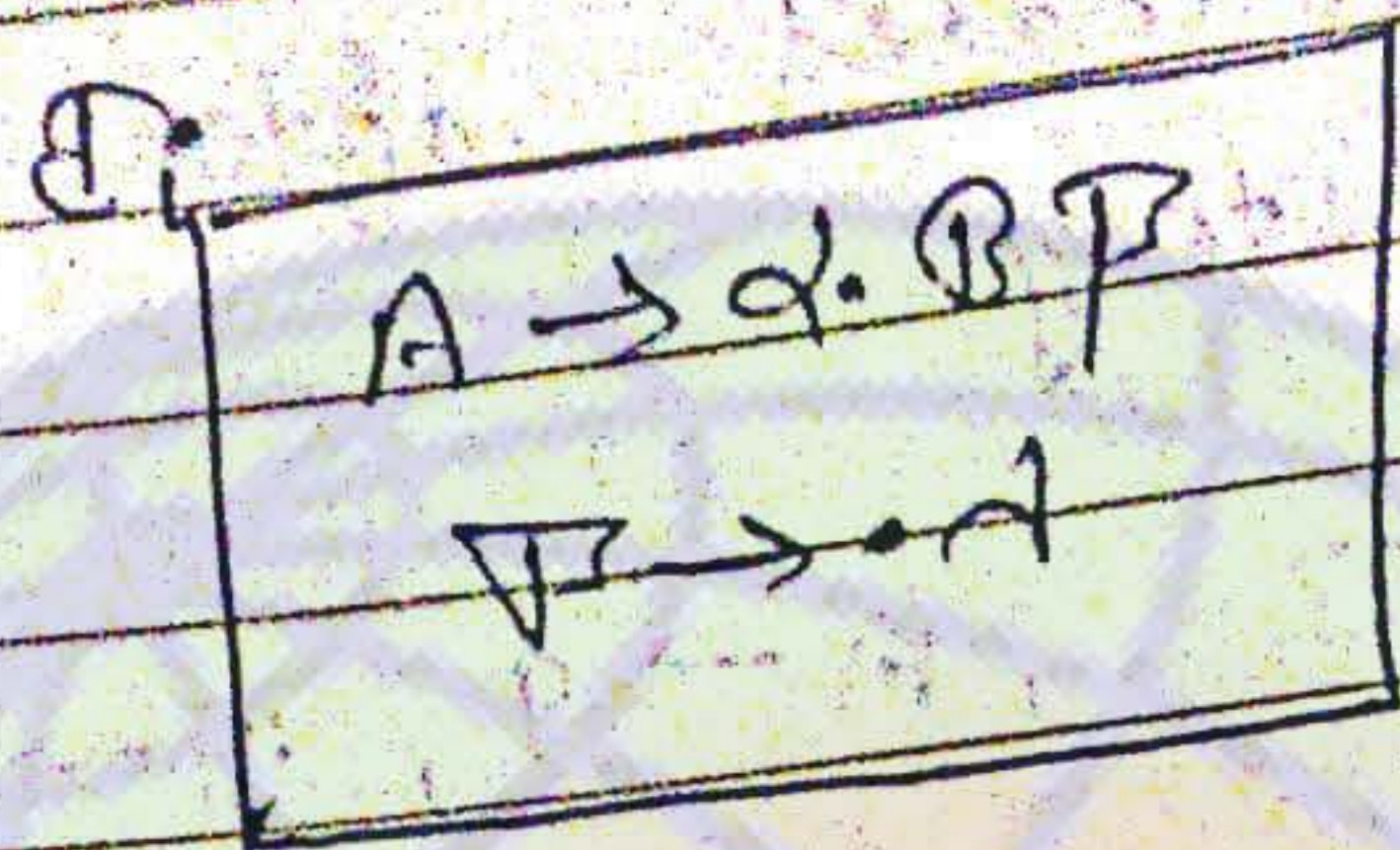
$$s' \rightarrow \bullet S$$

$$S \rightarrow \bullet AB$$

$$A \rightarrow \bullet a$$

$$B \rightarrow \bullet b$$

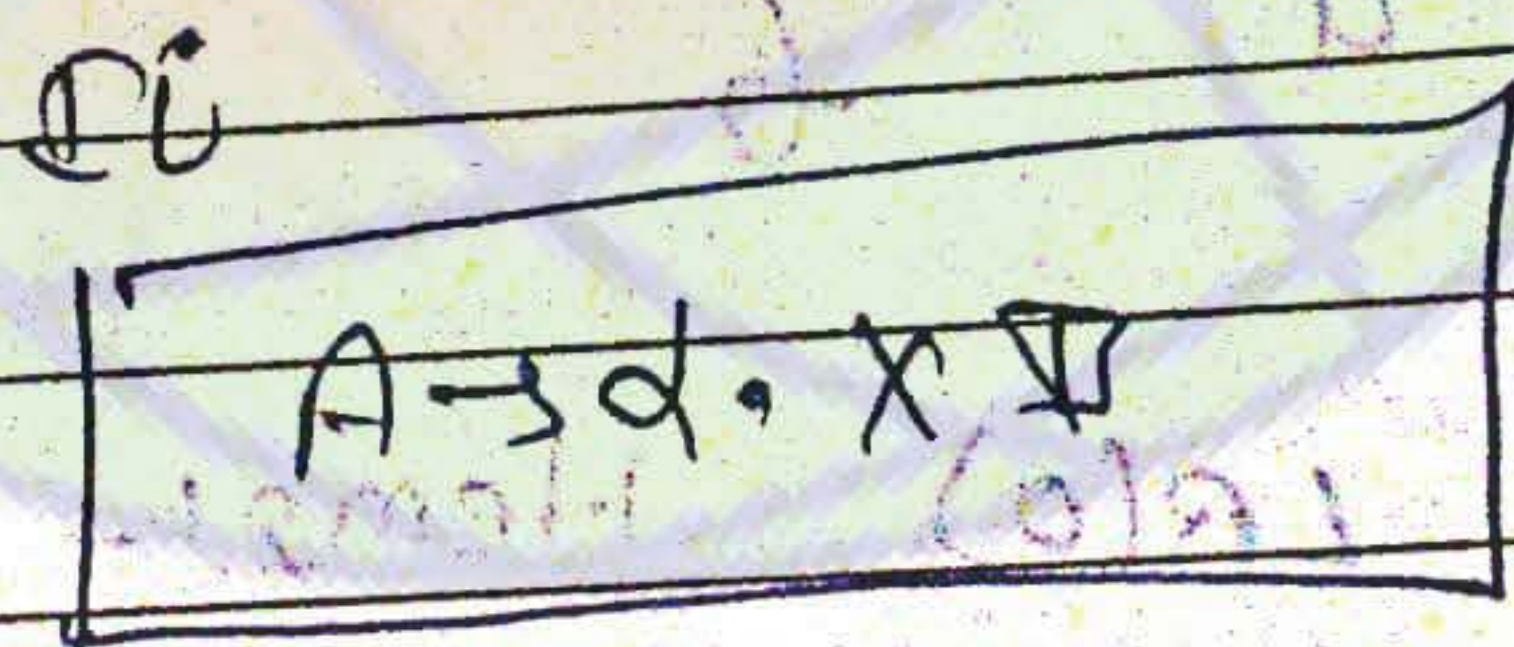
b) If $A \rightarrow \alpha \cdot B \beta$ is in D_i and if $B \rightarrow \gamma$ is a production, then add $B \rightarrow \cdot \gamma$ in D_i



ii) Goto operation - If $A \rightarrow \alpha \cdot X \beta$ is in D_i , then

$$\text{Goto}(D_i, X) = A \rightarrow \alpha \cdot X \beta$$

Here X can be terminal or non terminal



$$\text{Goto}(D_i, X) = A \rightarrow \alpha \cdot X \beta$$

c) Construct LR(1) parsing table for the following grammar.

$$G = \{ E \rightarrow E + T / T, T \rightarrow T * F / F, F \rightarrow (E) / id \}$$

\mathcal{D}_0

$E' \rightarrow \cdot E$
$E \rightarrow \cdot E + T$
$E \rightarrow \cdot T$
$T \rightarrow \cdot T * F$
$T \rightarrow \cdot F$
$F \rightarrow \cdot (E)$
$F \rightarrow \cdot id$

$\mathcal{D}_1 \text{ Goto}(\mathcal{D}_0, E)$

$E' \rightarrow E \cdot$
$E \rightarrow E \cdot + T$

$\mathcal{D}_6 \text{ Goto}(\mathcal{D}_1, +)$

$E \rightarrow E + \cdot T$
$T \rightarrow \cdot T * F$
$T \rightarrow \cdot F$
$F \rightarrow \cdot (E)$
$F \rightarrow \cdot id$

$\mathcal{D}_2 \text{ Goto}(\mathcal{D}_0, T)$

$E \rightarrow T \cdot$
$T \rightarrow T \cdot * F$

$\mathcal{D}_7 \text{ Goto}(\mathcal{D}_2, *)$

$T \rightarrow T * \cdot F$
$F \rightarrow \cdot (E)$
$F \rightarrow \cdot id$

$\mathcal{D}_3 \text{ Goto}(\mathcal{D}_0, F)$

$T \rightarrow F \cdot$

$\mathcal{D}_4 \text{ Goto}(\mathcal{D}_0, ($

$F \rightarrow (\cdot E)$
$E \rightarrow \cdot E + T$
$E \rightarrow \cdot T$
$T \rightarrow \cdot T * F$
$T \rightarrow \cdot F$
$F \rightarrow \cdot (E)$
$F \rightarrow \cdot id$

$\mathcal{D}_8 \text{ Goto}(\mathcal{D}_4, E)$

$F \rightarrow (E \cdot)$
$E \rightarrow E \cdot + T$

$\mathcal{D}_5 \text{ Goto}(\mathcal{D}_0, id)$

$F \rightarrow id \cdot$

$\text{Goto}(\mathcal{D}_4, T) = \mathcal{D}_2$

$\text{Goto}(\mathcal{D}_4, F) = \mathcal{D}_3$

$\text{Goto}(\mathcal{D}_4, () = \mathcal{D}_4$

$\text{Goto}(\mathcal{D}_4, id) = \mathcal{D}_5$

$\mathcal{D}_9 \text{ Goto}(\mathcal{D}_6, T)$

$E \rightarrow E + T \cdot$
$T \rightarrow T \cdot * F$

$\mathcal{D}_{10} \text{ Goto}(\mathcal{D}_6, F) = \mathcal{D}_3$

$T \rightarrow T * F \cdot$

$\mathcal{D}_{11} \text{ Goto}(\mathcal{D}_4, E)$

$T \rightarrow T * F \cdot$

$\mathcal{D}_{12} \text{ Goto}(\mathcal{D}_6, () = \mathcal{D}_4$

$\mathcal{D}_{13} \text{ Goto}(\mathcal{D}_7, () = \mathcal{D}_4$

$\mathcal{D}_{14} \text{ Goto}(\mathcal{D}_6, id) = \mathcal{D}_5$

$\mathcal{D}_{15} \text{ Goto}(\mathcal{D}_7, id) = \mathcal{D}_5$

$\mathcal{D}_{11}(\mathcal{D}_8, ()$

$F \rightarrow (E) \cdot$

$\text{Goto}(\mathcal{D}_8, +) = \mathcal{D}_6$

Now,
Construction of LR(1) parsing table-

It has two parts

- 1) ACTION
- 2) GOTO

1) Action - Action part of the table will be filled as follows -

$A \rightarrow \alpha \cdot a \beta$
 $A \rightarrow \alpha \cdot B \beta$
 $A \rightarrow \alpha a \beta$

a) If $A \rightarrow \alpha \cdot a \beta$ is in \mathcal{D}_i , for every symbol a after that we write goto

If $A \rightarrow \alpha \cdot a \beta$

and if $\text{goto}(\mathcal{D}_i, a) = \mathcal{D}_j$

then, set $\text{Action}(i, a) = S_j$

b) If $A \rightarrow \alpha \cdot$ is in \mathcal{D}_i then

set $\text{Action}(i, \epsilon) = \text{Reduce by } A \rightarrow \alpha$

where $\epsilon \in \text{Follow}(A)$

Here $A \rightarrow \alpha$ must not be an augmented production

c) If $e' \rightarrow S \cdot$ is in \mathcal{D}_i , then

$\text{Action}(i, \$) = \text{Accept}$



2) GOTO

or \mathcal{A}_1

$$A \rightarrow a_1 a_2 a_3$$

and \mathcal{A}_2

$$\text{GOTO}(\mathcal{A}_1, \mathcal{A}_2) = \mathcal{A}_1 \text{ then}$$

$$\text{not } \text{GOTO}(\mathcal{A}_1, \mathcal{A}_2) = \mathcal{A}_2$$

Q4
Σ

- 1) $E \rightarrow E + T$
- 2) $E \rightarrow T$
- 3) $T \rightarrow T * F$
- 4) $T \rightarrow F$
- 5) $F \rightarrow (E)$
- 6) $F \rightarrow id$

$$\text{Follow}(E) = \{ +,), \$ \}$$

$$\text{Follow}(T) = \{ *, +,), \$ \}$$

$$\text{Follow}(F) = \{ *, +,), \$ \}$$

GOTO

States	ACTION				id	\$	E		T
	+	*	()			1	2	
0			S4		SS	Accept			
1	S6					R2			
2	R2	S7		R2		R4			
3	R4	R4		R4			8	2	3
4			S4		SS	R6			
5	R6	R6		R6				9	2
6			S4		SS				
7			S4		SS				
8	S6			S11		R1			
9	R1	S7		R1		R3			
10	R3	R3		R3		R5			
11	R5	R5		R5					

E → E, Augment (Accept)

! (i, \$) Accept

E → T → Reduce

E → sid.

[S, ε] = R6

In the above table, all the entries are single therefore the grammar is SLR(1)

~~Def~~ Conflict निकालने का आसान तरीका

Conflicts in LR(1)

- i) Shift-Reduce
- ii) Reduce-Reduce

✓ Shift-Reduce (S/R) conflict -

Ex

$A \rightarrow \alpha \cdot a \beta$
$B \rightarrow \gamma \cdot$

	a	b	c	\$
i				

if $\{ a \} \cap \text{Follow}(B) \neq \emptyset$
 \Rightarrow S/R conflict
 \Rightarrow Not LR(1)

✓ Reduce-Reduce conflict (R/R)

Ex

$A \rightarrow \alpha \cdot$
$B \rightarrow \alpha \cdot$

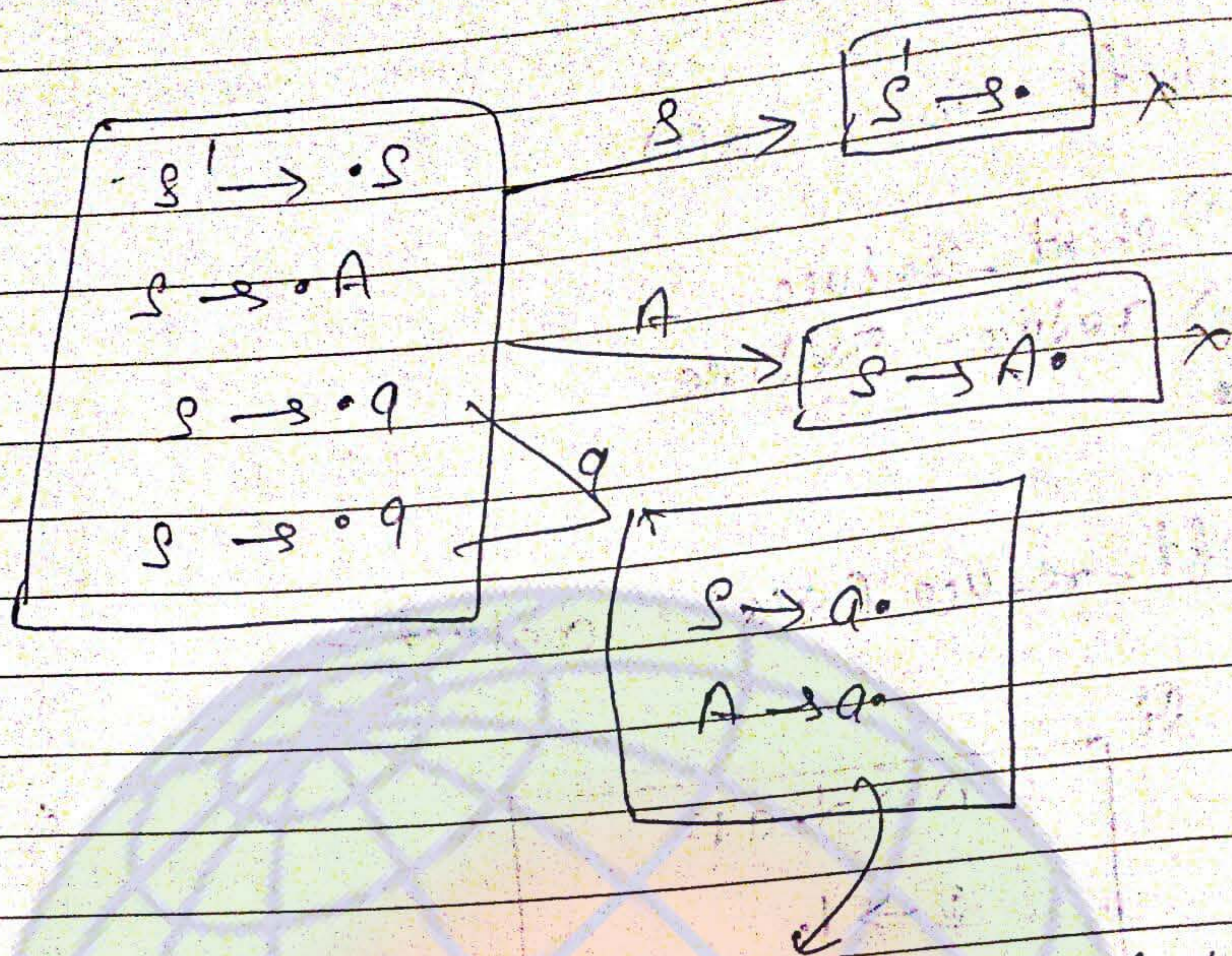
if $\text{Follow}(A) \cap \text{Follow}(B) \neq \emptyset$
 \Rightarrow R/R conflict
 \Rightarrow not LR(1)

✓
 1) ~~Trick~~

Check whether the following grammar is LR(1) or not

1) $G = \{ S \rightarrow A/a, A \rightarrow a \}$

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$FOLLOW(S) \cap FOLLOW(A)$

$= \{ \$ \} \cap \{ \$ \}$

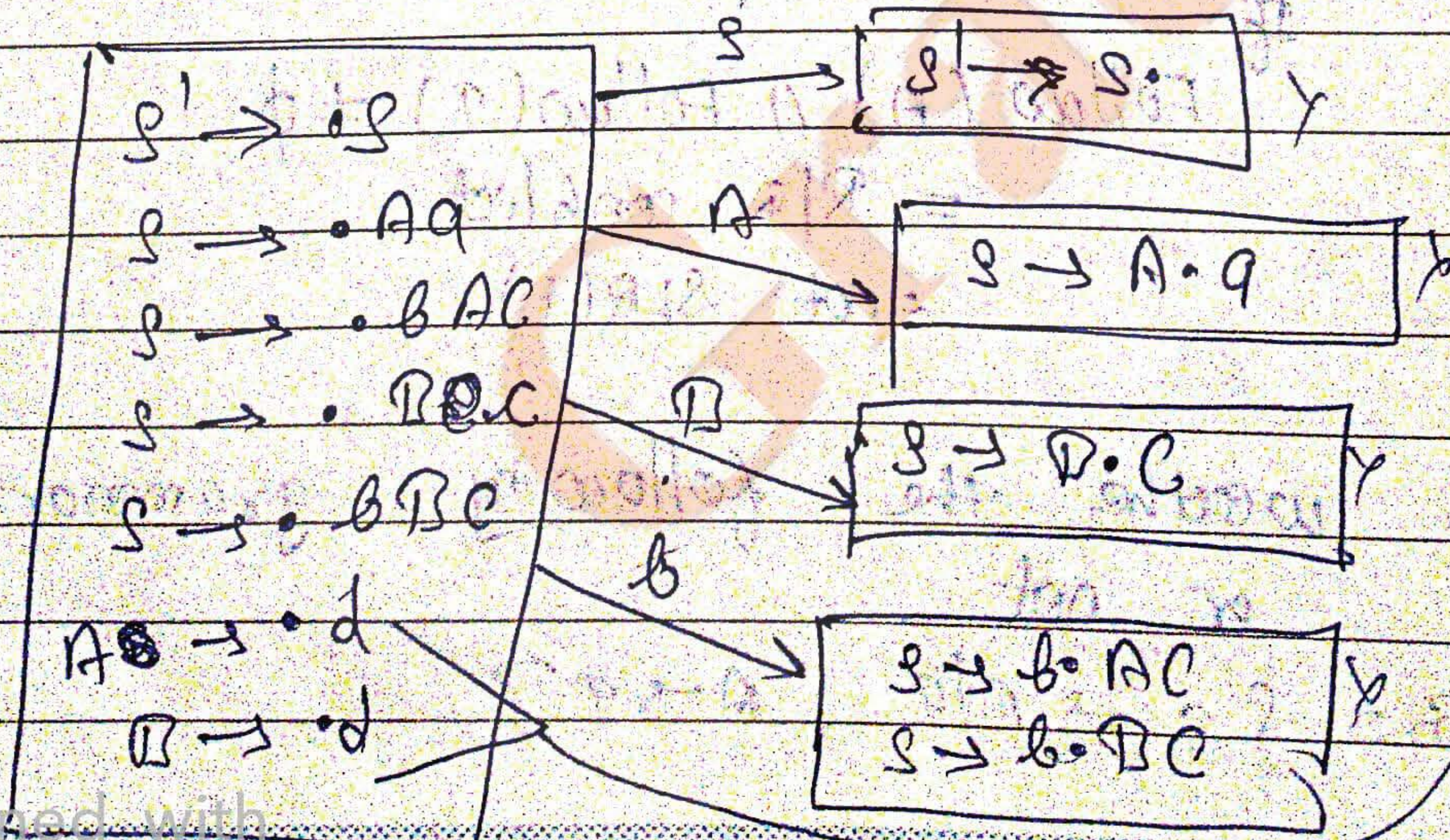
$= \{ \$ \}$

$= \emptyset$

= R/R conflict

= Not LR(0)

2) $G = \{ S \rightarrow Aa / bAc / Bc / bBc, A \rightarrow d, B \rightarrow d \}$

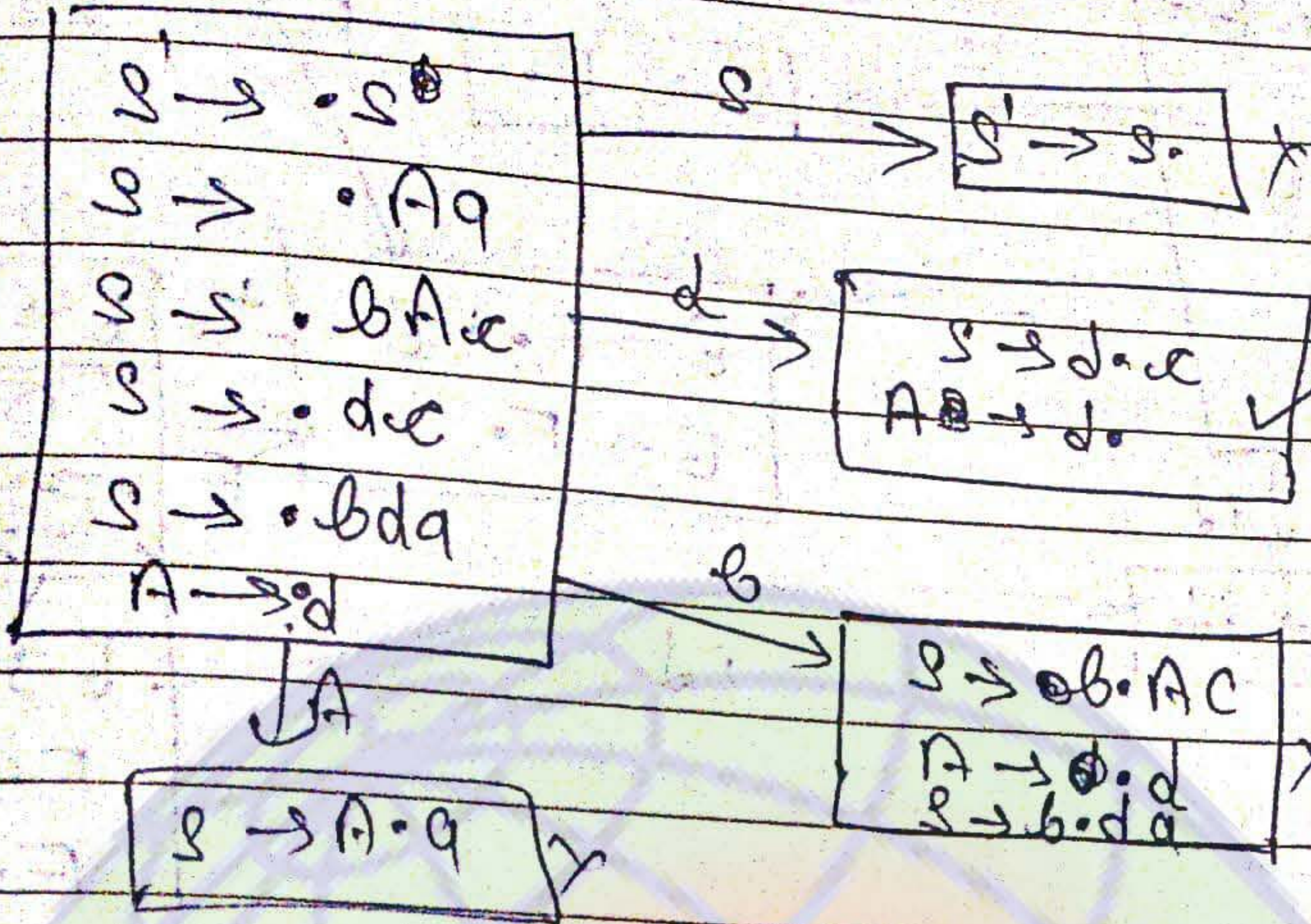


$FOLLOW(A) \cap FOLLOW(B)$

$= \{ a, c \} \cap \{ c, a \}$

$= \{ a, c \}$

3) $G = \{ S \rightarrow Aa \mid bAc \mid dc \mid bda, A \rightarrow d \}$



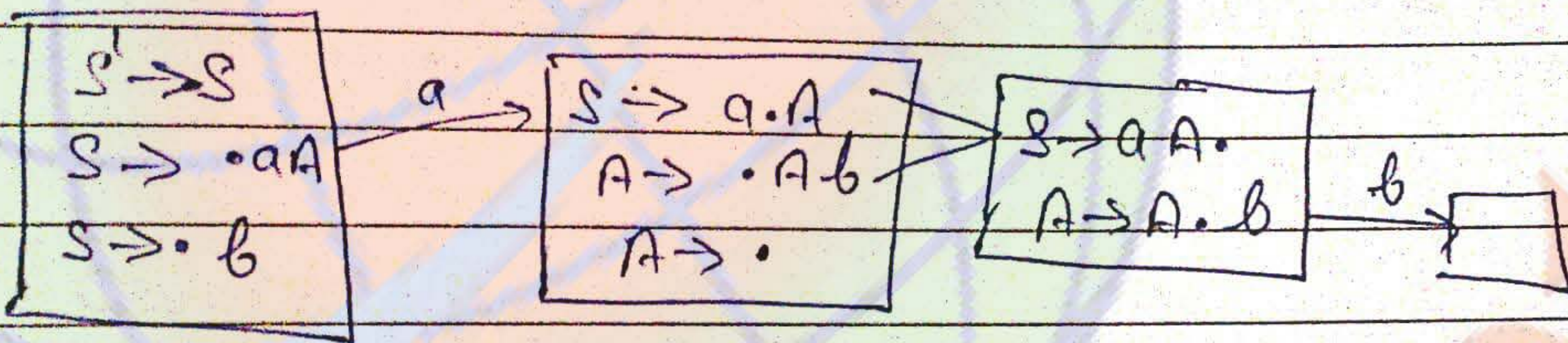
$\Sigma \{ S \} \cap \text{Follow}(A)$

$\Sigma \{ c \} \cap \{ a, c \} \neq \emptyset$

\rightarrow LR conflict

\Rightarrow Not SLR

4) $G = \{ S \rightarrow aA \mid b, A \rightarrow AB \mid \epsilon \}$



$$= \{ b \} \cap \text{Follow}(S)$$

$$= \{ b \} \cap \{ \epsilon \}$$

$$= \emptyset$$

e) Consider the following grammar under LR(0) items of the grammar

$G = \{ S \rightarrow S * E \mid E, E \rightarrow F + E \mid F, F \rightarrow id \}$

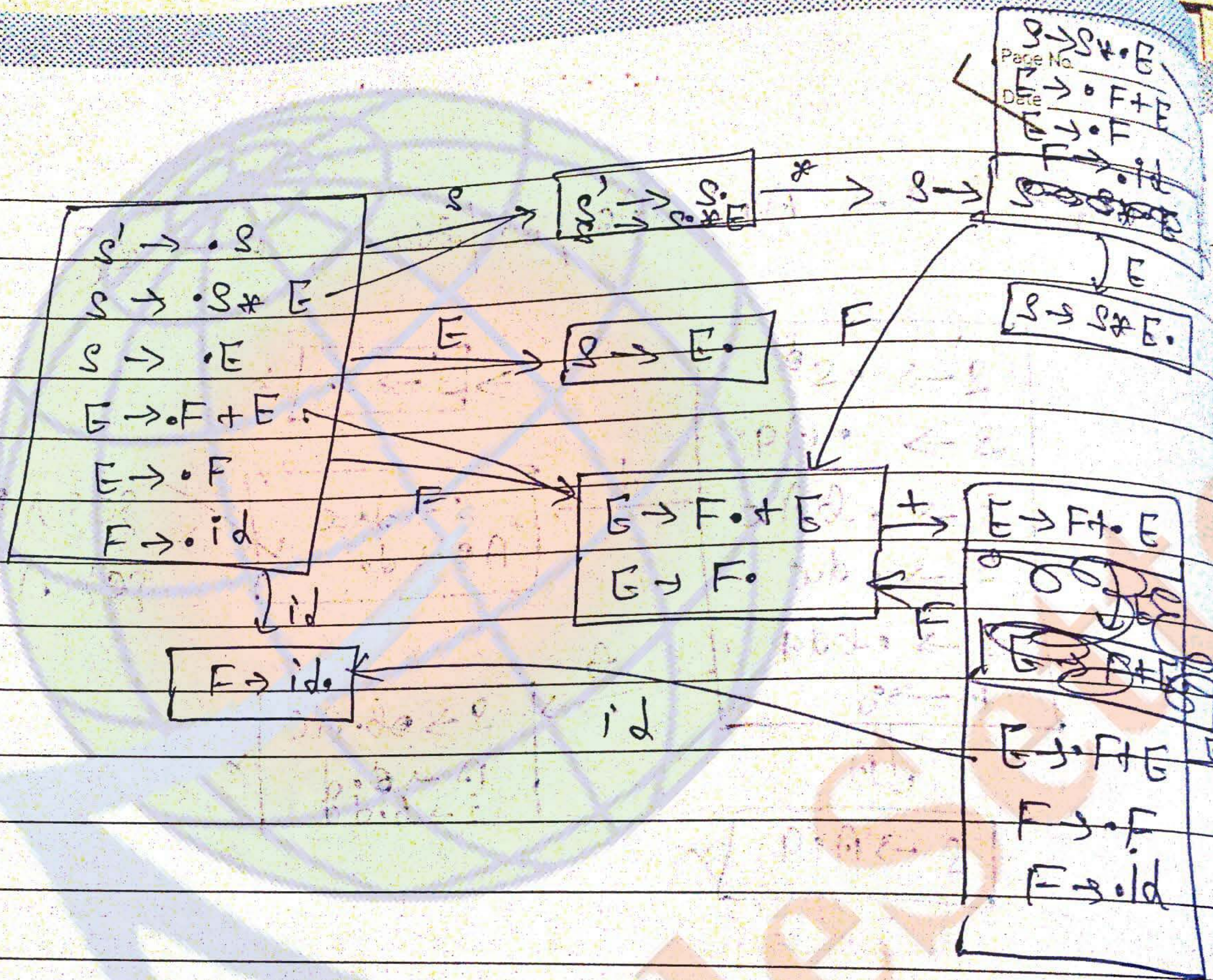
- 1) $S \rightarrow S * . E$ 2) $E \rightarrow F . + E$ 3) $E \rightarrow F + . E$

Given the items above, which two of them will be same set of canonical set of items of the grammar.

- a) 1 & 2 b) 2 & 3 c) 1 & 3 d) none

No LR conflict
Not SLR(1)

S/N



Page No.
Date



LR(0) Parsing:

LR(0) parser has two parts:

- a) Construction of LR(0) items
- b) construction of parsing table

1) Construction of LR(0) items:

It is same as construct of LR(0) items in SLR(1).

2) Construction of parsing table -

It is also same as SLR(1), except that,

if S_i $[A \rightarrow \alpha]$ is in S_i , then write reduce by $A \rightarrow \alpha$ in entire i th row of action part of the table.

Conflicts: -

- 1) shift-reduce
- 2) Reduce-Reduce

1) shift-reduce conflict

S_i

$A \rightarrow \alpha \cdot a \beta$
$B \rightarrow \gamma$

	a	b	c	$\$$
i	R_1	R_2	R_3	R_4

Conflict

\Rightarrow S/R conflict
 \Rightarrow Not LR(0)

2) Reduce-Reduce conflict

S_i

$A \rightarrow \alpha$
$B \rightarrow \gamma$

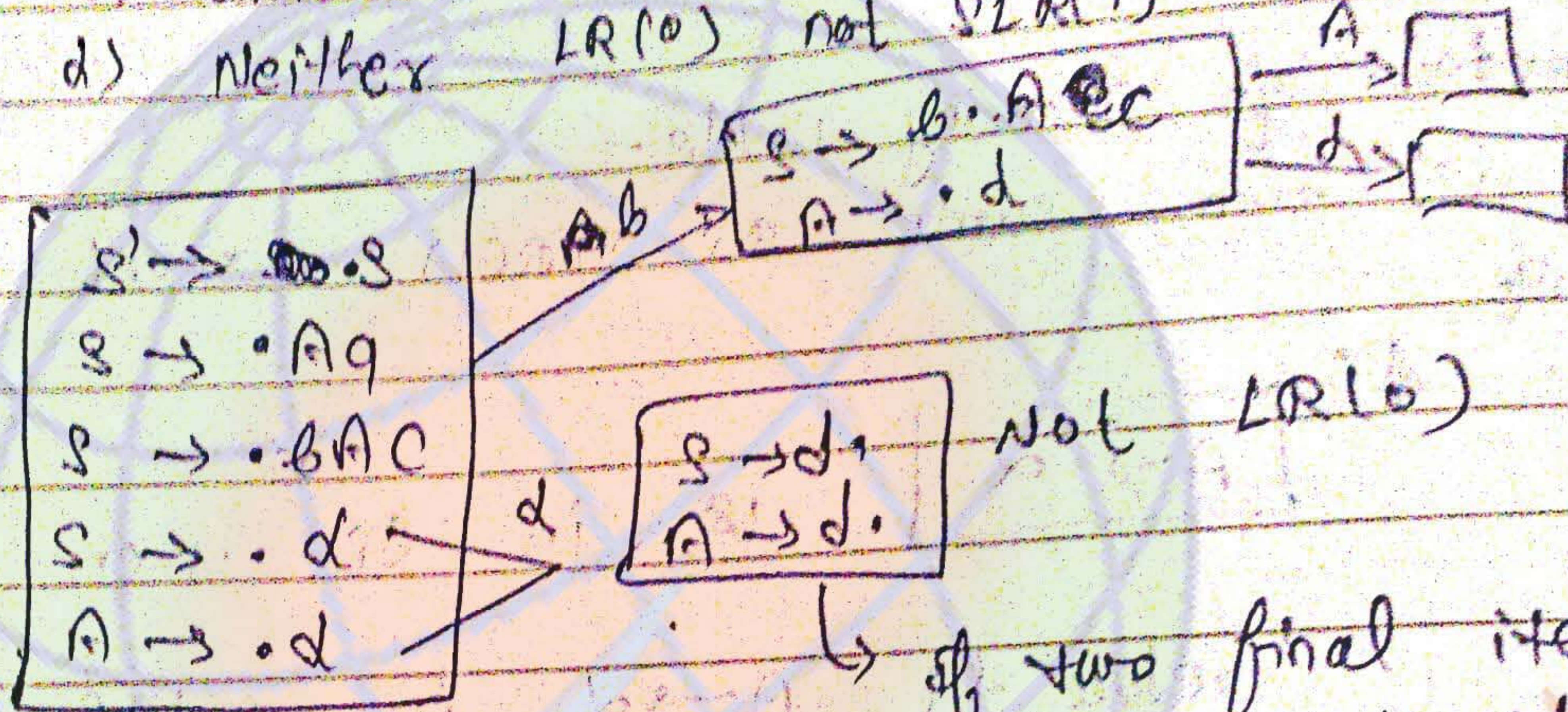
	a	b	c	$\$$
i	R_1	R_2	R_3	R_4

\Rightarrow R/R conflict \Rightarrow Not LR(0)

Q) The following grammar is
 $G = \{ S \rightarrow Aa / BAe / d, A \rightarrow d \}$

- a) LR(0) but not SLR(1)
- b) SLR(1) but not LR(0)
- c) both LR(0) & SLR(1)
- d) Neither LR(0) nor SLR(1)

Soln



Not LR(0)

of two final items then R/R conflict in LR(0) \Rightarrow Not LR(0)

Now,

$$\text{Follow}(S) \cap \text{Follow}(A)$$

$$= \{ \$ \} \cap \{ a, c \}$$

$$= \phi$$

The grammar is SLR(1)

Note:

$$LR(0) \subset SLR(1)$$

Every LR(0) grammar is also SLR(1), but every SLR(1) is not LR(0)

* CLR(1) or LR(1) :-

R1

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It has two parts.

1) construction of Canonical set of items
LR(1) items

2) construction of parsing table

① Construction of LR(1) items.

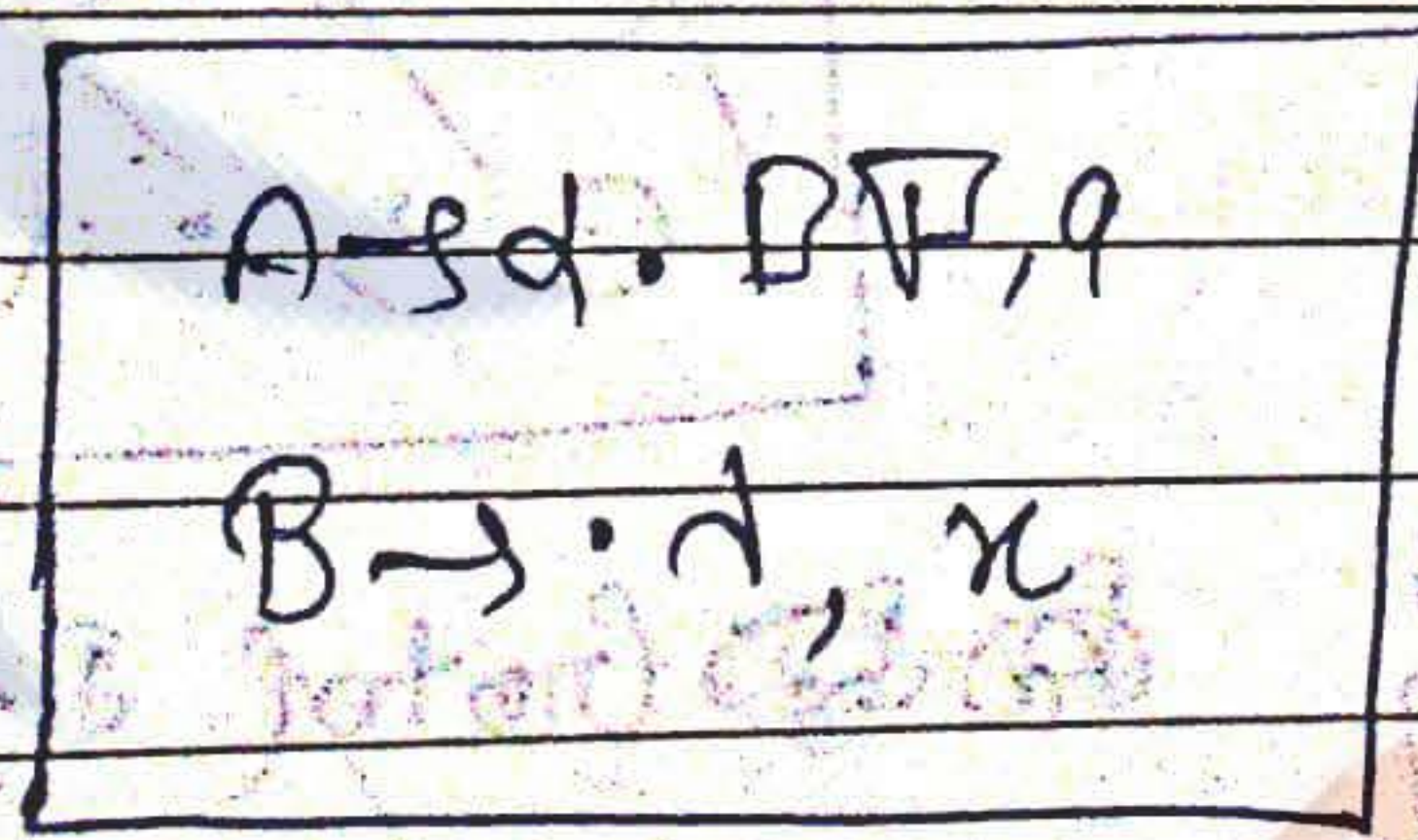
It has two parts: -

- a) closure operations
- b) Goto operation

a) Construction of closure operations

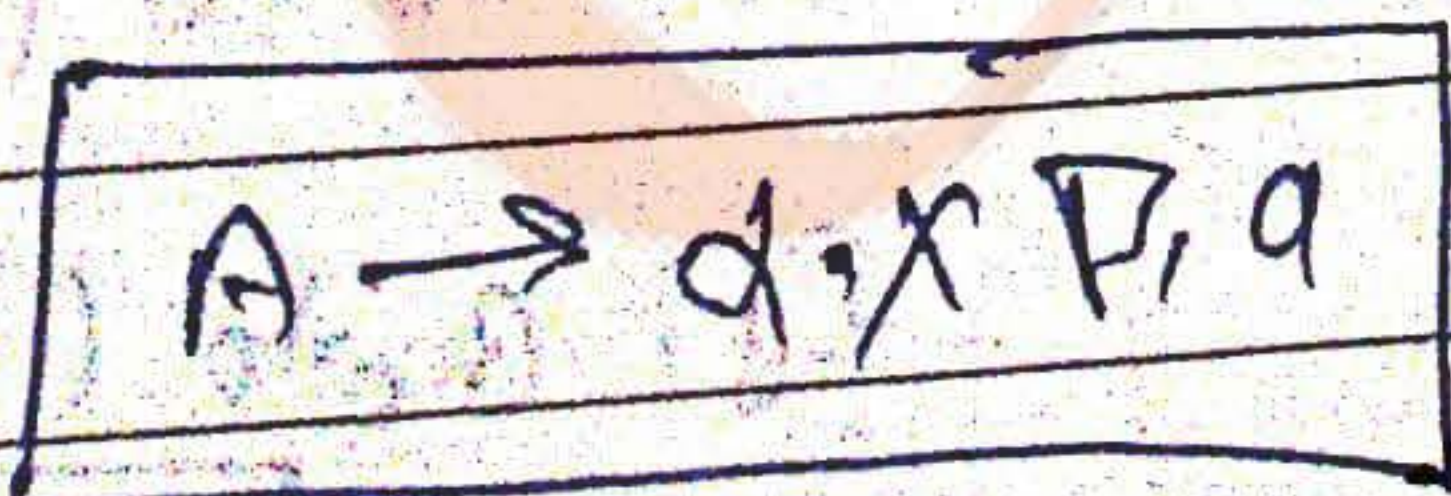
Initially add $S' \rightarrow \cdot S, \$$

2) If $A \rightarrow \alpha \cdot B \beta, a$ is in D_i and if $B = \gamma$ is a production then add $B \rightarrow \cdot \gamma, x$ in D_i where $x \in \text{First}(\gamma a)$



where $x \in \text{First}(\gamma a)$

3) If $A \rightarrow \alpha \cdot X \beta, a$ is in D_i , then goto D_j



then $\text{Goto}(D_i, X) = A \rightarrow \alpha X \cdot \beta, a$

o) Construct LR(1) \leftarrow CLR(1) parsing tables -
 $G = \{ S \rightarrow CC, C \rightarrow aC/d \}$

D_0

$S' \rightarrow \cdot S, \$$
$S \rightarrow \cdot CC, \$$
$C \rightarrow \cdot aC, a/d$
$C \rightarrow \cdot d, a/d$

$D_1: \text{Goto}(D_0, S)$

$S' \rightarrow S \cdot, \$$

$D_2: \text{Goto}(D_0, C)$

$S \rightarrow C \cdot C, \$$
$C \rightarrow \cdot aC, \$$
$C \rightarrow \cdot d, \$$

$D_3: \text{Goto}(D_0, a)$

$C \rightarrow a \cdot C, a/d$
$C \rightarrow \cdot aC, a/d$
$C \rightarrow \cdot d, a/d$

$D_4: \text{Goto}(D_0, d)$

$C \rightarrow d \cdot, a/d$

$D_5: \text{Goto}(D_2, C)$

$S \rightarrow CC \cdot, \$$

~~$D_6: \text{Goto}(D_2, a) = D_3$~~ , ~~$D_7: \text{Goto}(D_2, d) = D_4$~~

$C \rightarrow a \cdot C, \\$
$C \rightarrow \cdot aC, \\$
$C \rightarrow \cdot d, \\$

$D_8: \text{Goto}(D_3, C)$

$C \rightarrow aC \cdot, a/d$

~~$D_9: \text{Goto}(D_3, d) = D_4$~~

$C \rightarrow a \cdot C, a/d$
--

$D_6: \text{Goto}(D_2, a)$

$C \rightarrow a \cdot C, \$$
$C \rightarrow \cdot aC, \$$
$C \rightarrow \cdot d, \$$

$\text{Goto}(D_7, a) = D_3$
 $\text{Goto}(D_7, d) = D_4$

$D_9: \text{Goto}(D_6, C)$

$C \rightarrow aC \cdot, \$$

$\text{Goto}(D_6, a) = D_0$
 $\text{Goto}(D_6, d) = D_4$

Total states = 10

o) Construction

a) ACTION

[D]

He

[D]

b)

a) Construction of LR(1) parsing table

It has two parts:-

- a) action
- b) Goto

a) ACTION:-

[i] of \mathcal{D}_i

$$\boxed{A \rightarrow \alpha \cdot a \beta, b} \quad \text{and}$$

$$\text{if } \text{Goto}(\mathcal{D}_i, a) = \mathcal{D}_j$$

then

$$\text{set Action}[i, a] = S_j$$

[i] of \mathcal{D}_i

\mathcal{D}_i

$$\boxed{A \rightarrow \alpha \cdot, a} \quad \text{and } a \text{ is in } \mathcal{D}_i$$

then

$$\text{set action}[i, a] = \text{Reduce by } A \rightarrow \alpha$$

Here, $A \rightarrow \alpha$ must not be an augmented production.

[i] of \mathcal{D}_i

$$\boxed{S' \rightarrow S, \$} \quad \text{is in } \mathcal{D}_i$$

then

$$\text{set Action}[i, \$] = \text{Accept}$$

b) Goto:

[i] of \mathcal{D}_i $\boxed{A \rightarrow \alpha \cdot B \beta, a}$ is in \mathcal{D}_i , and

Stack = 10

If $Goto (E_i, B) = E_j$

then

set $Goto [E_i, B] = J$

Now, give the numbering to each of the production

- 1) $S \rightarrow CC$
- 2) $C \rightarrow aC$
- 3) $C \rightarrow d$

States	ACTION			GOTO	
	a	d	\$	S	C
0	S3	S4		1	2
1			ACCEPT		
2	S6	S7			5
3	S3	S4			8
4	R3	R3			
5			R1		6
6	S6	S7			9
7			R3		
8	R2	R2			
9			R-2		

In the above table all the entries are single.

Therefore the grammar is CLR(1)



Conflicts: -

①

i.) Shift-Reduce conflict

ii.) Reduce-Reduce conflict

i.) Shift-Reduce conflict -

\mathcal{P}_i

$A \rightarrow \alpha \cdot a \beta, b$
$B \rightarrow \alpha \cdot, a$

\Rightarrow SR conflict
 \Rightarrow Not CLR(1)

ii.) Reduce-Reduce conflict! -

\mathcal{P}_i

$A \rightarrow \alpha \cdot, a$
$B \rightarrow \alpha \cdot, a$

\Rightarrow R/R conflict
 \Rightarrow Not CLR(1)

ce) Check whether the following grammar is CLR(1) or not

i) $G = \{ S \rightarrow A/a, A \rightarrow a \}$

$S' \rightarrow \cdot S, \phi$
$S \rightarrow \cdot A, \phi$
$S \rightarrow \cdot a, \phi$
$A \rightarrow \cdot a, \phi$

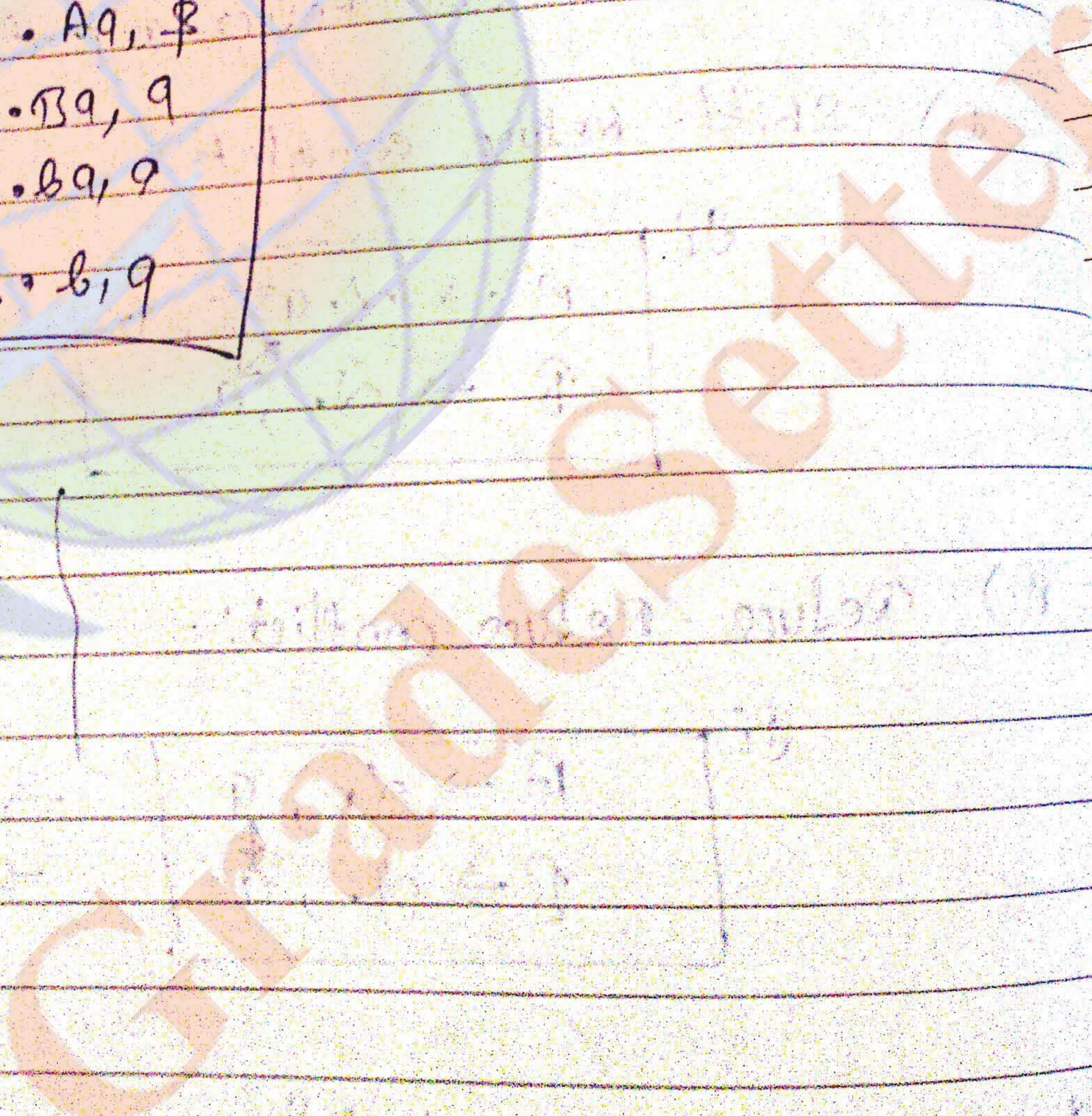
some look ahead
to not
CLR(1)

$S \rightarrow a \cdot, \phi$
$A \rightarrow a \cdot, \phi$

\Rightarrow R/R conflict
 \Rightarrow Not CLR(1)

Q) $G = \{ S \rightarrow Aa, A \rightarrow Ba/ba, B \rightarrow B \}$

$S' \rightarrow \cdot S, \phi$
 $S \rightarrow \cdot Aa, \phi$
 $S \rightarrow S \cdot Ba, a$
 $A \rightarrow \cdot ba, a$
 $A \rightarrow S \cdot b, a$



LALR(1) Parsing

In the first example of LR(1), those states, having everything is same but different look aheads, we have divided them into two different states but in LALR(1) of parsing, we will merge them into single state.

\mathcal{I}_3

$C \rightarrow a \cdot C, a/d$
$C \rightarrow \cdot aC, a/d$
$C \rightarrow \cdot d, a/d$

\mathcal{I}_6

$C \rightarrow a \cdot C, \phi$
$C \rightarrow \cdot aC, \phi$
$C \rightarrow \cdot d, \phi$

~~\mathcal{I}_3~~ $\mathcal{I}_3 + \mathcal{I}_6 = \mathcal{I}_{36}$

$C \rightarrow a \cdot C, a/d/\phi$
$C \rightarrow \cdot aC, a/d/\phi$
$C \rightarrow \cdot d, a/d/\phi$

$\mathcal{I}_4 + \mathcal{I}_7 = \mathcal{I}_{47}$

$C \rightarrow d \cdot, a/d/\phi$

$\mathcal{I}_8 + \mathcal{I}_9 = \mathcal{I}_{89}$

$C \rightarrow aC \cdot, a/d/\phi$

Construction of LALR(1) parsing table is same as

Construction of LR(1) parsing table

\mathcal{I}_0

\mathcal{I}_1

\mathcal{I}_2

\mathcal{I}_{36}

\mathcal{I}_{47}

\mathcal{I}_5

\mathcal{I}_{89}

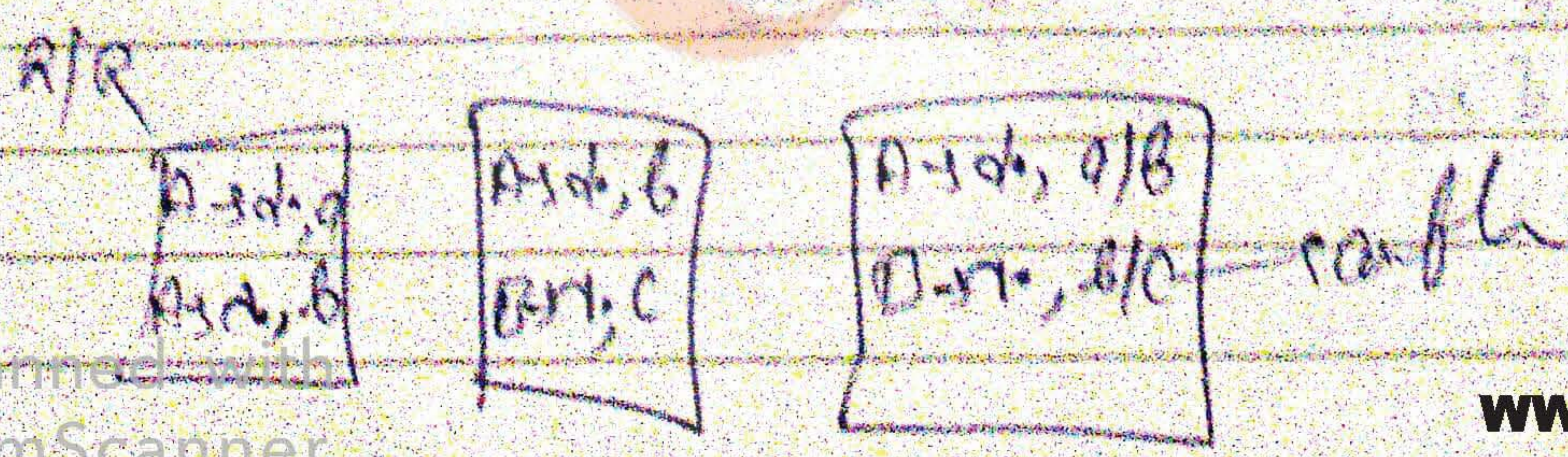
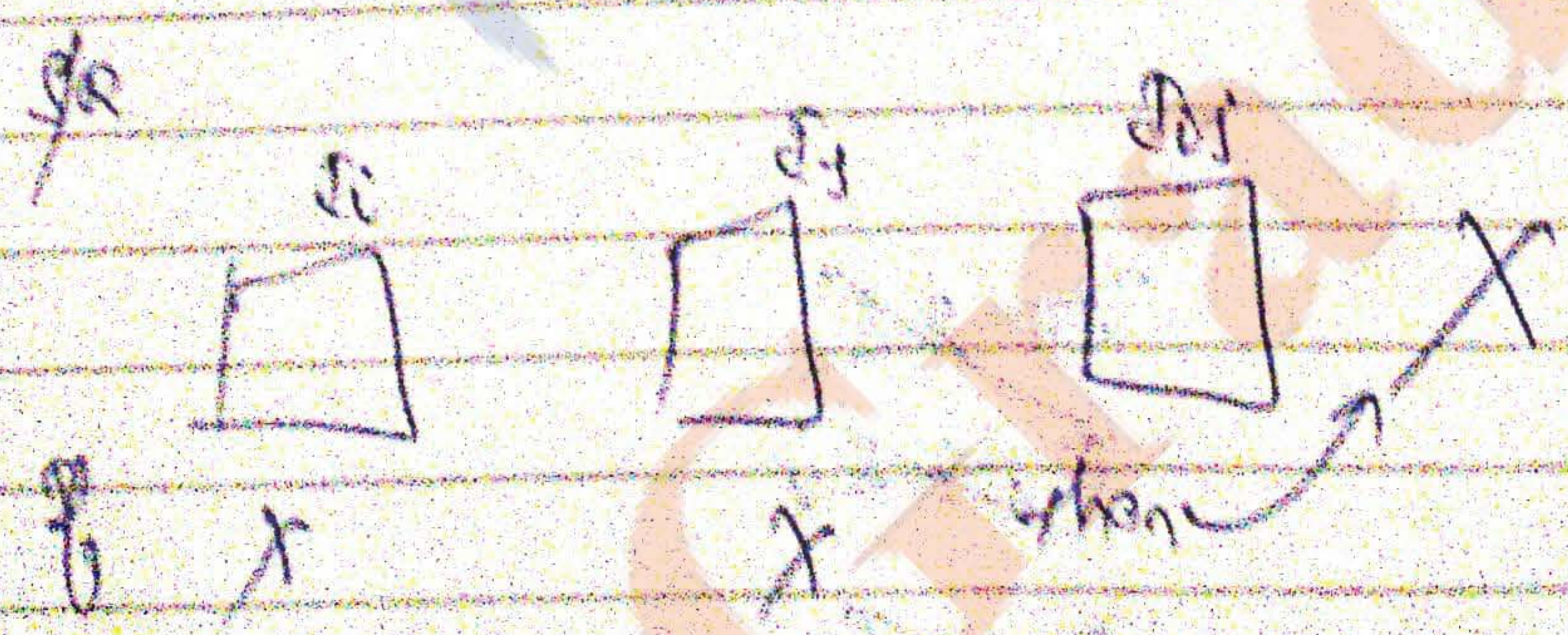
~~\mathcal{I}_3 & \mathcal{I}_6~~

~~\mathcal{I}_4 & \mathcal{I}_7~~

~~\mathcal{I}_8 & \mathcal{I}_9~~

state	ACTION			GOTO	
	a	d	g	f	e
0	S06	S47	ACCEPT		
1					
2	S56	S47			S
36	S36	S47			
44	R3	R7	R5		
5			R1		
89	R9	R8	R9		

	CIRCI)	LAI(RCI)
LR conflict	NO	NO
R/R conflict	NO	yes/NO



Note:
① LR

e.) The
1) R.G

80/7 any

read

Note:

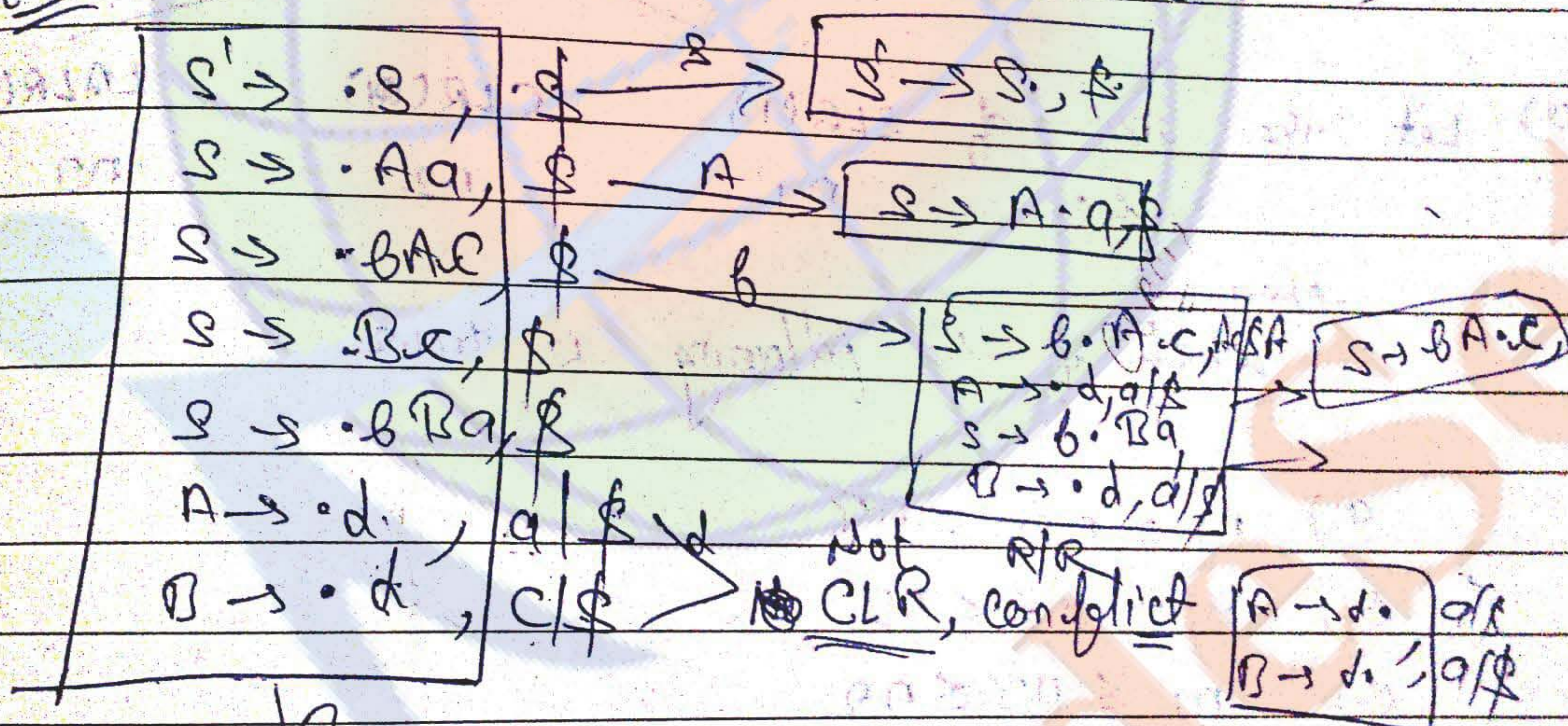
① LR(0) \subset SLR(1) \subset LALR(1) \subset CLR(1)
 every LR(0) is SLR(1) and every SLR(1) is LALR(1) and every LALR(1) is CLR(1).

a) The following grammar is

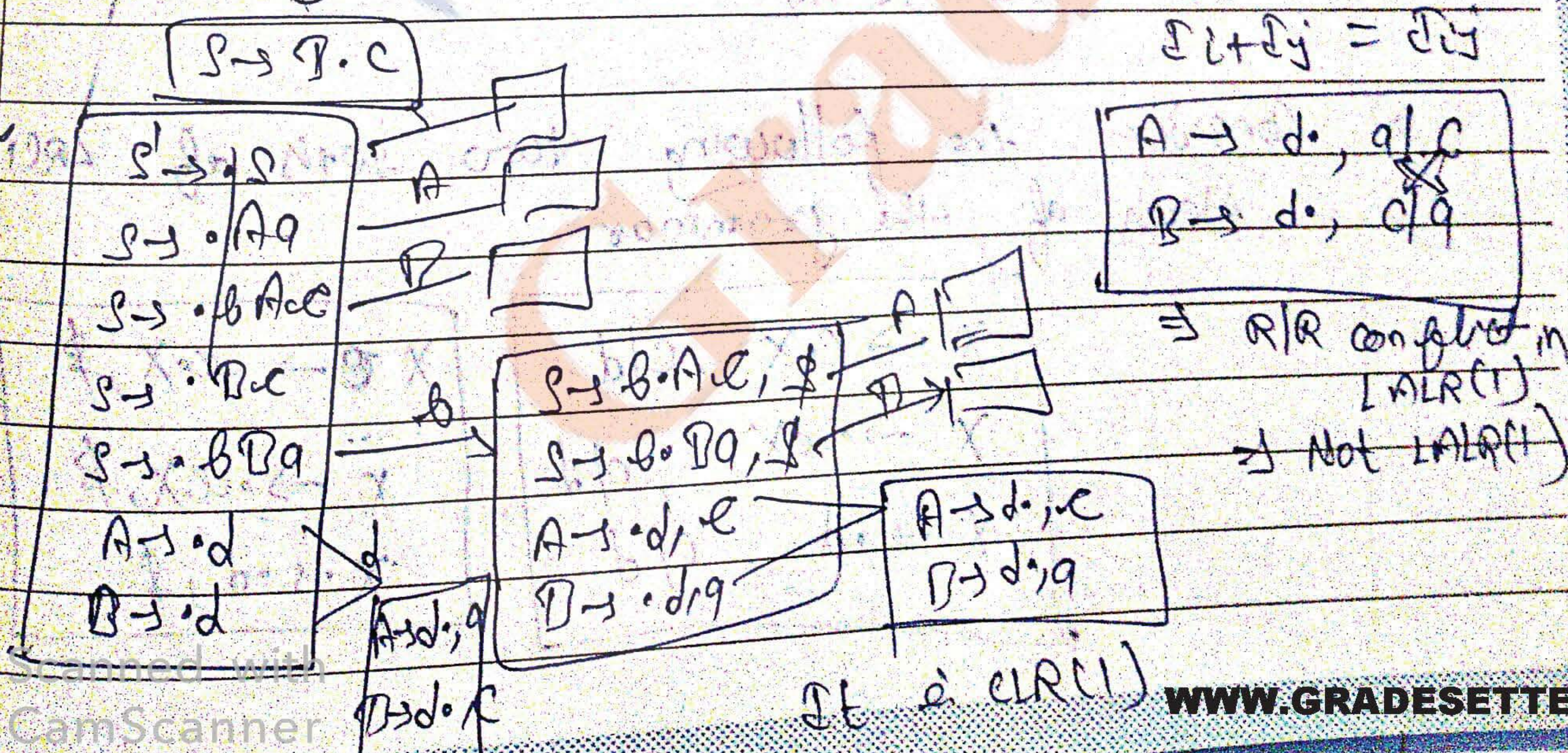
1) $G = \{ S \rightarrow Aa / bAc / Bc / bBa, A \rightarrow d, B \rightarrow d \}$

- a) LALR(1) but not CLR(1)
- b) CLR(1) but not LALR(1)
- c) both LALR(1) & CLR(1)
- d) Neither LALR(1) nor CLR(1)

8/7 own



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SLR	LALR(1)	CLR(1)
1) SLR is the smaller in size	1) The size of LALR is same as SLR	1) CLR is largest size
2) SLR is an easy method based on follow function	2) This method can be applicable more under class than SLR	2) CLR is the most powerful method than SLR & LALR
3) Error detection is not immediate	3) Not immediate	3) Immediate error detection

Q) Let the sizes of SLR(1) CLR(1) LALR(1) be n_1 , n_2 , n_3 respectively then

which of the following is true

- a) $n_1 = n_2 = n_3$
- b) $n_1 = n_2 < n_3$
- c) $n_1 \leq n_3 \leq n_2$
- d) $n_1 = n_3 < n_2$

Q) Consider the following two sets of LR(1) items of the grammar

$X \rightarrow c \cdot X, c/d$
 $X \rightarrow \cdot c X, c/d$
 $X \rightarrow \cdot d, c/d$

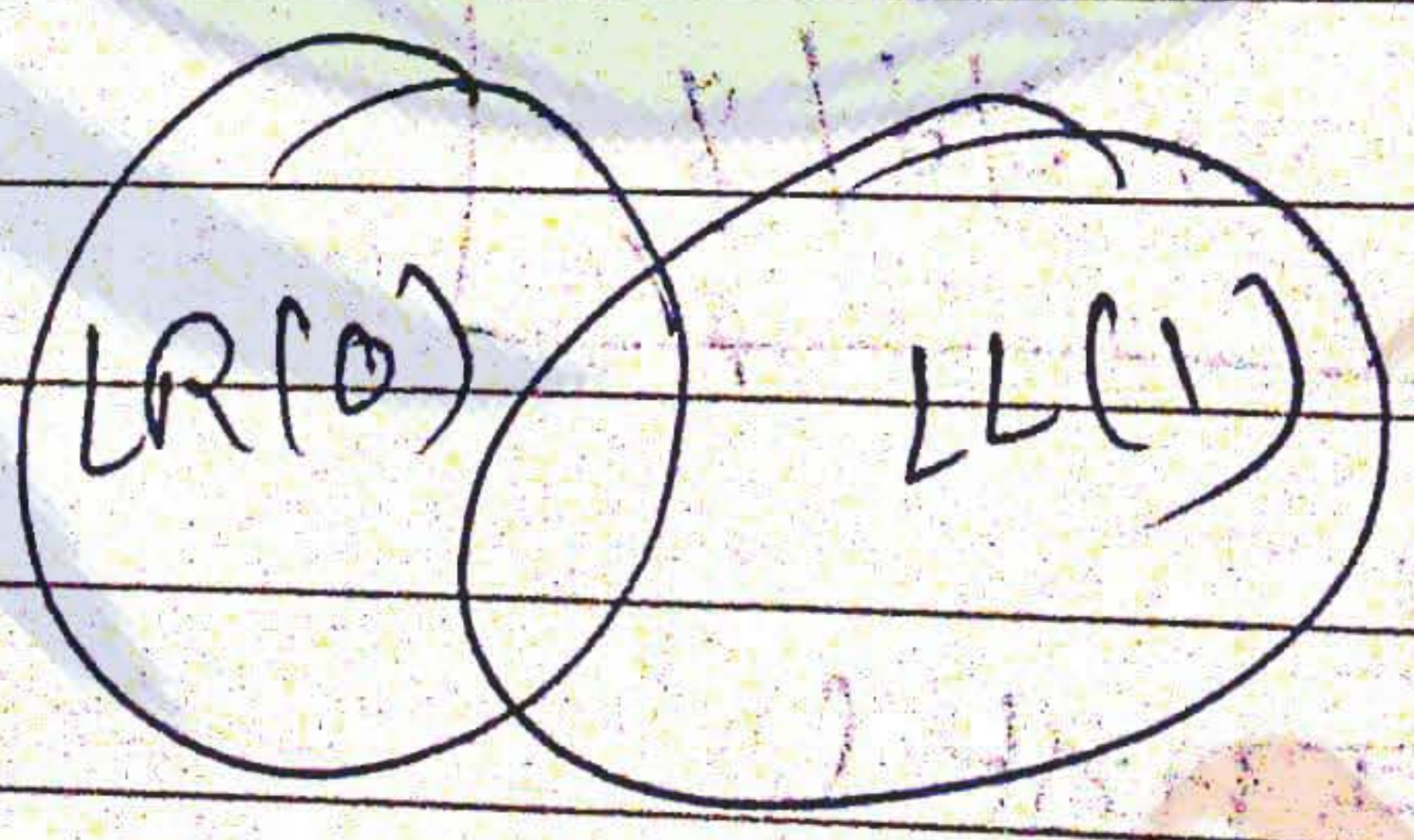
$X \rightarrow c \cdot X, \$$
 $X \rightarrow \cdot c X, \$$
 $X \rightarrow \cdot d, \$$

Note

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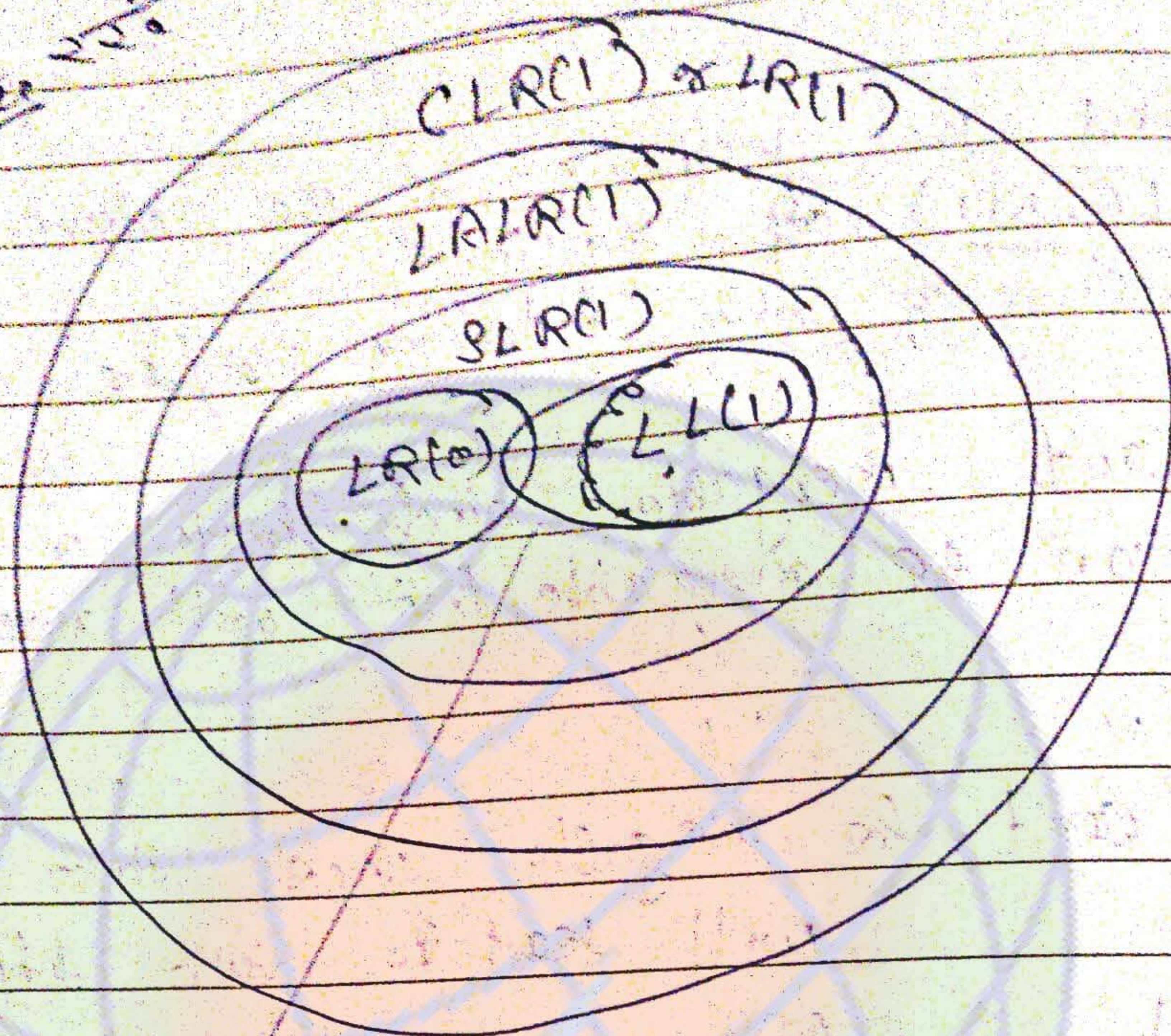
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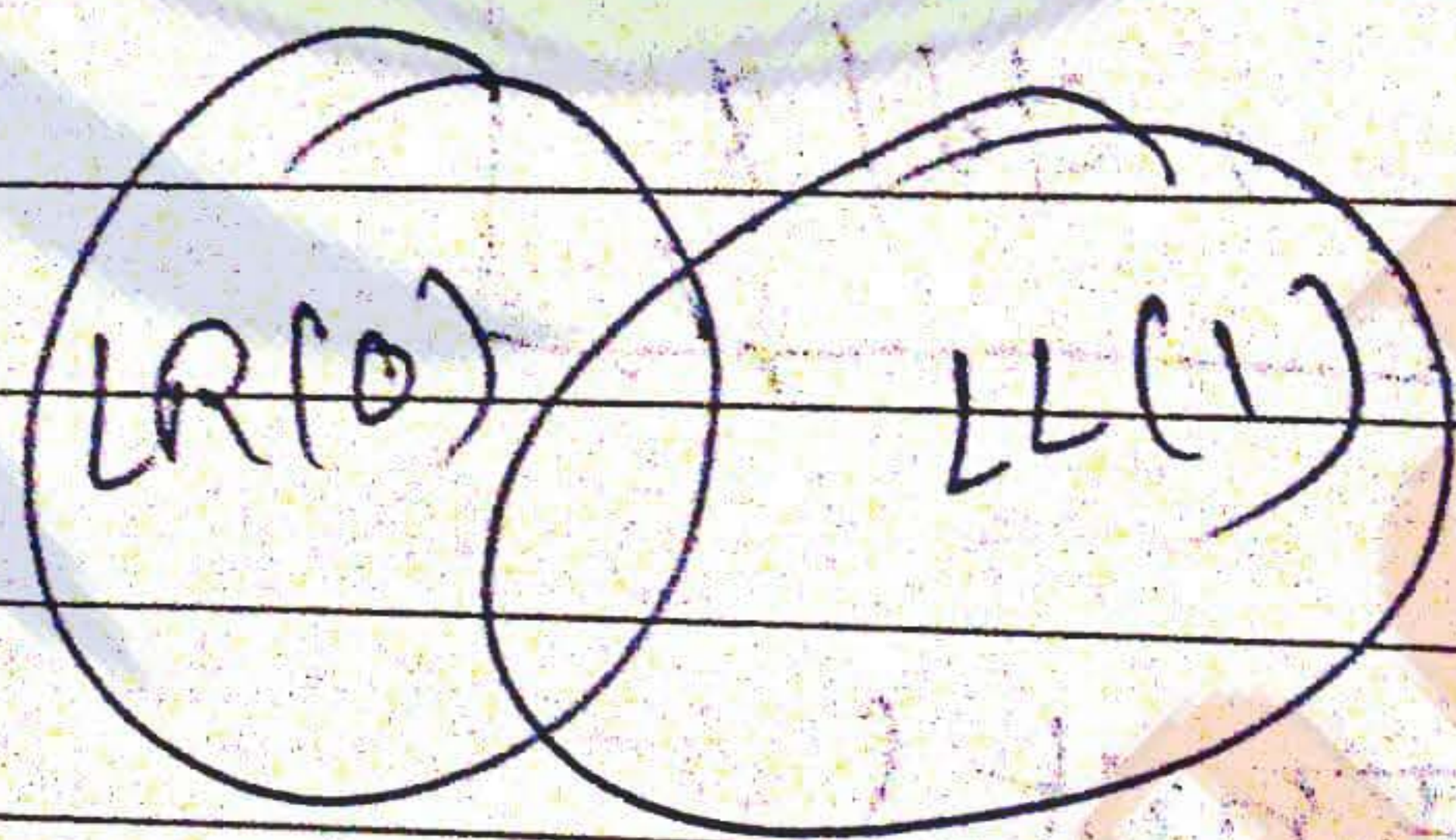
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विवरण
प्रमाण



कभी यह कुछ तिम हुआ भी होता है



Semantic Analysis

Note

Grammar + ~~Semantic~~ ^{Page No.} = Syntax ^{Date}
 directly ~~translates~~
 (S.D.D)

The tokens generated by lexical analyser will be grouped together in ~~some~~ syntax analysis to form a parse tree, it can not check the meaning of the source code.

The meaning of the source code will be verified in semantic analysis.

This can be done by attaching some rules to every production of the grammar.

The grammar with semantic rules is called syntax

~~The~~ Consider the following grammar with semantic rules

~~if~~ ~~1 + 2 * 3~~

$$E \rightarrow E + E \quad \{ E.val = E.val + E.val \}$$

$$E \rightarrow E * E \quad \{ E.val = E.val * E.val \}$$

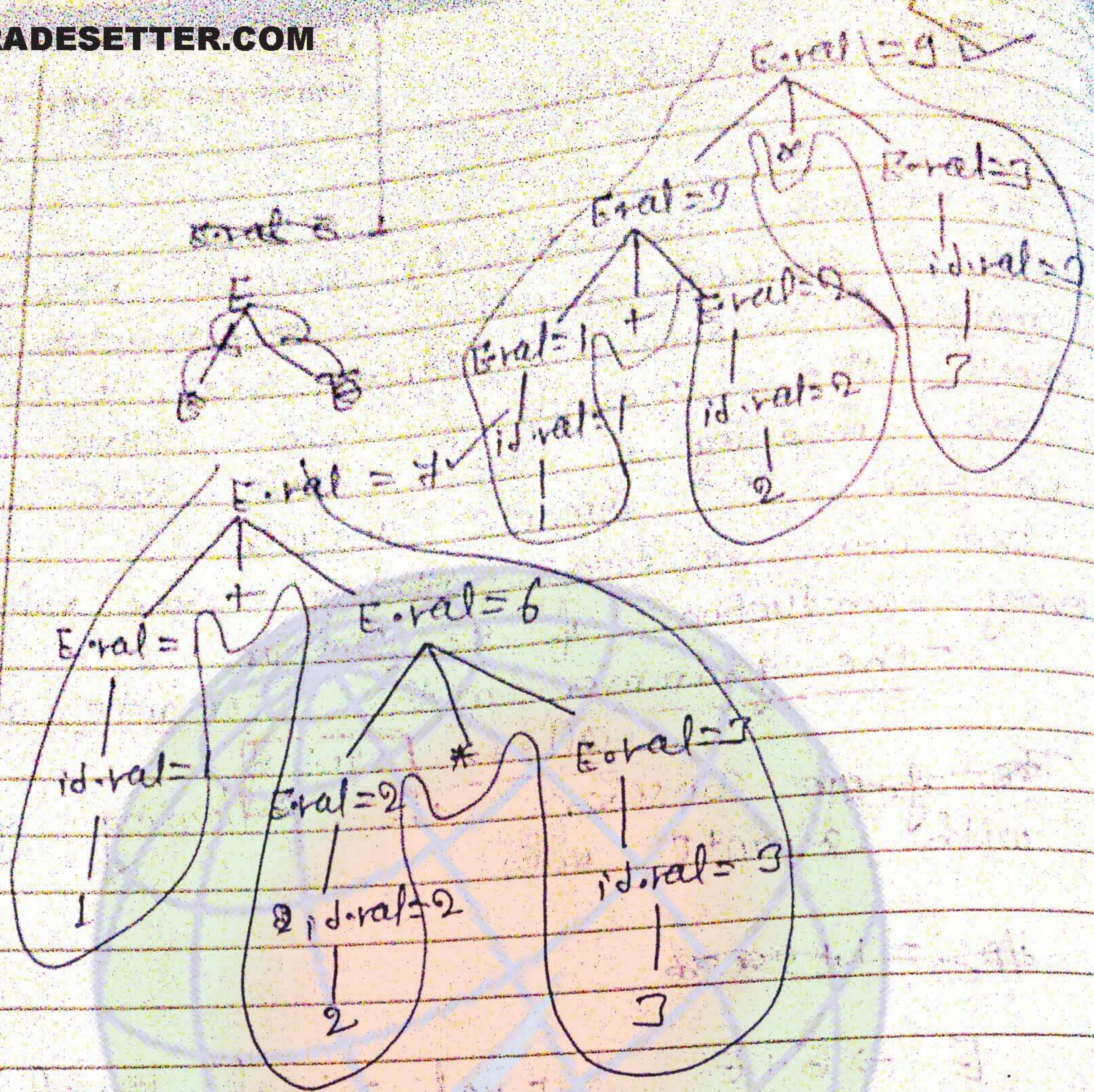
$$E \rightarrow id \quad \{ E.val = id.val \}$$

if the input is

if $1 + 2 * 3$ then o/p is

- a) 7 b) 9 c) both 7 & 9, (D) none
 because ambiguous

$1 + 2 * 3$
 $id + id * id$



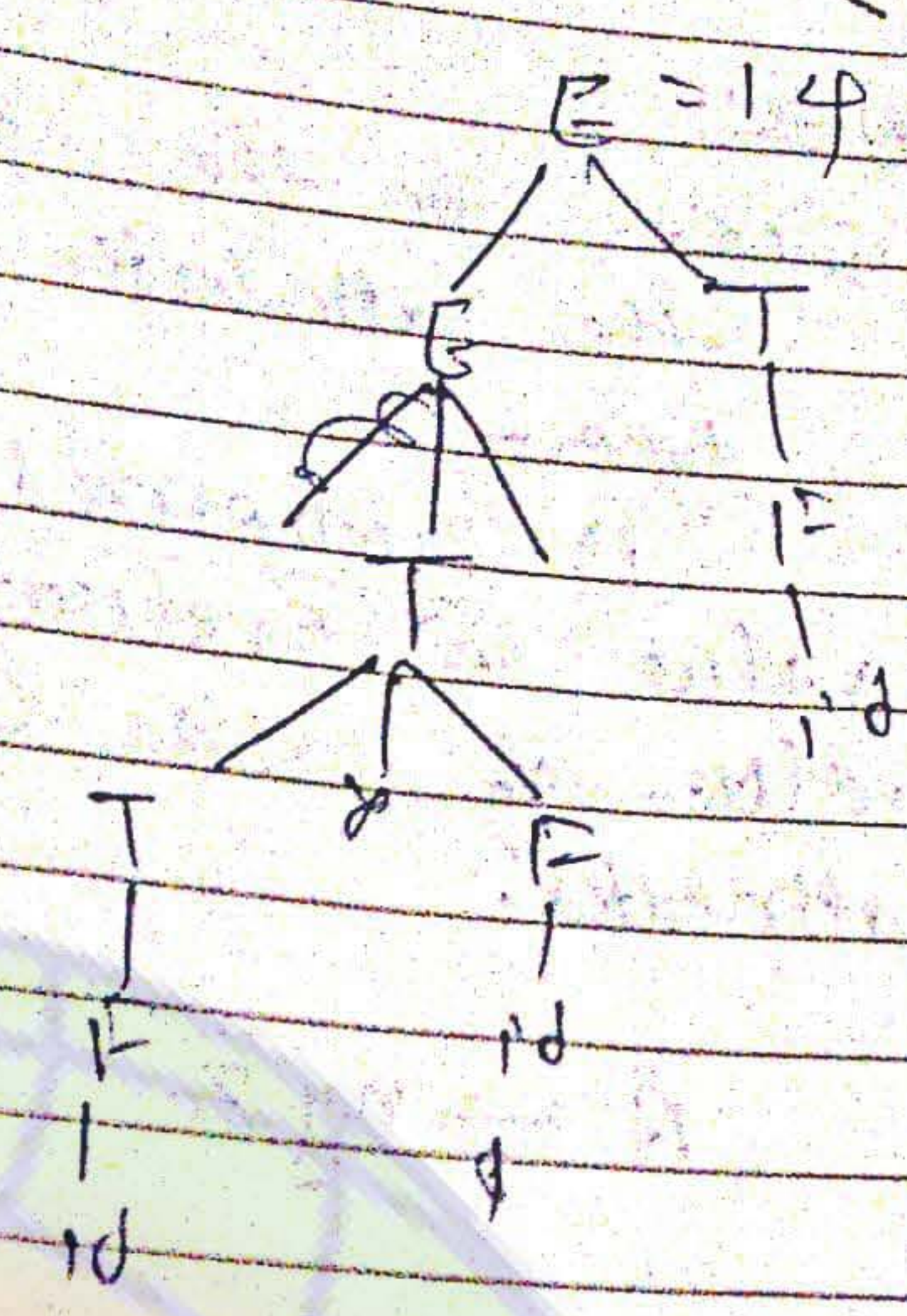
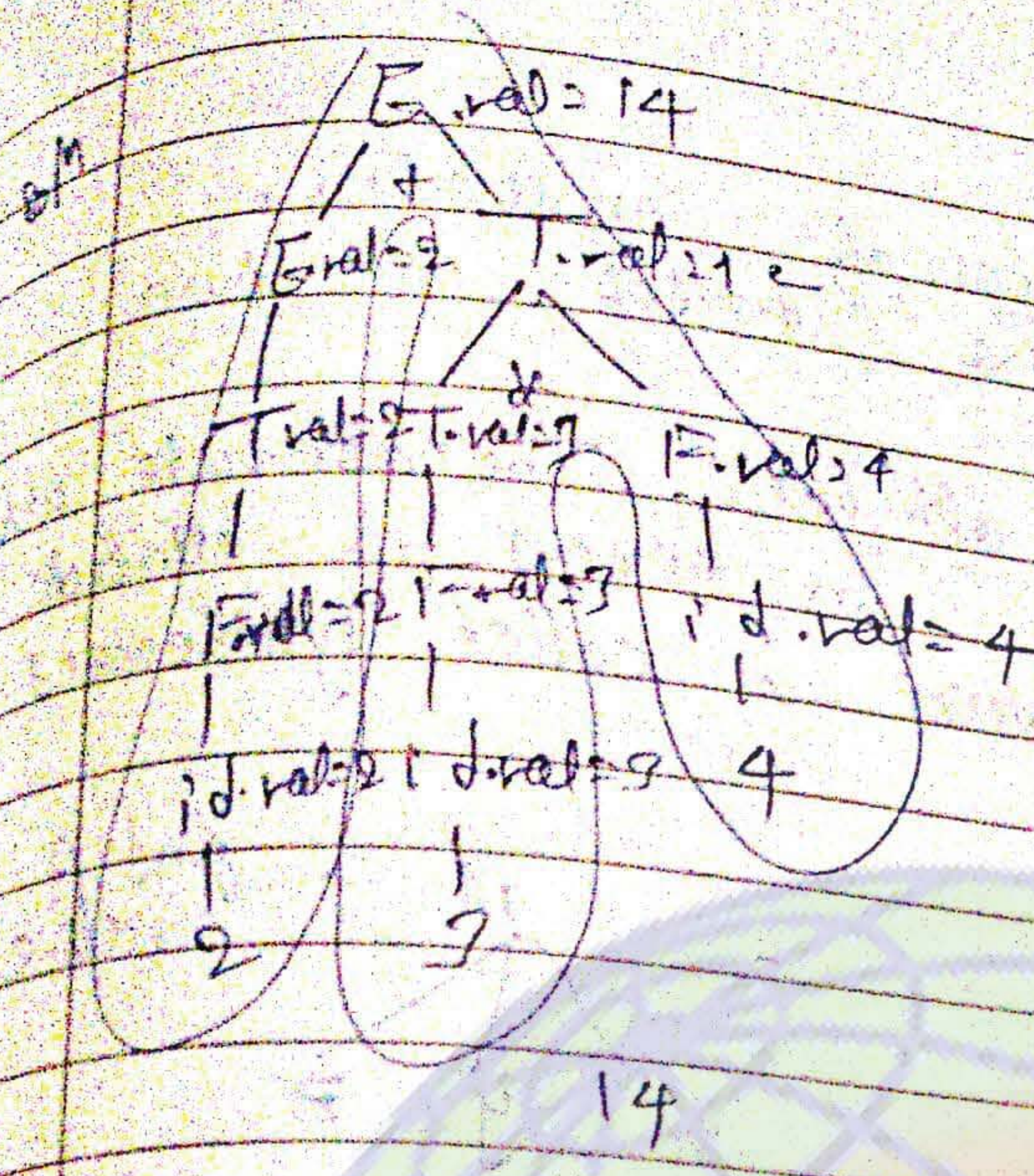
Ambiguous

Q2.) Consider the following grammar with semantic rule.

- $E \rightarrow E + T$ $\{ E.val = E_1.val + T.val \}$
- $E \rightarrow T$ $\{ E.val = T.val \}$
- $T \rightarrow T * F$ $\{ T.val = T_1.val * F.val \}$
- $T \rightarrow F$ $\{ T.val = F.val \}$
- $F \rightarrow id$ $\{ F.val = id.val \}$

If i/p = $2 + 3 * 4$ then o/p is

- a) 14 b) 20 c) 14 & 20 d) None



a) Consider the following grammar with semantic rules

$E \rightarrow E + T$ { Print (" + "); }

$E \rightarrow T$ { }

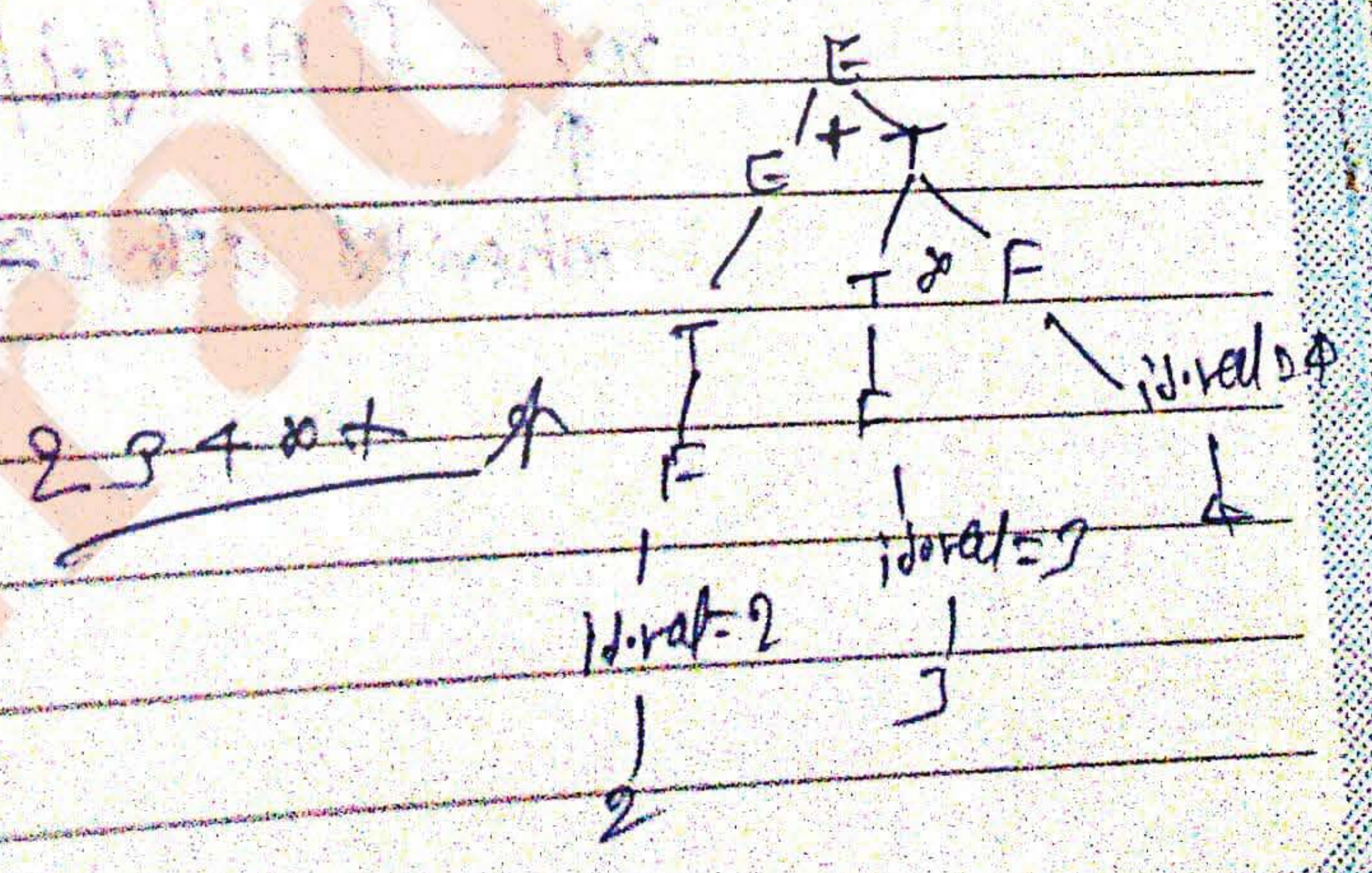
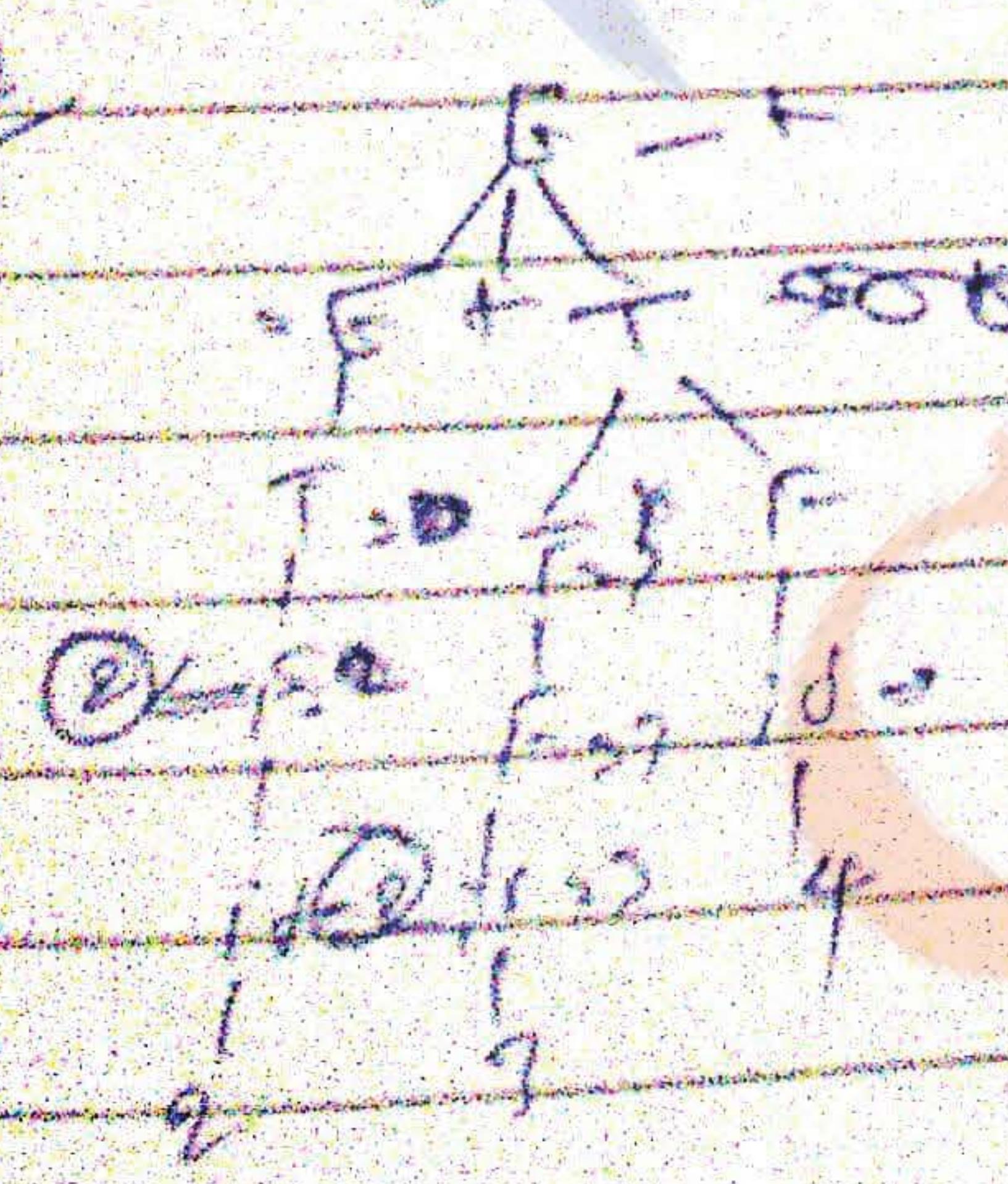
$T \rightarrow T * F$ { Print (" * "); }

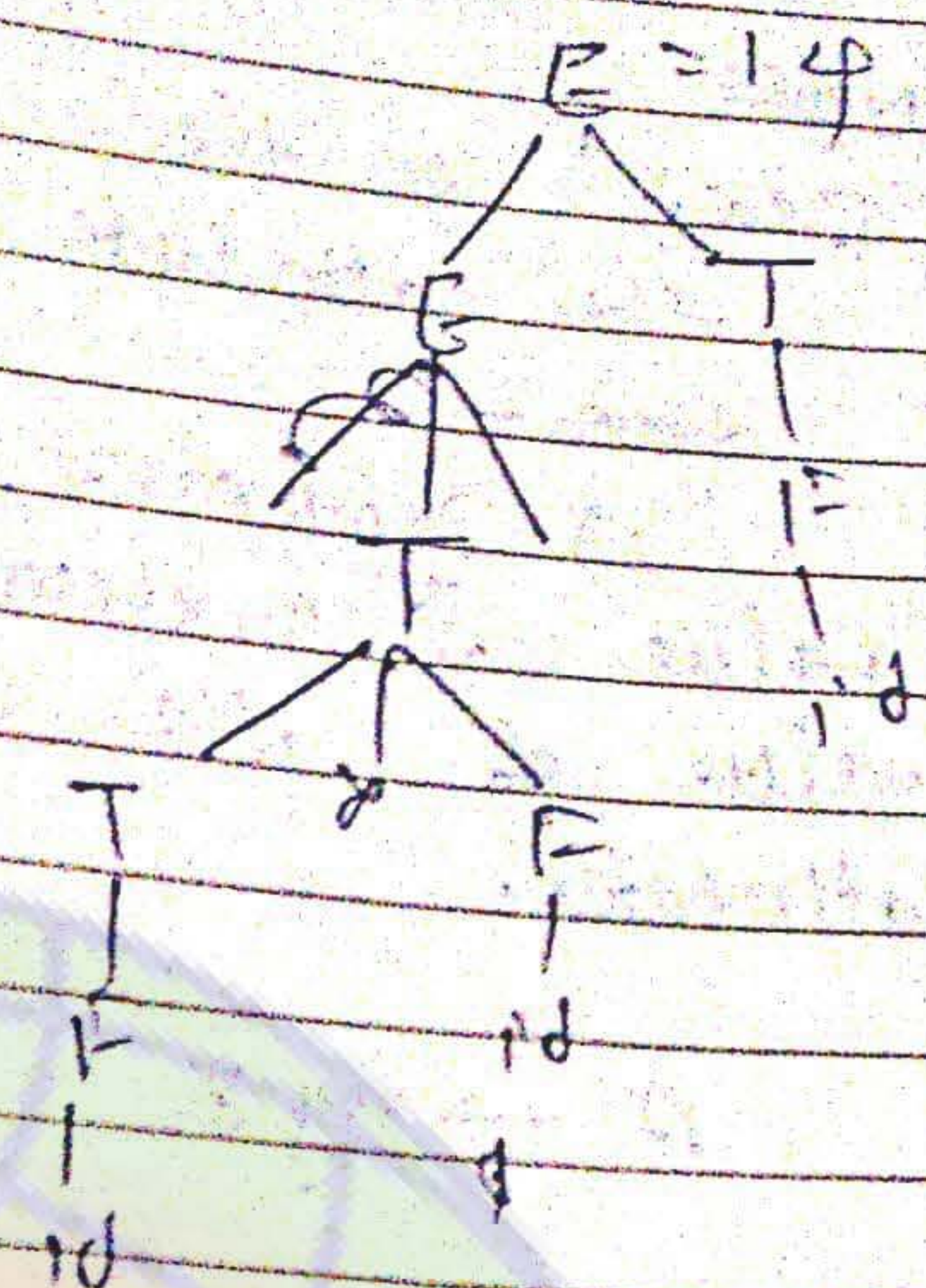
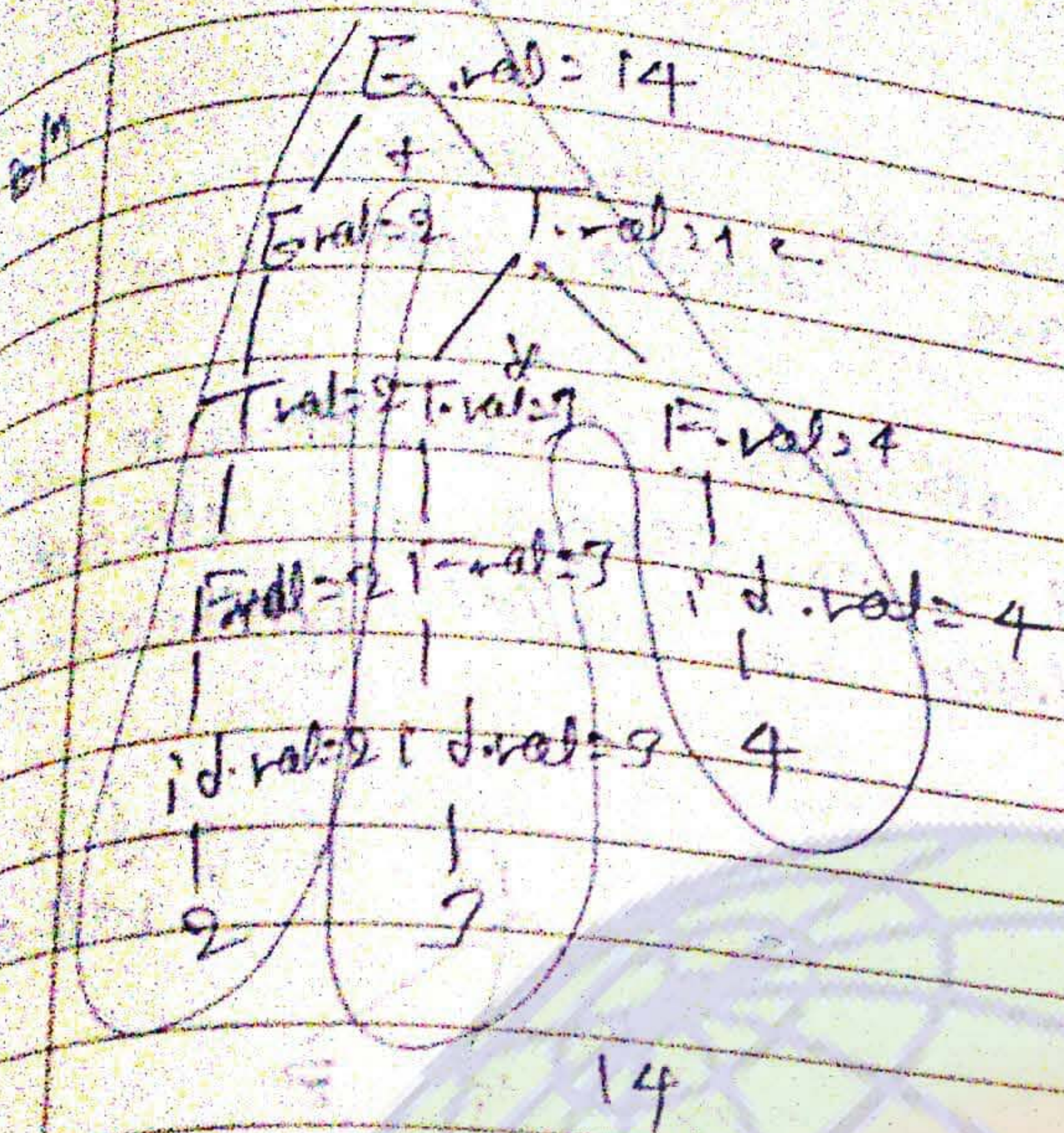
$T \rightarrow F$ { }

$F \rightarrow id$ { Print (id.val); }

If $2+3*4$ then $O/P = 9$

- 9) $234 + *$ b) $234 * +$ c) $23 * 4 +$ d) 14



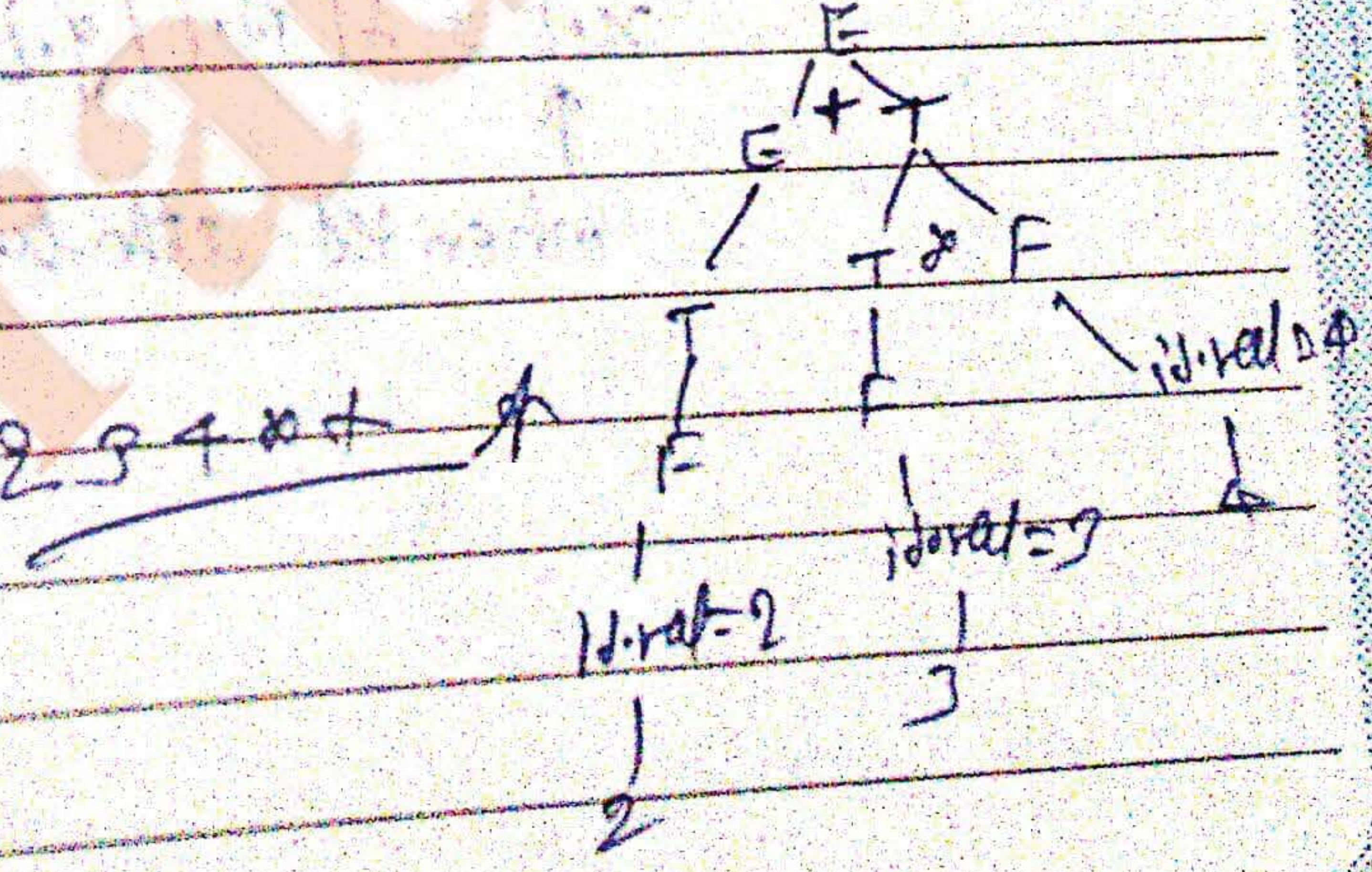
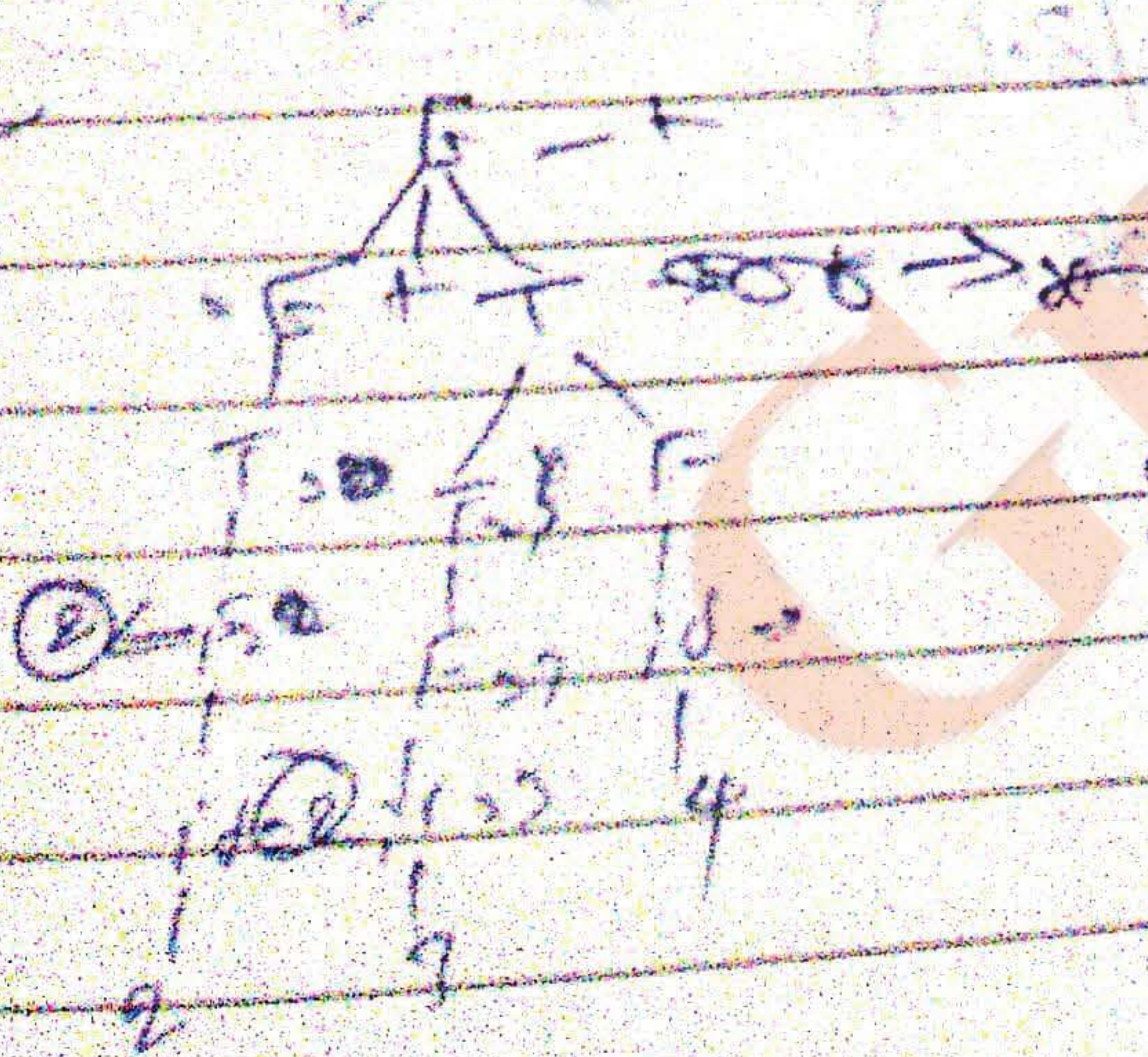


8) Consider the following grammar with semantic rules

- $E \rightarrow E + T$ { printf (" + "); }
- $E \rightarrow T$ { }
- $T \rightarrow T * F$ { printf (" * "); }
- $T \rightarrow F$ { }
- $F \rightarrow id$ { printf (id.val); }

If $i/p = 2 + 3 * 4$ then $o/p = ?$

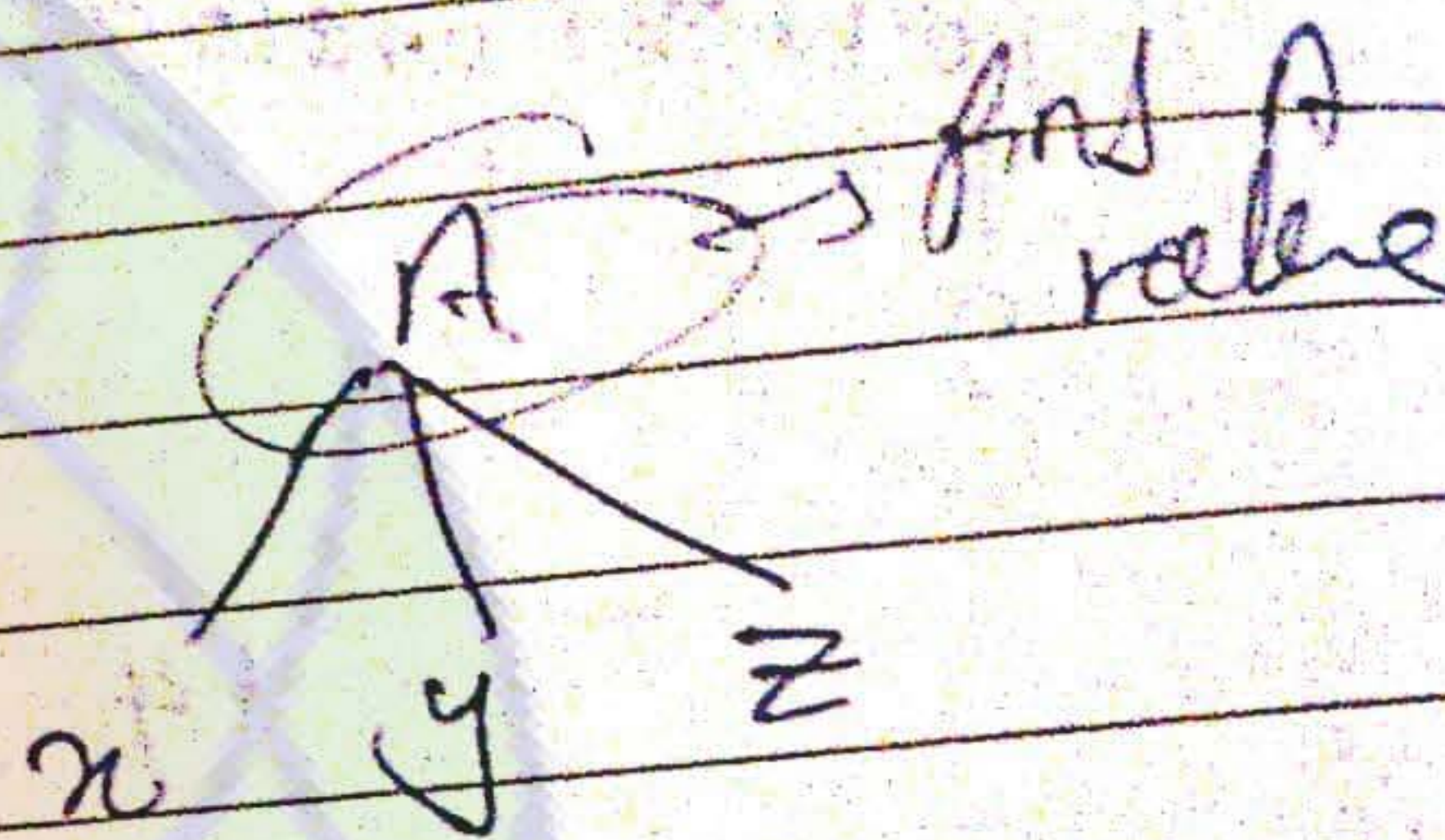
- a) $234 + * \quad$ b) $234 * + \quad$ c) $23 * 4 + \quad$ d) 14



Note:
Based on the process of evaluation, the attributes are divided into two types -

1) Synthesized attributes: The attribute whose value is evaluated in terms of attribute values of its children is called synthesized attributes.

$$A \rightarrow xyz$$



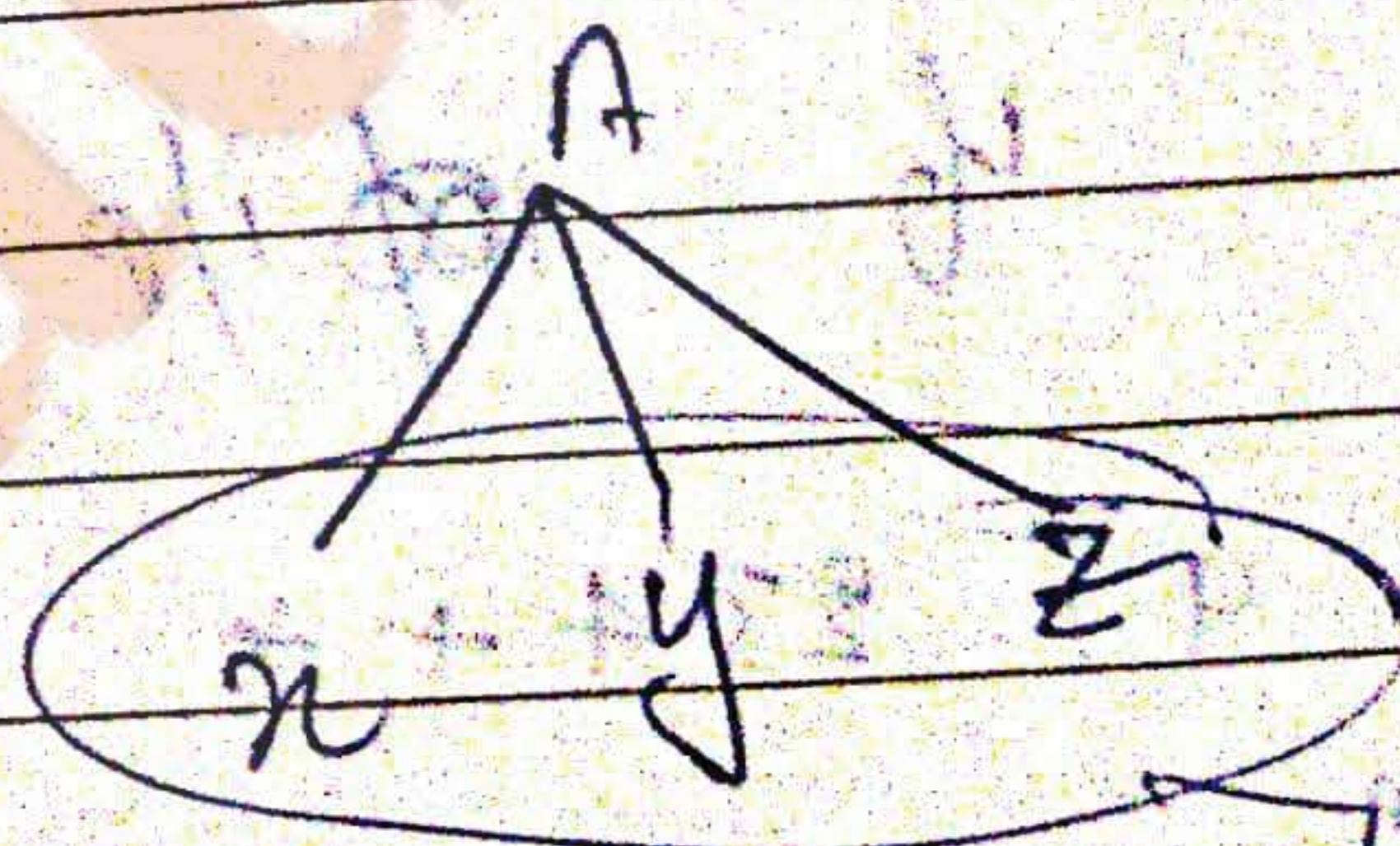
$$A \cdot \alpha = f(x \cdot \alpha / y \cdot \alpha / z \cdot \alpha)$$

↑
Synthesizes attributes.

2) Inherited attributes -

The attribute whose value is evaluated in terms of its parent or sibling's is called inherited attribute.

$$A \rightarrow xyz$$



$$x \cdot i = f(A \cdot i / y \cdot i / z \cdot i)$$

↑
Inherits attribute.

find x, y, z value.

S-attribute

S-attribute

L-attribute

every S-attribute is L-attribute

R_i

synthesized attribute

L-attribute

If it is inherited value from the siblings only it's parent or left side of R_i both synthesized and inherited attribute, it must inherit the value from the parent or left side of R_i



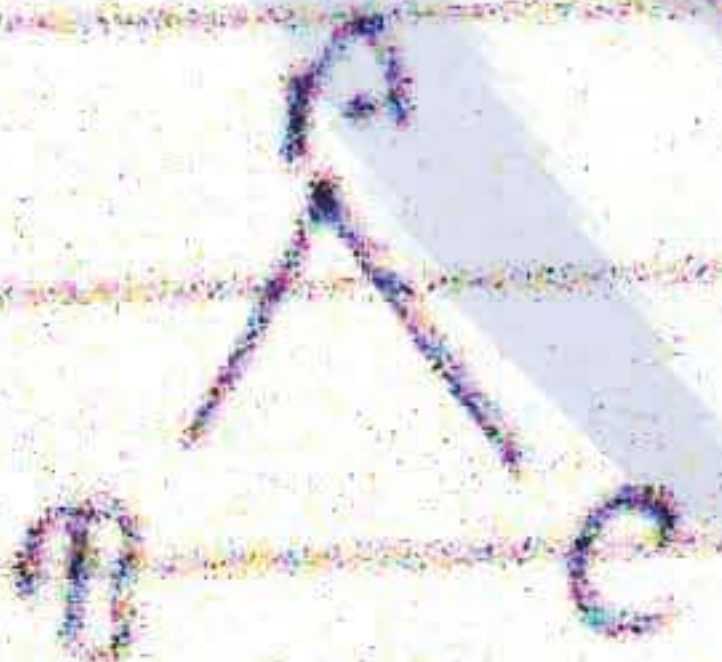
$y.i = (A.i)$ ✓

$x.i = (y.i)$ ✗ (Not L-attr)

2) The following grammar is

a) $A \rightarrow BC$ $\{ A.z = f(B.z) \& C.i = f(A.i) \}$

- a) S-attr ✓ b) L-attr ✓ c) both a & b ✓ d) None ✗



$A.z = f(B.z)$ ✓

$C.i = f(A.i)$

L-attr ✓

Not S ✗

L-attr ✓ ✓

S-attr ✓

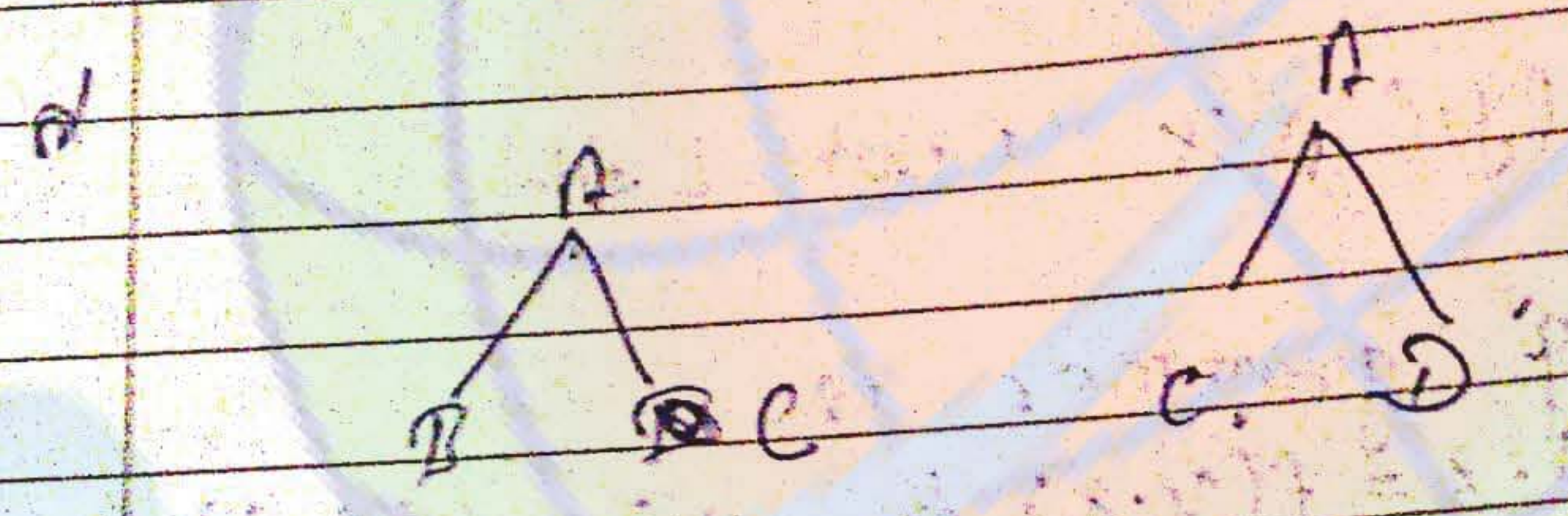
(e) $A \rightarrow BC$ $\left\{ \begin{array}{l} B \cdot i = f(A \cdot i); \\ C \cdot i = f(B \cdot i); \\ A \cdot j = f(B \cdot j) \end{array} \right.$

Not L

$A \rightarrow CD$ $\left\{ \begin{array}{l} A \cdot j = f(C \cdot j); \\ C \cdot i = f(D \cdot i); \\ D \cdot i = f(A \cdot i) \end{array} \right.$

Not L

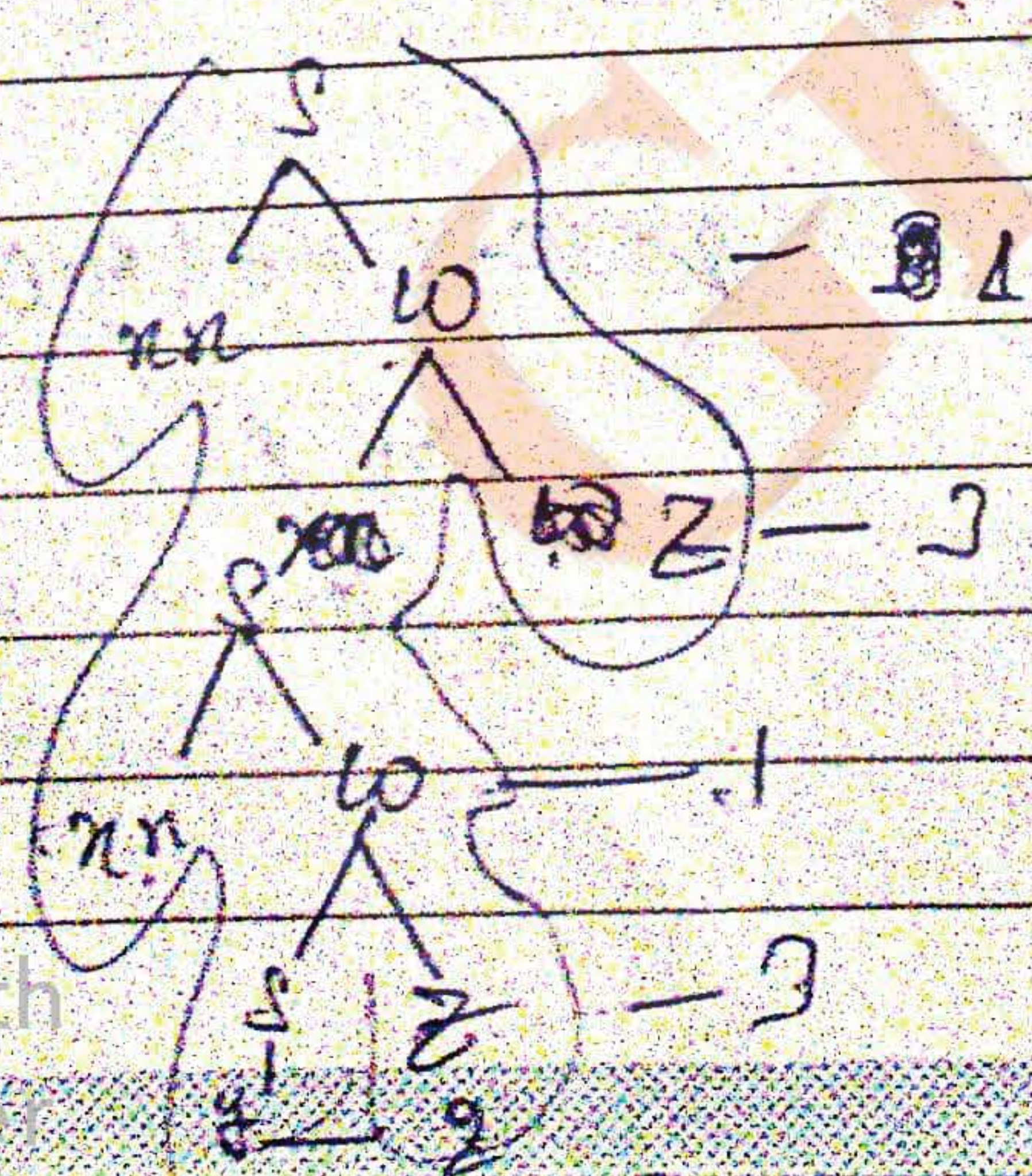
- a) S-attr b) L-attr c) both a & b is none



(c) $S \rightarrow xyz$ $\left\{ \begin{array}{l} \text{Print}(1); \\ \text{Print}(2); \\ \text{Print}(3); \end{array} \right.$

y
 $w \rightarrow z$

i/p = xyzxyz
then o/p = ?



2/2/2

more powerful

more powerful

consider

$E \rightarrow E^*$

IT

$T \rightarrow F$

IF

$F \rightarrow S$

IA

if

ans

consider the following

$E \rightarrow E * T$

IT

$\{ E.val = E.val * T.val \}$
 $\{ E.val = T.val \}$

$T \rightarrow F - T$

IF

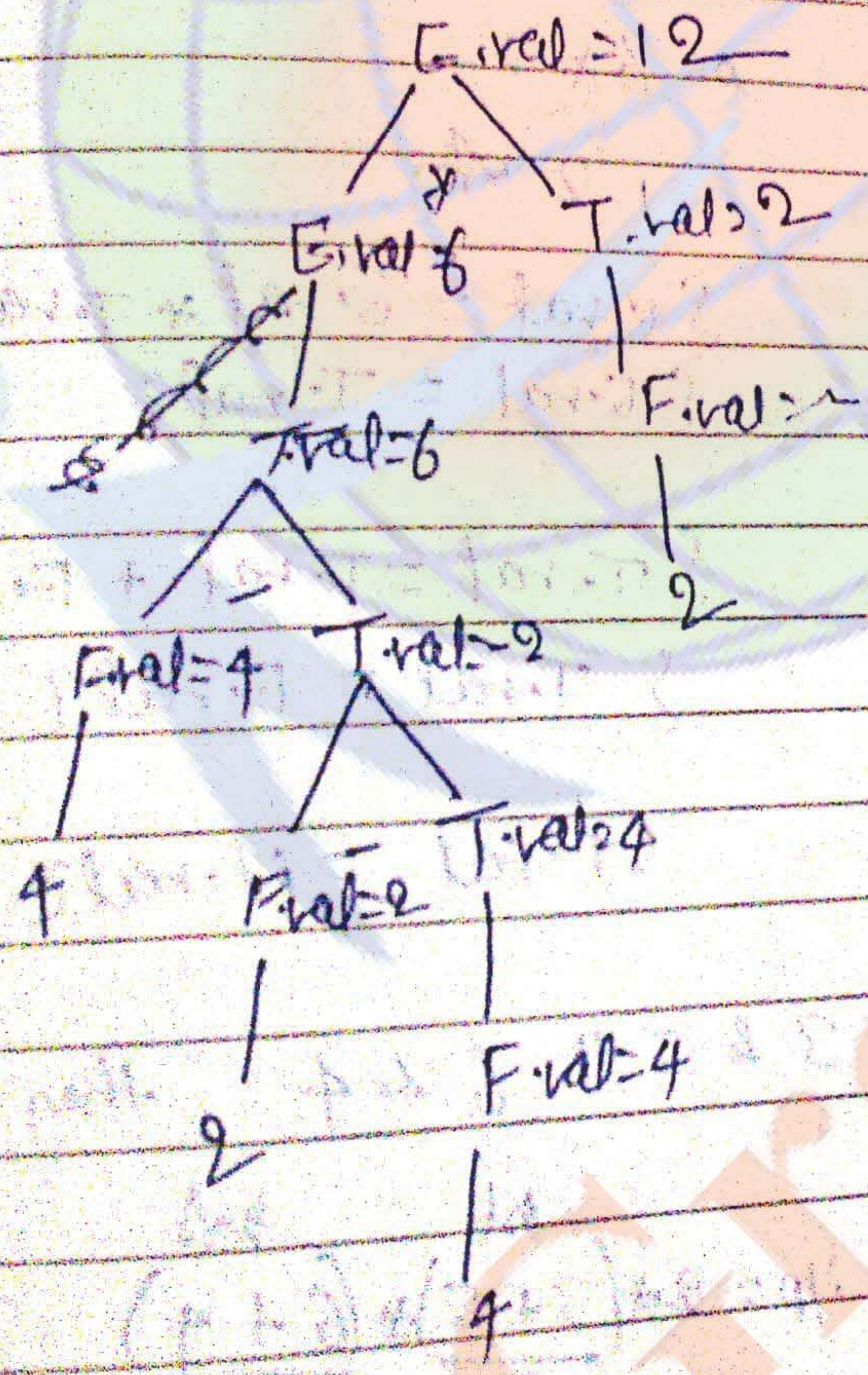
$\{ T.val = F.val - T.val \}$
 $\{ T.val = F.val \}$

$F \rightarrow 2$

4

$\{ F.val = 2 \}$
 $\{ F.val = 4 \}$

if $i/p = 4 - 2 - 4 * 2$ then $o/p = 9$

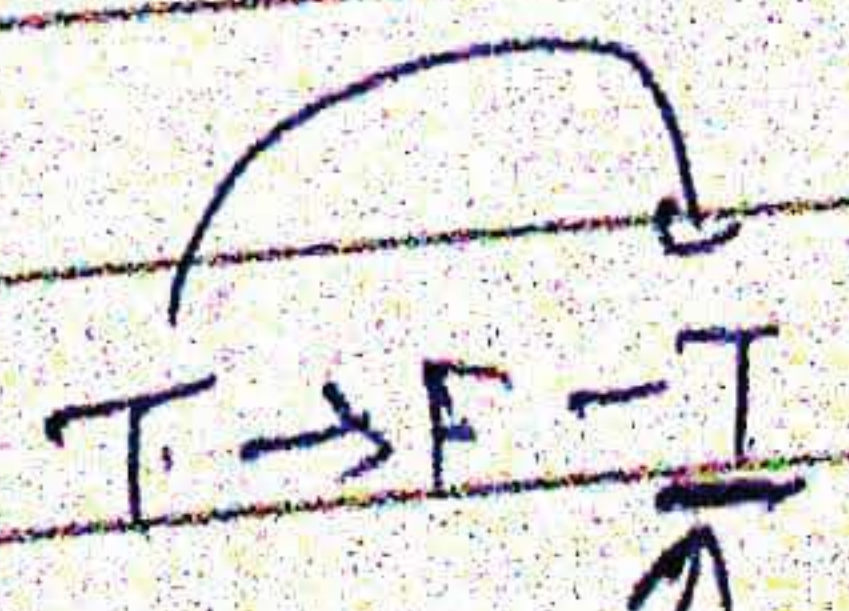


short cut

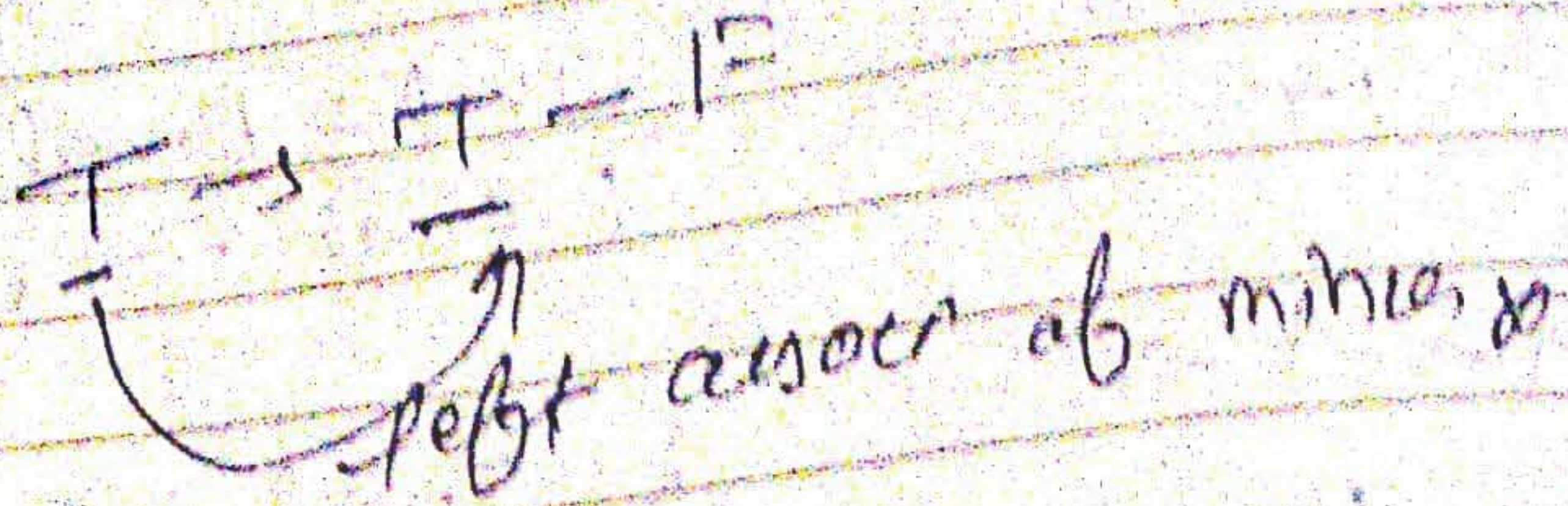
The lower operator is highest priority

$- \rightarrow *$

$-$ is right associative



Note:



$$\left((4 - (2 - 4)) * 2 \right)$$

$$(4 - (-2)) * 2$$

$$= 6 * 2$$

$$\{ E.val = E.val * T.val \}$$

$$\{ E.val = T.val \}$$

$$\{ T.val = T.val + F.val \}$$

$$\{ T.val = F.val \}$$

$$\{ F.val = id.val \}$$

a.) $E \rightarrow E \# T$
IT

$T \rightarrow T * F$
IF

$F \rightarrow id$

ip = 2 # 3 & 5 # 6 & 4 then op =)

soln

$$2 \rightarrow + \text{(last)} \quad \text{ip} = 2 * \left(\frac{3 + 5}{8} \right) * \left(\frac{6 + 4}{10} \right)$$

$\frac{\infty}{\infty}$ (left)

ip =

$$2 * 8 * 10$$

$$= 16 * 10$$

$$= 160 \text{ ans}$$

e) $N \rightarrow L$

$$\{ N.val = L.val \}$$

$L \rightarrow LB$

$$\{ L.val = L.val + B.val \}$$

ϵ

$$\{ L.val = B.val \}$$

$B \rightarrow 0$

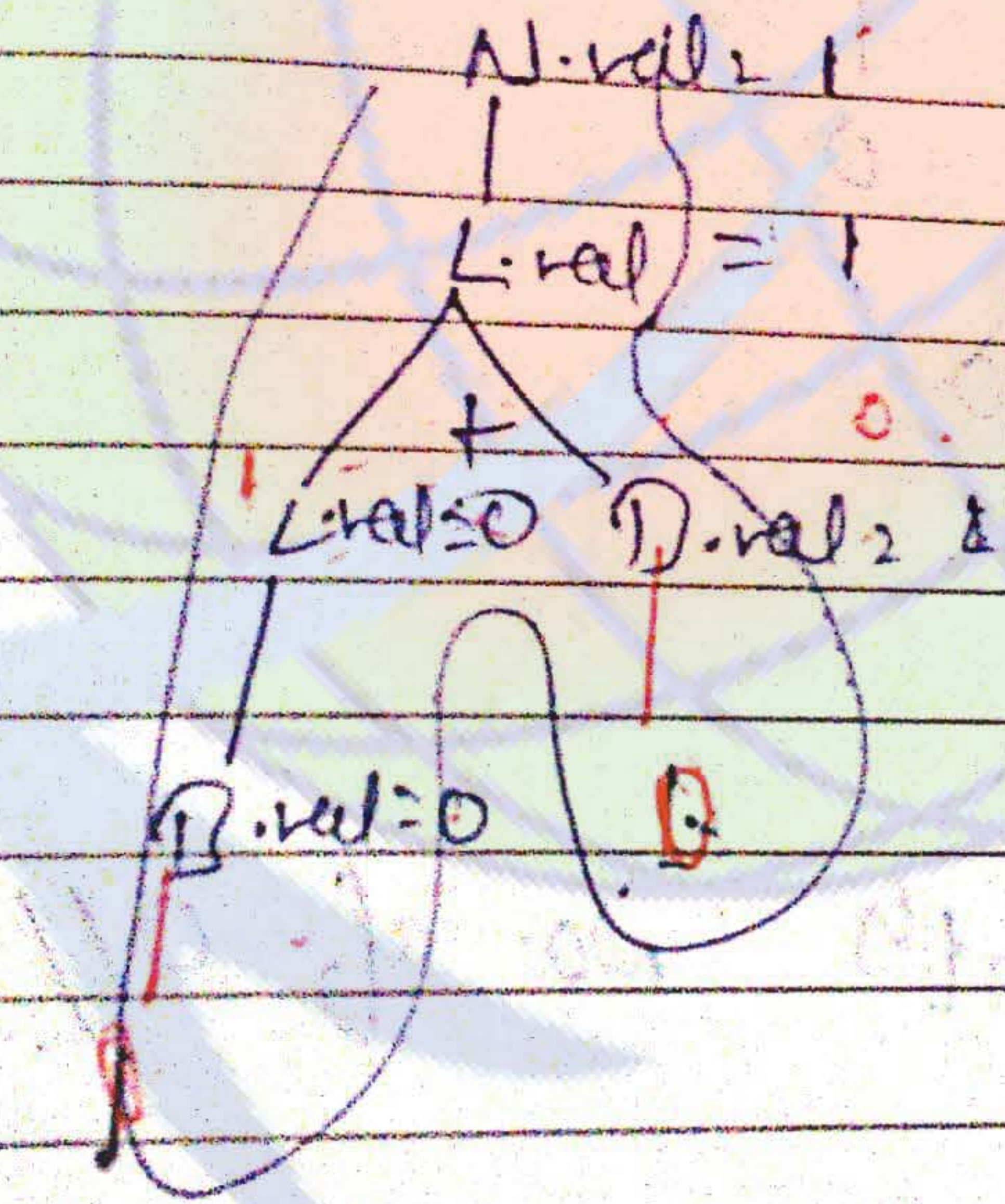
$$\{ B.val = 1 \}$$

ϵ

$$\{ B.val = 0 \}$$

what is the purpose of the grammar.

10/11



take any input

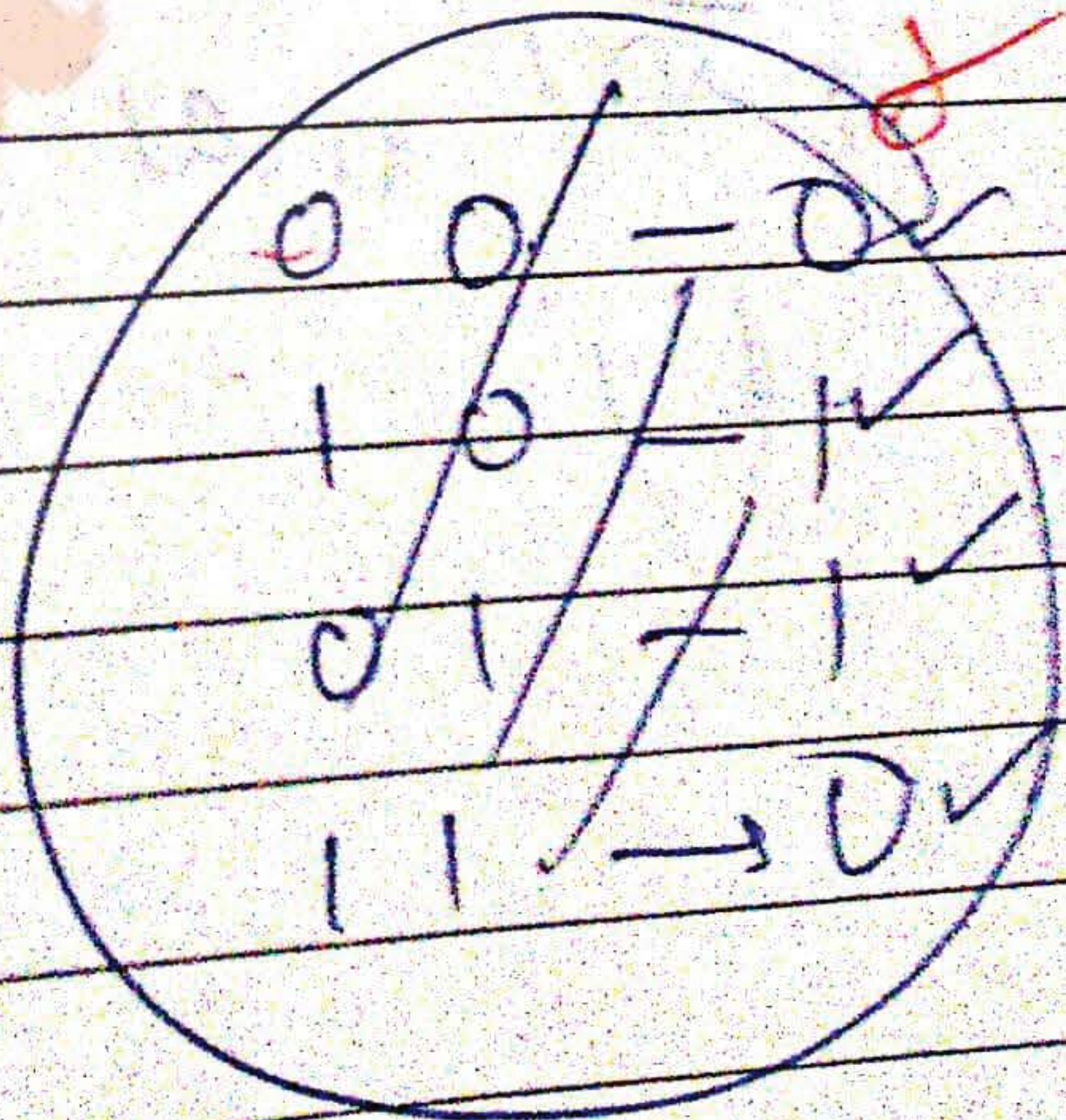
0100
BBB



10/11

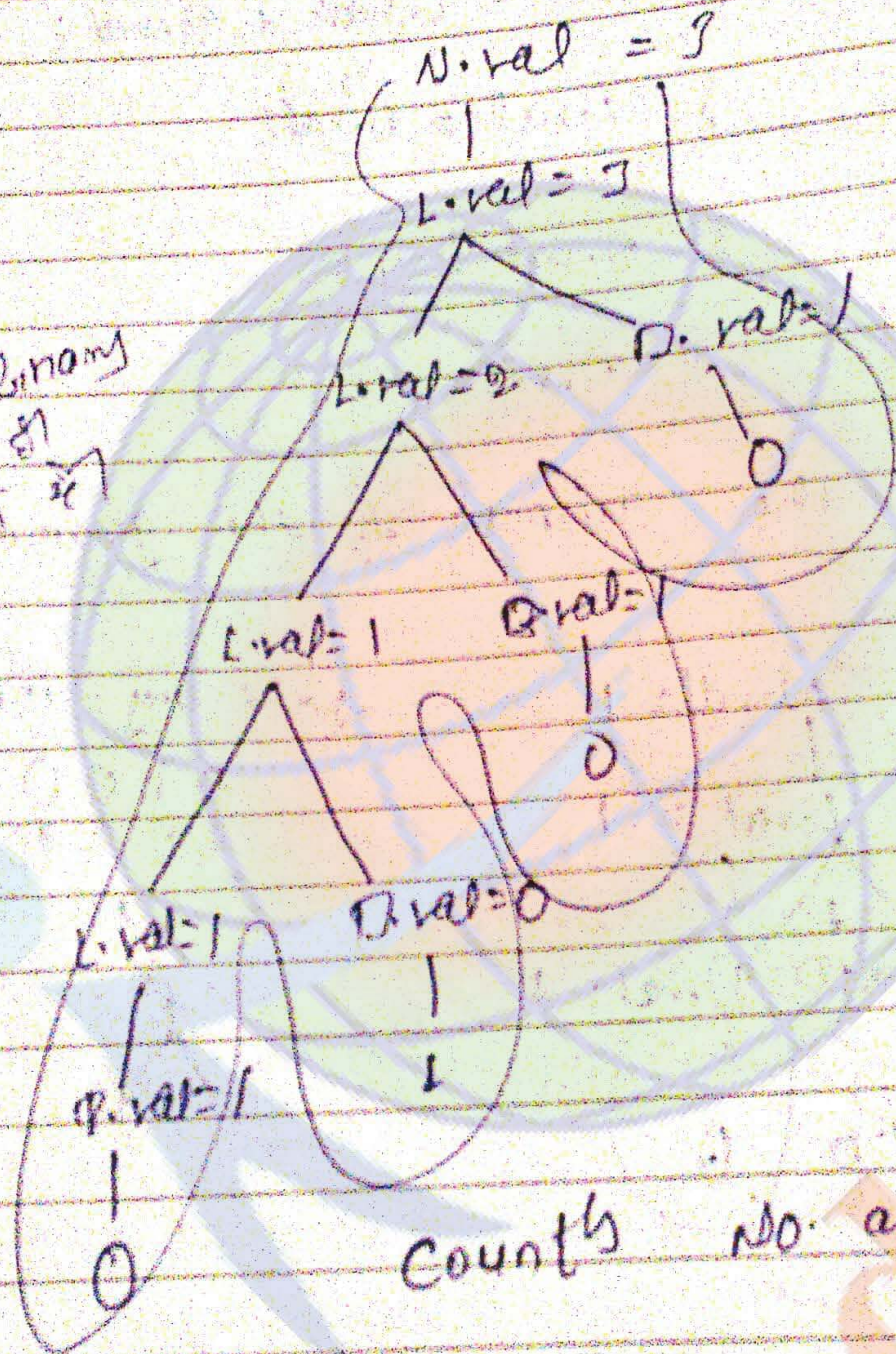
0100

10/11



0 1 0 0
1 1 1 1

Binary
1 0 1 1
0 1 1 1
1 1 1 1



Counts no. of 0/1

Note:

0 1 0 / 1 1 1 1

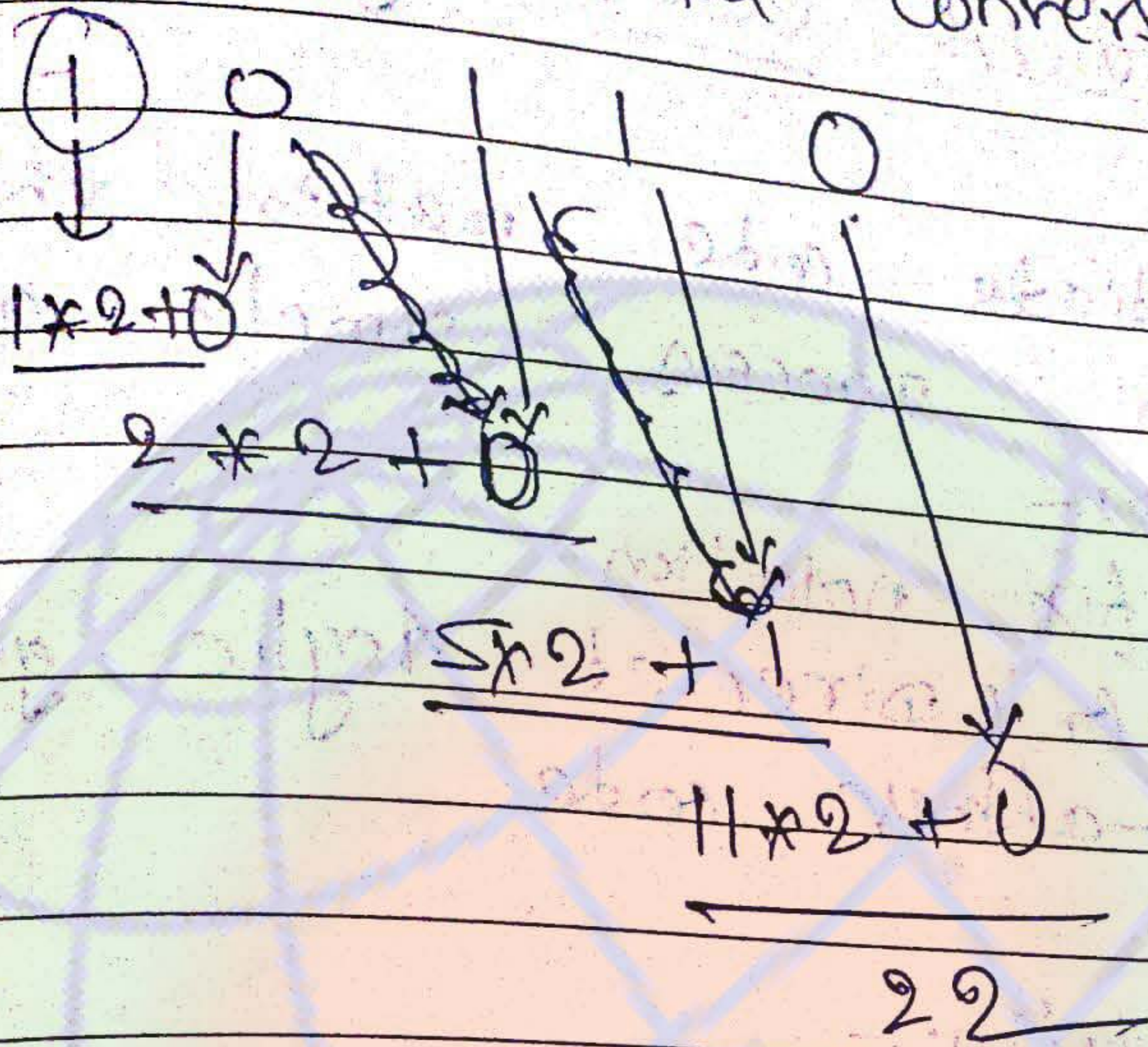
1 /



Count no of bits

Binary to Decimal Conversion

Page No. _____
Date _____



$$N \rightarrow L \quad \{ N \cdot \text{val} = L \cdot \text{val} \}$$

$$L \rightarrow LD \quad \{ L \cdot \text{val} = L \cdot \text{val} * 2 + B \cdot \text{val} \}$$

$$| B \quad \{ L \cdot \text{val} = B \cdot \text{val} \}$$

$$B \rightarrow 0 \quad \{ B \cdot \text{val} = 0 \}$$

$$| L \quad \{ B \cdot \text{val} = 1 \}$$

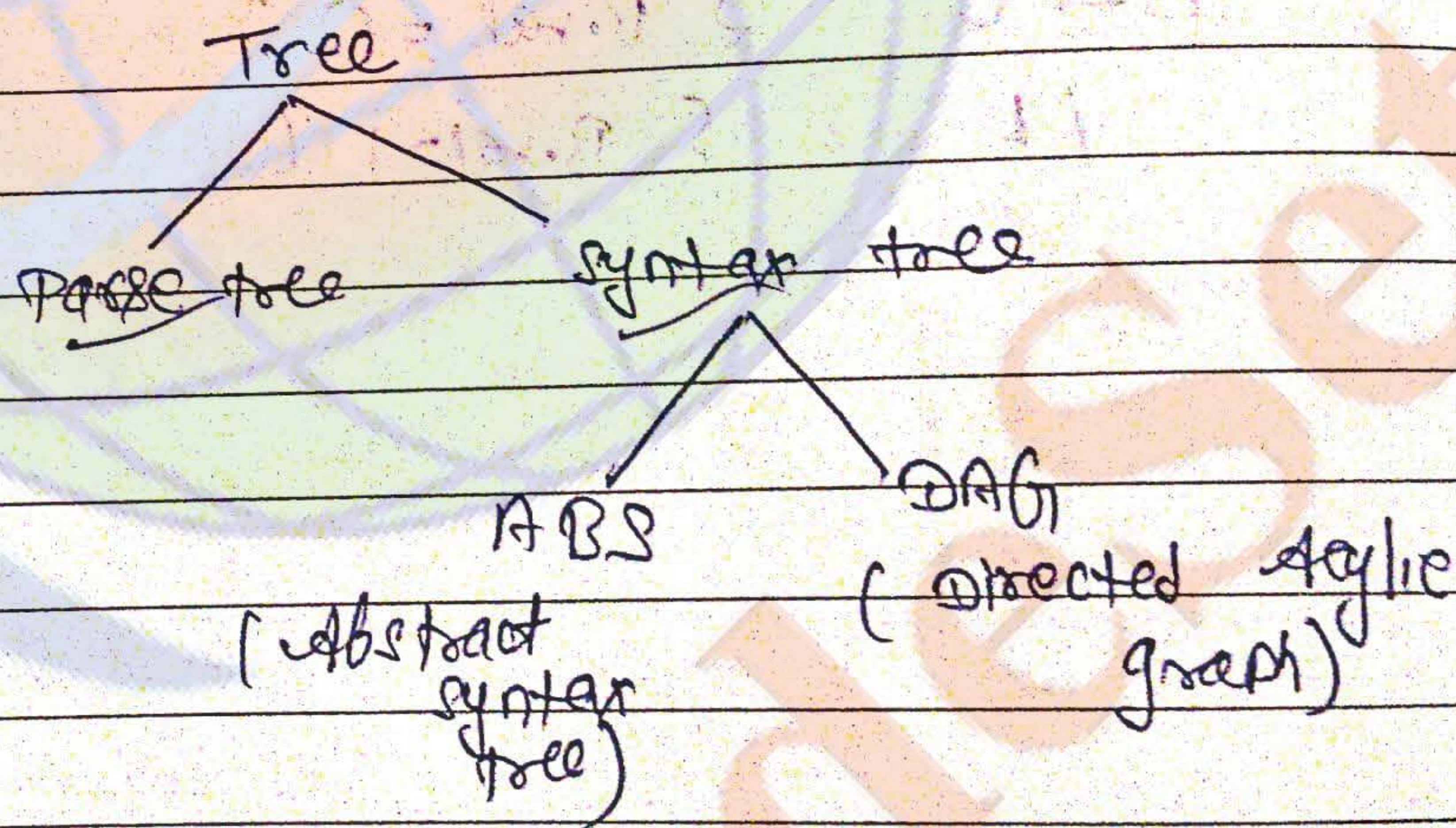
Intermediate code generation

Intermediate code generation process makes the code simple and easy.
 Representation:-

- 1) Post fix notation
- 2) DAG (Directed Acyclic graph)
- 3) 3-address code

① Post-fix notation:-

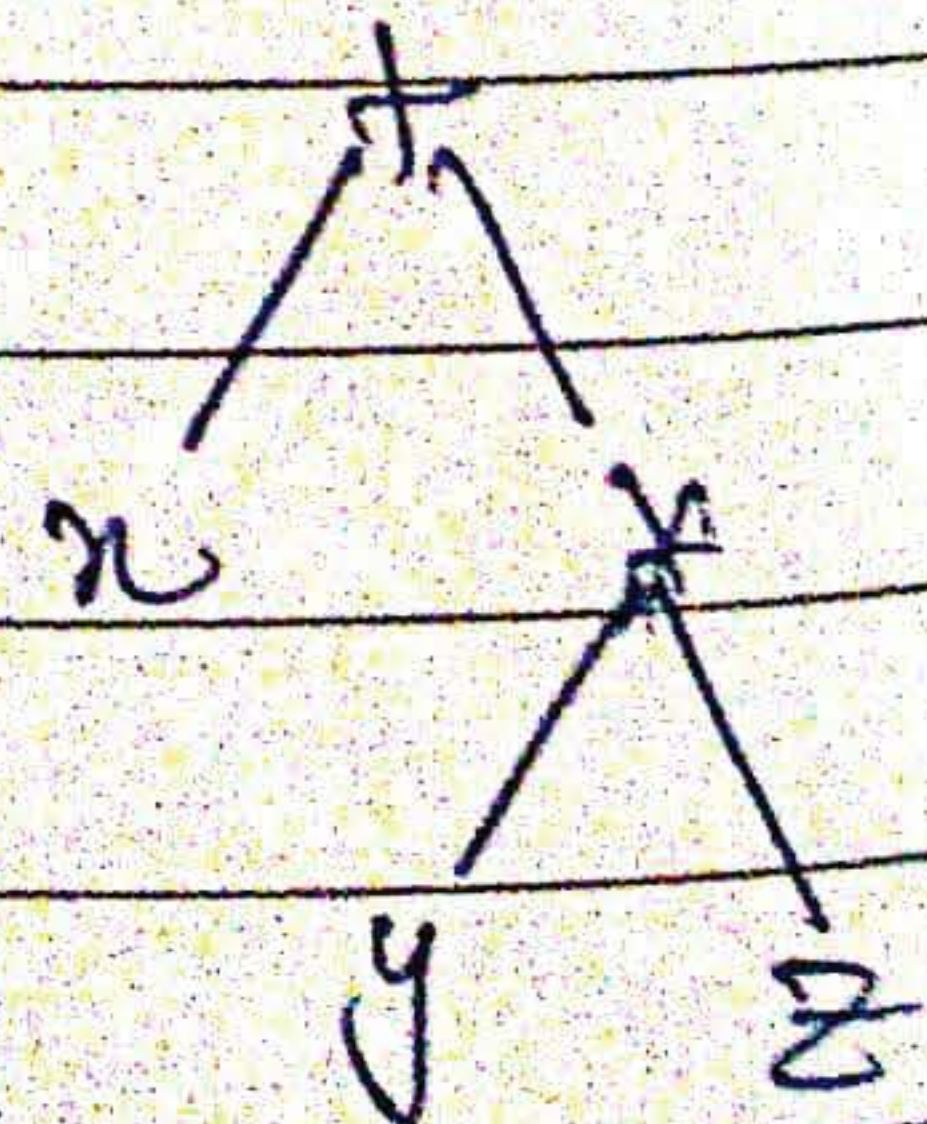
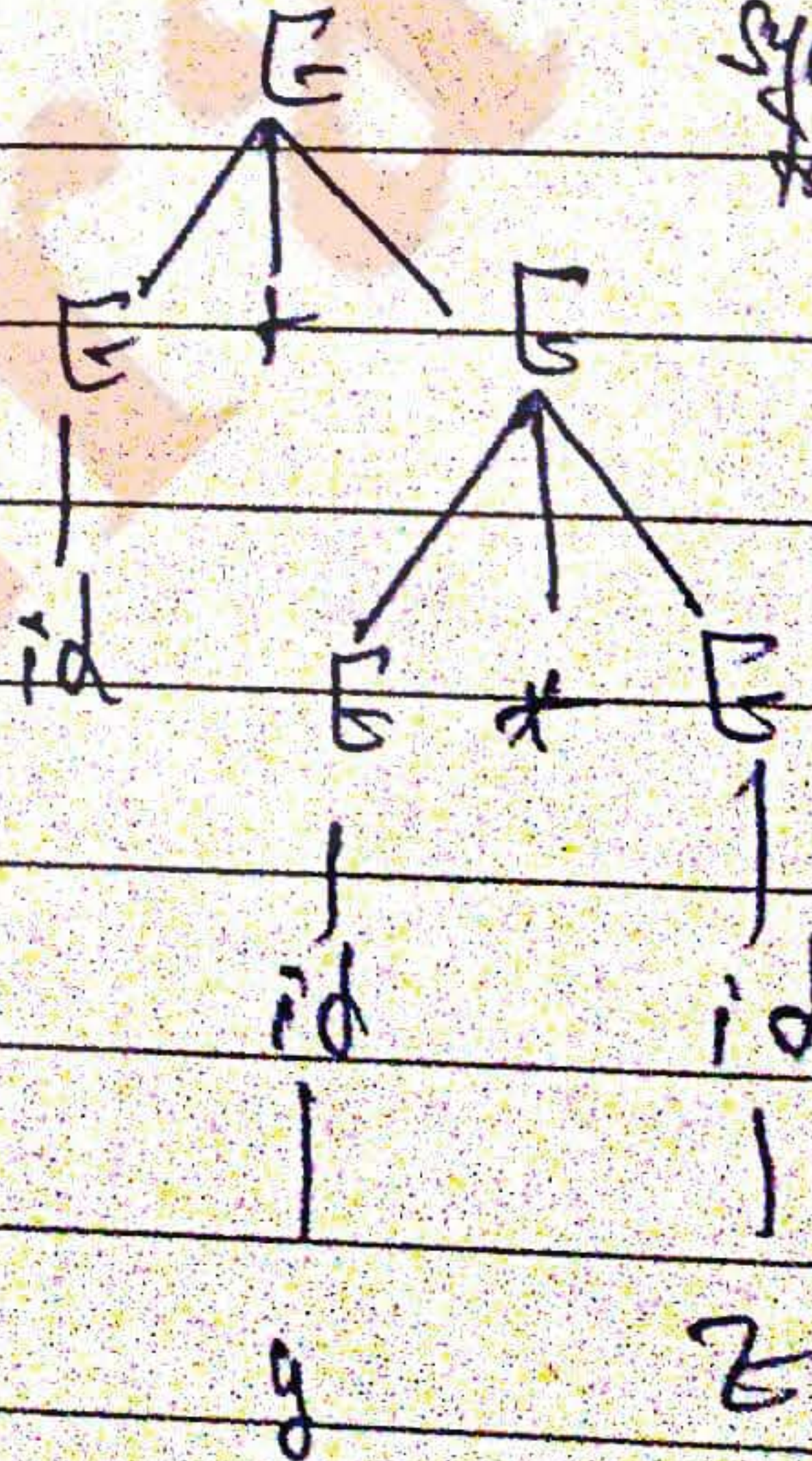
$a + b$: $ab+$
 $b * c$: $bc*$
 $a + b * c$: $a.b.c*+$



Parse & syntax tree

$E \rightarrow E + E$
 $E \rightarrow E * E$
 $E \rightarrow id$

Parse tree or concrete syntax tree



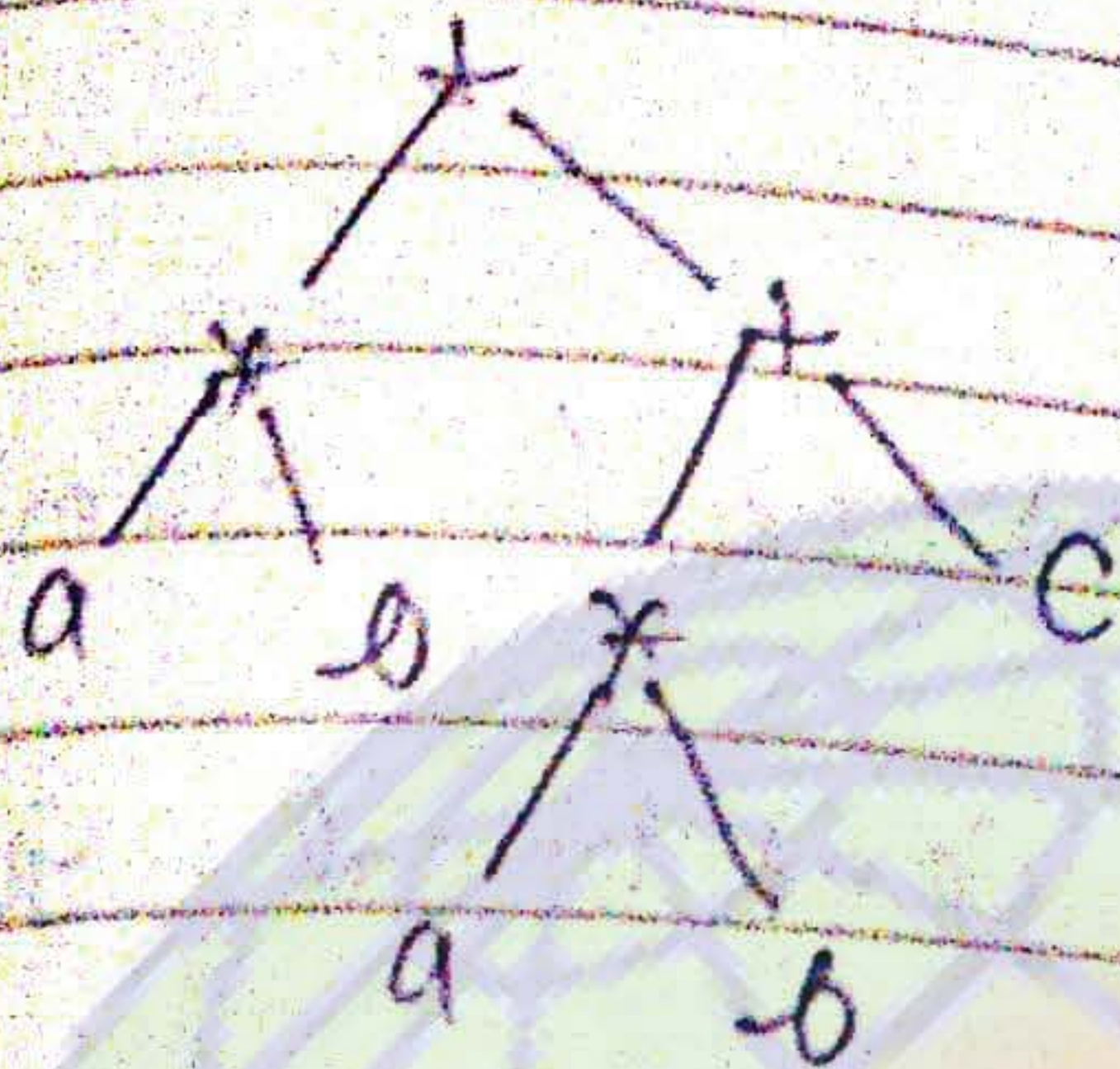
②

LAGS & DAG

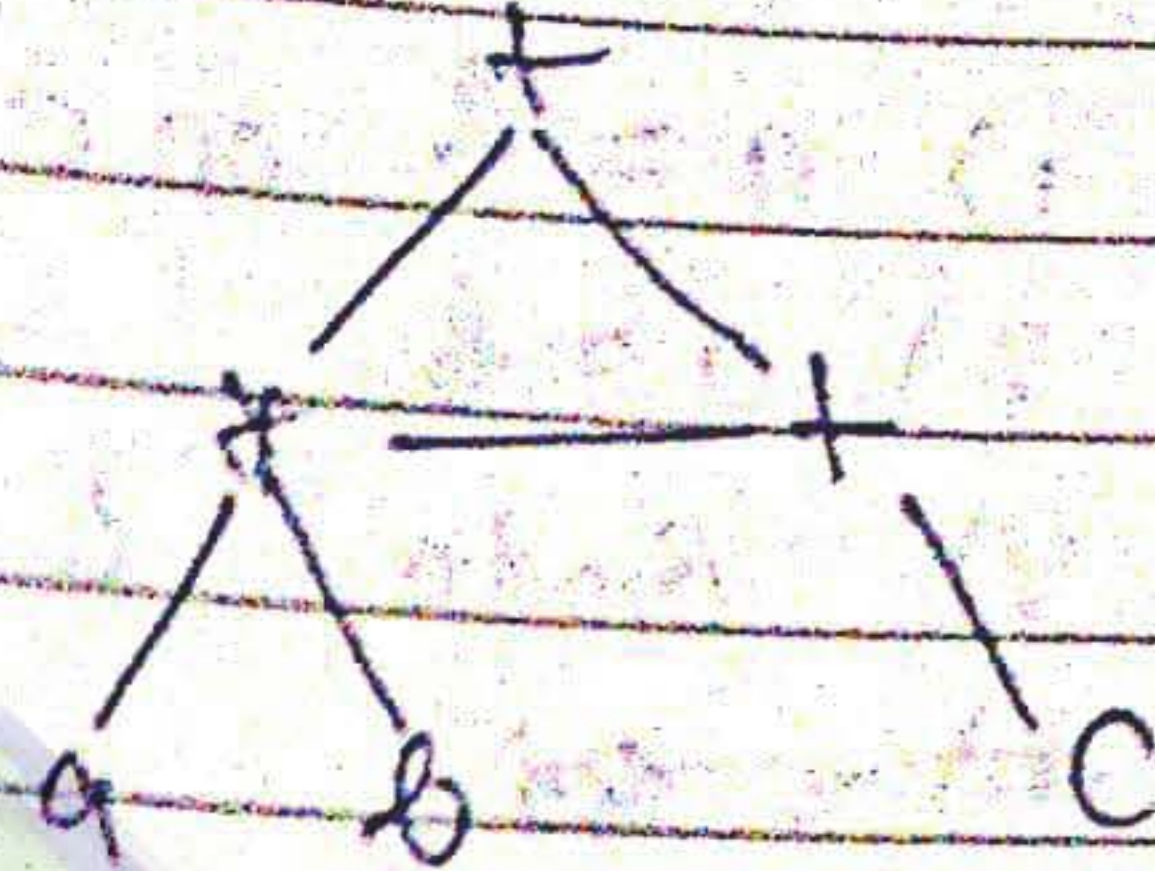
ASS

$a * b + a * b + c$

ASSAD: \downarrow

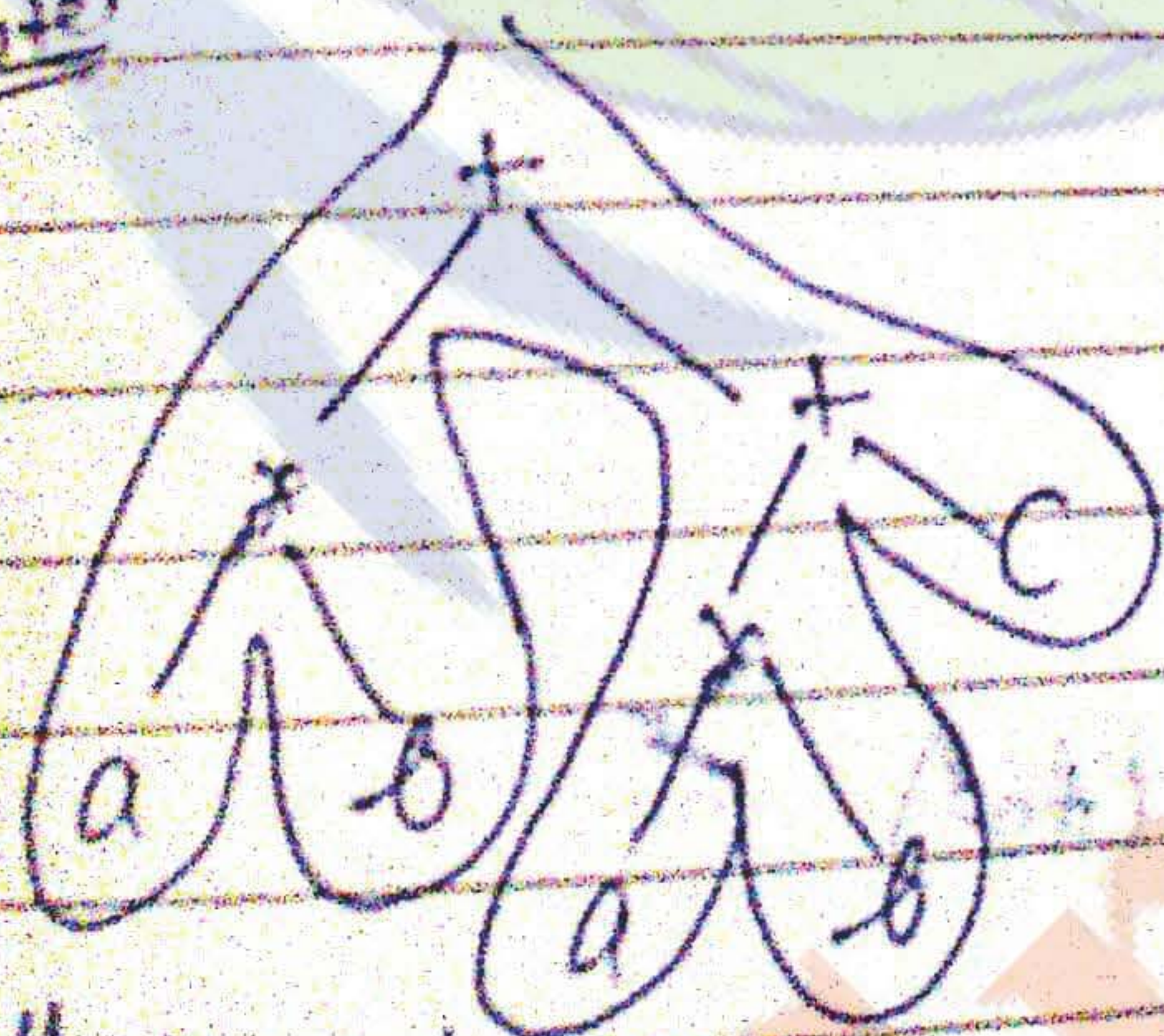


DAG: \downarrow



In DAG if a node is already created, instead of creating the same node again, we will make use of already created node.

Note:



3-address code

In three-address code in any statement, maximum three temporary variable or three memory reference will be used. and at least one operator can be used other than assignment operator.

$$a = b \text{ or } c$$

Some valid three address code statements

- 1) $a = b \text{ or } c$
- 2) $a = b$
- 3) $\text{Goto } L$ — Unconditional jump
- 4) $\text{if } \dots \text{Goto } L$ — Conditional jump
- 5) $a[i] = b$
- 6) $b = a[i]$
- 7) $a = *b$

Q) write the three address code for the following statements.

$$x = a + b + c * d \quad \text{where } x, a \text{ are real; } b, c, d \text{ are integer}$$

$$t_1 = c * d$$

$$t_2 = a + b$$

~~$$x = t_1 + t_2$$~~

$$t_2 = b + t_1$$

$$t_2 = \text{int to real}(t_2)$$

$$x = a + t_2$$

Q) $\text{if } (a > b)$

$$a = a + 1$$

else

$$b = b + 1$$

- 1) ~~If (a > b) goto 2~~
- 2) ~~a = a + 1~~
- 3) ~~If (b > a) goto 4~~
- 4) ~~b = b + 1~~

```

If a > b goto L1
    b = b + 1
    goto L2
L1: a = a + 1
L2: —
    
```

Backpatching: - leaving the ~~for~~ labels and filling them after is called backpatching.

a) for (i=0, i ≤ n, i++)

at run

- 1) a = 0
- 2) ~~is if~~ if i ≤ n
- 3) i = i + 1
- 4) goto 2

reache

a) for (i=0, i ≤ n, i++)

{
a = a + 1


```

i = 0
L1: if (i > n) goto L2
    a = a + 1
    i = i + 1
    goto L1
L2:
    
```

Implementation of three-address code:-

$-(a+b) * (c+d) + a + b * c$

manual representation:-

```

t1 = a + b
t2 = -t1
t3 = c + d
t4 = t2 * t3
t5 = t1 + t3
t6 = t4 + t5
    
```

NBQ, in computer, there are three types of representation.

Temporary register	Quadruple			Result	Triple		Entered into
	Op	Arg1	Arg2		Op	Arg1 Arg2	
1	+	a	b	(t1) 1) +	a	b	(i) 1)
2	-	t1		t2 2) -	(1)		(ii) 2)
3	+	c	d	t3 3) +	c	d	(iii) 3)
4	*	t2	t3	t4 4) *	(2)	(3)	(iv) 4)
5	+	t1	c	t5 5) +	(1)	c	(v) 5)
6	+	t4	t5	t6 6) +	(4)	(5)	(vi) 6)

Diff: more memory
 Adv: statements can be more around.
 (means parallel in any order)

Diff: statements can't be more around
 Adv: less memory

Diff: two times memory access
 Adv: statements can be moves around.

Code Optimization

It is process of reducing the no. of instruction without affecting the outcome of the source code.

It is of two types:

1) machine dependent code optimization -

It depends on characteristics of the target machine for the addressing modes uses.

This can be achieved by, allocating sufficient no. of resources.

2) machine independent code optimization -

It is based on characteristics of the programming language. This can be achieved by analysing the code completely and finding alternative source code equivalent of the

of trip

- 1)
- 2)
- 3)
- 4)

Techniques

1) Common sub expression elimination
 It is a technique in which working re-calculation of an same expression

```

i = a * i
n = a[t]
t1 = a * i
t2 = a * i
t3 = a[t]
a[t3] = t4
t5 = a * i
a[t5] = n
    
```

```

i = a * i
a = a[t]
t1 = a * i
t2 = a[t]
a[t] = t4
a[t1] = n
    
```

2) Dead code elimination:-

A code is called dead code if it never gets executed

i = 0

if (i < 7)

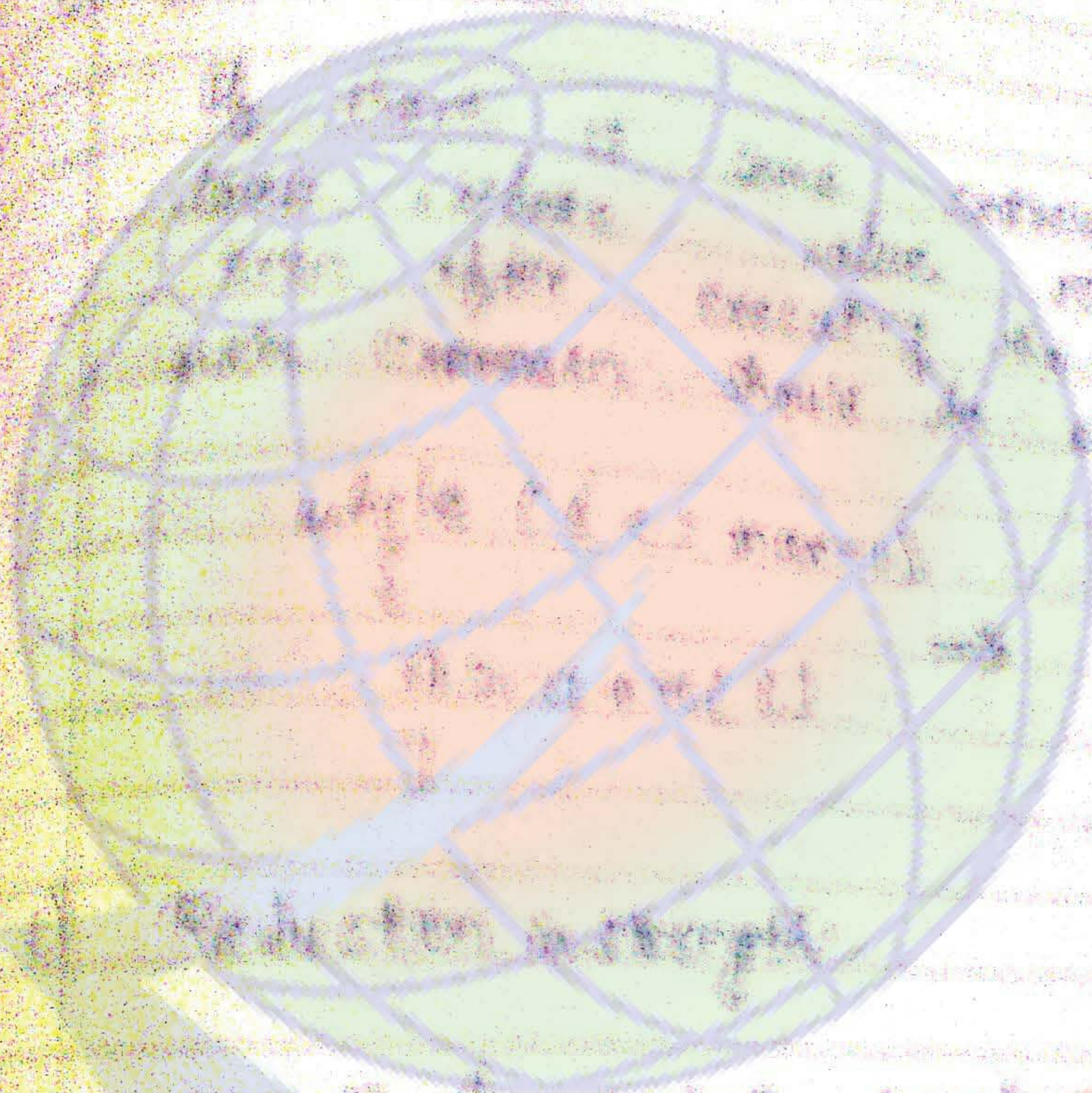
{
 =
 =
 }

this is dead code

Here if statement is dead code which never satisfied

3) Constant folding:-

It is a technique in which constants expressions are calculated



GradeSetter

during compilation time.

```
a = 3  
b = 2 + a;  
c = 3 * b + d
```

⇒

```
a = 3  
b = 5  
c = 15 + d
```

4) code motion:

If there is some expression inside the loop, whose value remains unchanged, even after executing the loop several times, such expression should be placed before the loop.

```
while (i <= max - 1)  
{  
  a = a + x[i]  
}
```

⇒

```
n = max - 1  
while (i <= n)  
{  
  a = a + x[i]  
}
```

5) Reduction in strength:-

strength of certain operator is more than the other operator

~~to do~~

eg. strength of * is more than +

```
for (i = 1; i <= n; i++)  
{  
  a = a + i * 5;  
}
```

⇒

```
a = 0;  
for (i = 1; i <= n; i++)  
{  
  a = a + 5;  
}
```

er

which

6) Loop Invariant

Avoiding the evaluation of computation inside the loop.

```

for (i=0; i < n; i++)
{
    k = i + a/b
}
    
```

$n = a/b$
 $k = i + a/b$

7) Loop fusion

merge several loops into one loop.

```

for (i=1; i <= 10; i++)
{
    for (j=1; j <= 10; j++)
    {
        print("HC");
    }
}
    
```

$i = 1, i <= 100, i++$
 $print("HC");$

8) Loop Unrolling

No. of jumps and tests will be reduced by writing the code this time.

```

while (i <= 100)
{
    a[i] = b[i]
    i++
}
    
```

$while (i <= 100)$
 $\{$
 $a[i] = b[i]$
 $i++$
 $a[i] = b[i]$
 $i++$
 $\}$