

DSA

* steps for program development & execution

- 1. > edit ✓
- 2. > compile ✓
- 3. > linking ✓
- 4. > loading ✓
- 5. > execution ✓

Edit:

```

first: c ✓
int div (int a, int b) ✓
{ ✓
  int c; ✓
  c = a/b; ✓
  return (c); ✓
}

```

```

main() ✓
{ ✓
  int x = 10, y = 5, z; ✓
  z = div(x, y); ✓
  printf ("%d", z); ✓
}

```

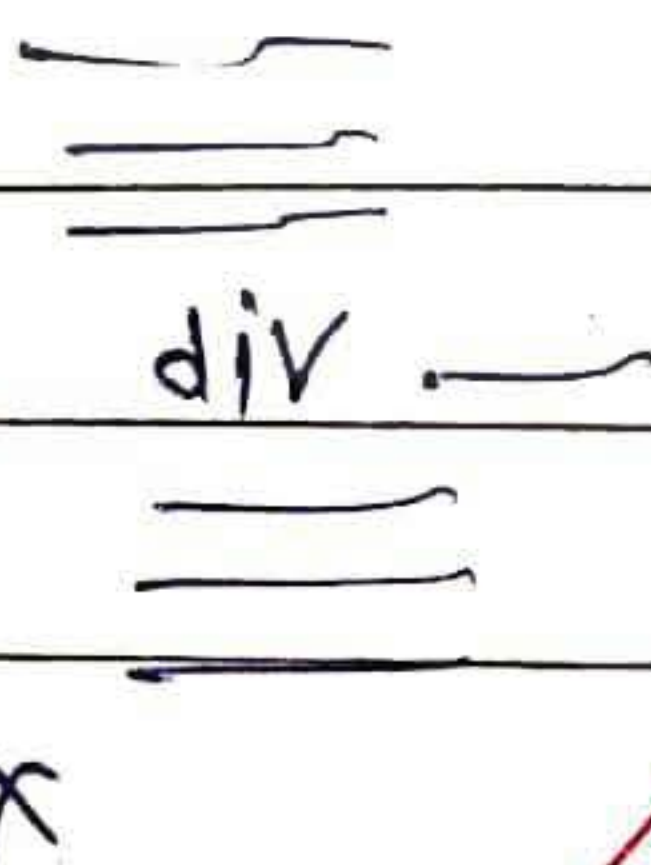
IDE → Integrated development environment [Turbo C]

↓ compile

Compile converts HLL → LL

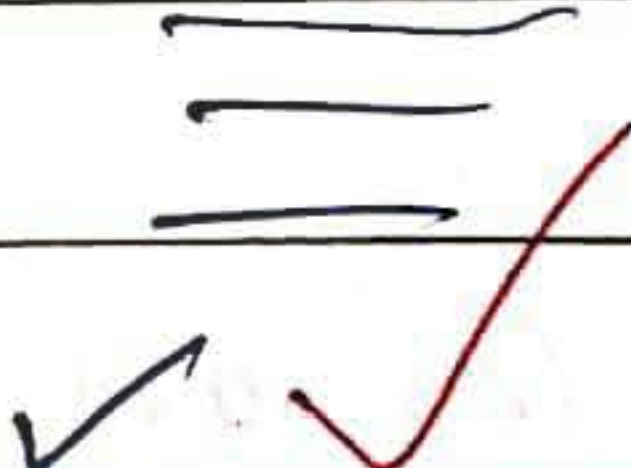
Comp:

first: obj ✓
 first: exe ✓
 main



div ✓
 main ✓

uses defined function



* Compiler vs Interpreter

• Compiler translates program once ✓

• fast ✓

• Program runs independently ✓

for eg.

• .exe file ✓

• Interpreter every time is translated whenever is executes:

• slow ✓

• Interpreter runs with

• first.js → Browser ✓

• first.jsp → web browser ✓

** C is a compiled language ✓

Java is slower than compiled language

Linking:

Linking of a library ✓

stdio.lib ✓

[Having machine code] ✓

include <stdio.h> ✓

[Having prototype] ✓

File: obj ✓

first.exe ✓

dir ✓

≡

main ✓

* (1) static library ✓

(2) statically linked library ✓

<3> dynamically linked library ✓

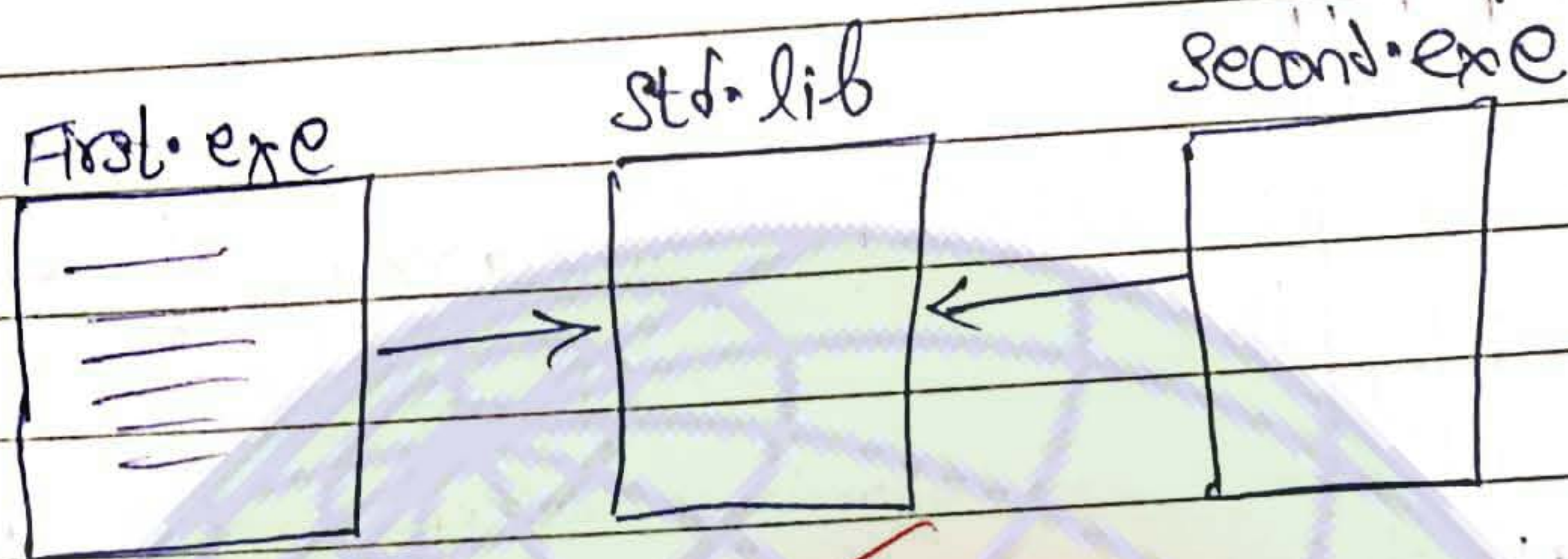
(1) static ✓

- Everything from the library ✓

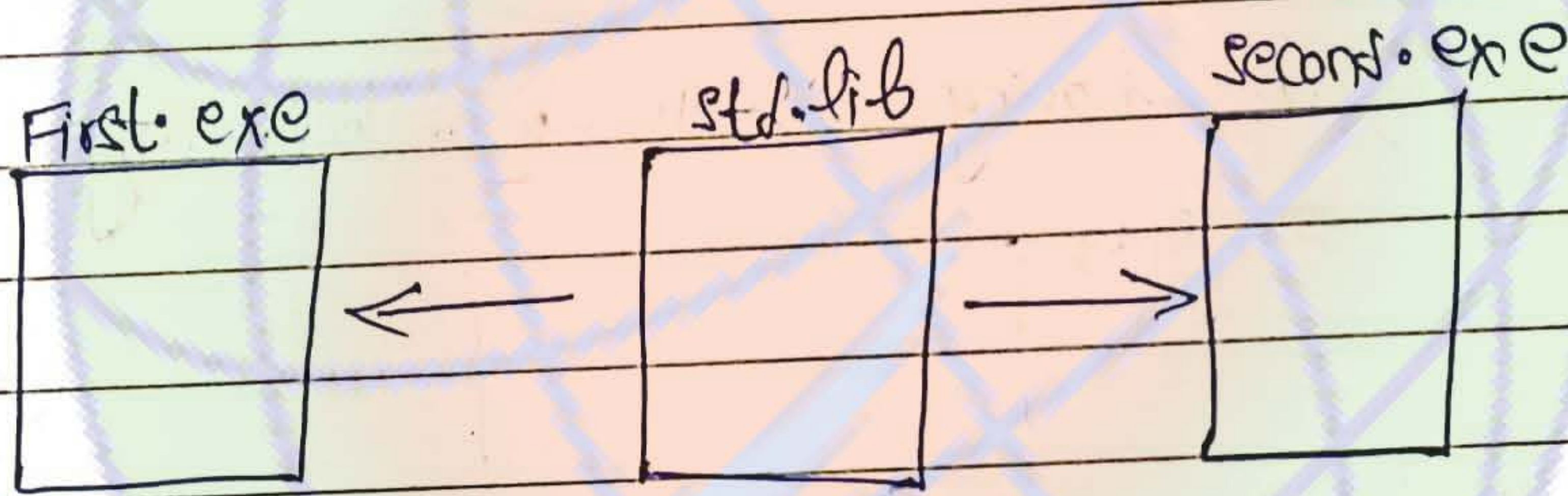
- Program can run independently. ✓

Linked library

- There is no copy of the library
- But the program is dependent on the library



linked library



Static library

statically

dynamically

- edit } library is attached to the program before execution
- compile }
- linking }
- loading }

- Execution i.e. Run time
- DLL [Dynamically link library]

library is attached to the program during DLL

- Anything happening before execution

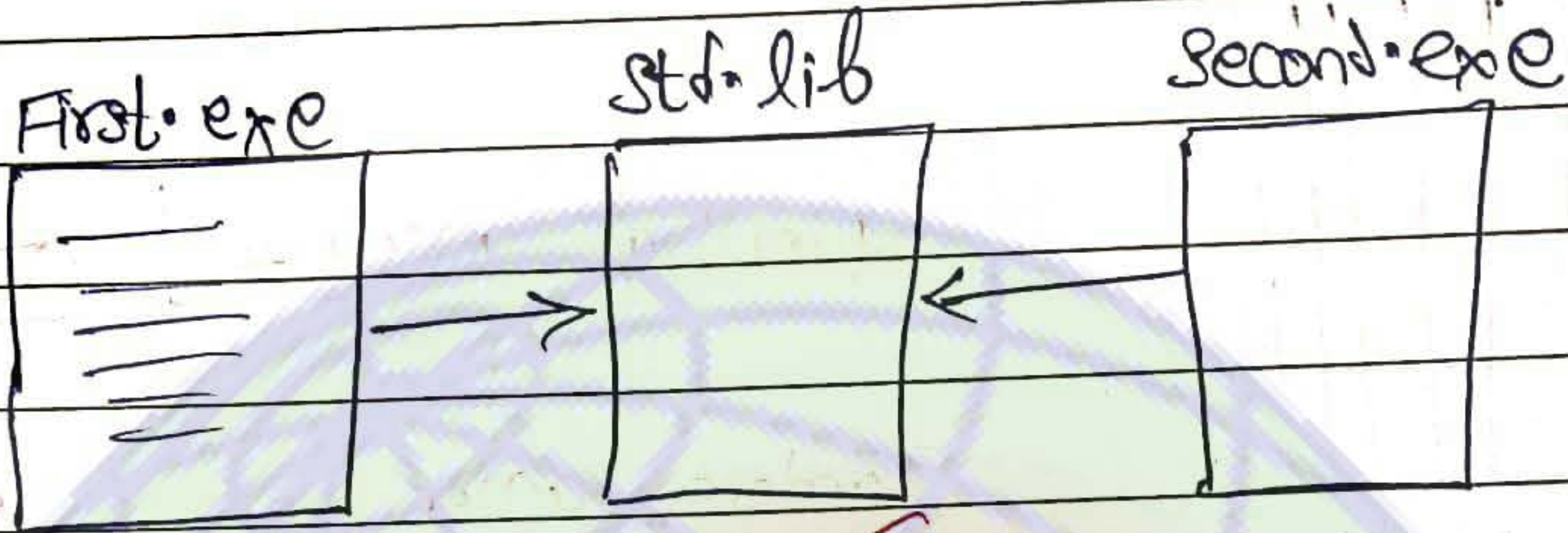
- with the help of this we can achieve multi-tasking.

- compiler design time for dll takes 2 bytes

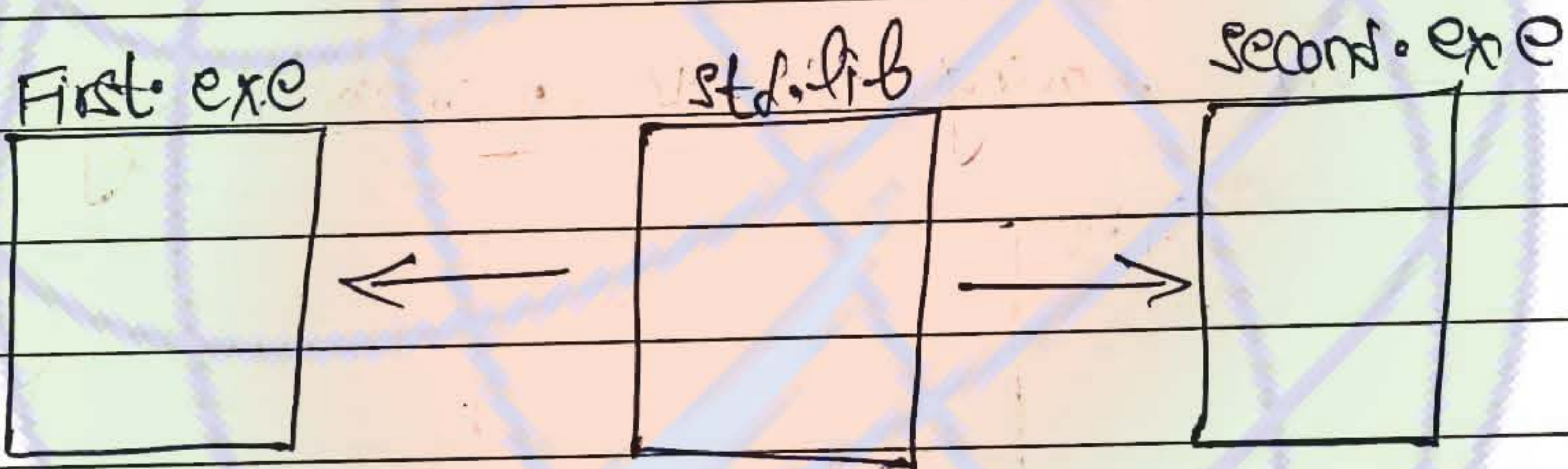
Loading: The memory is divided into smallest unit. i.e. byte called as cell & size is 1 byte.

Linked library

- There is no copy of the library
- But the program is dependent on the library



linked library



Static library

*

statically

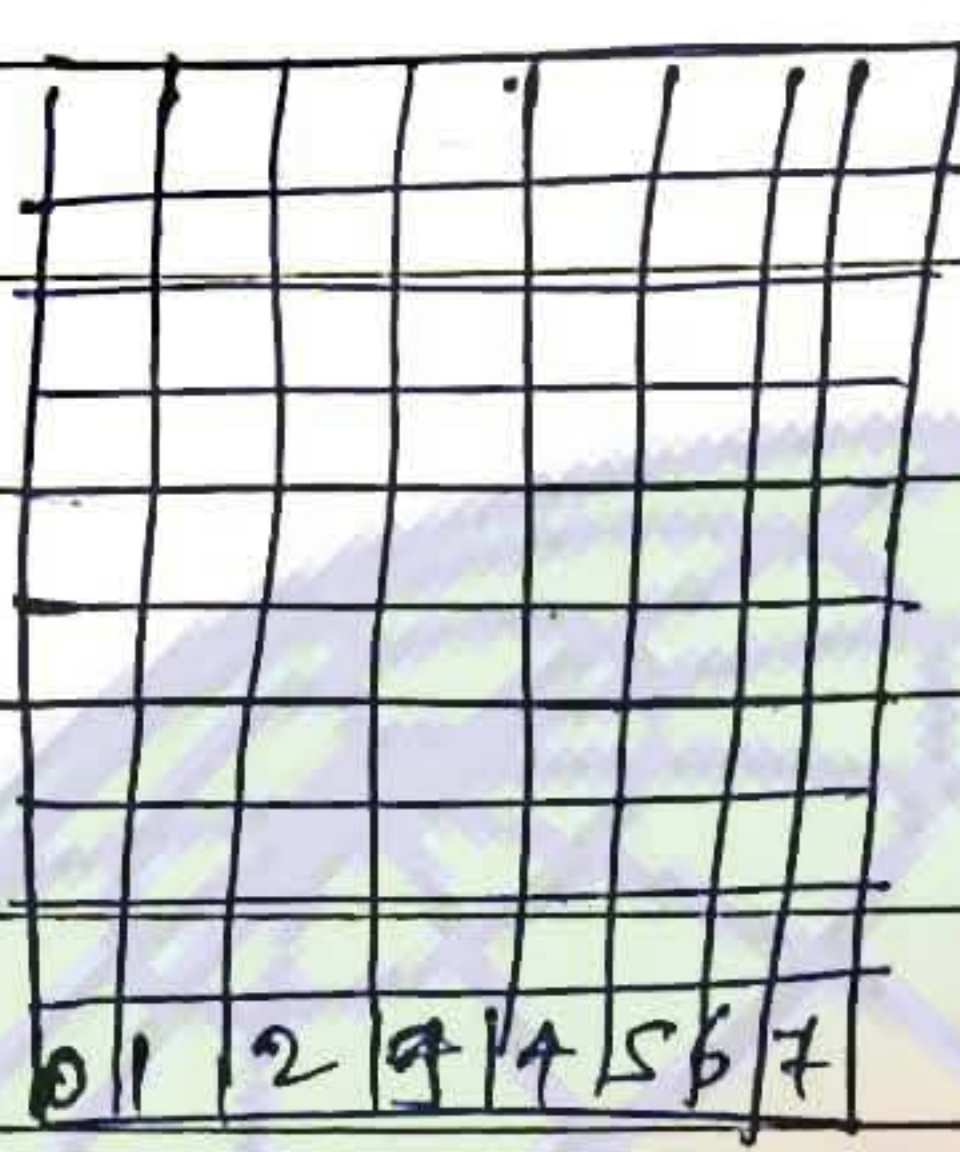
dynamically

- edit } library is attached
 compile } to the program
 linking } before execution
 loading }
- Anything happening before execution
- compiler design time [for int takes 2 bytes]

- Execution i.e. Run time
- DLL (Dynamically link library)
- library is attached to the program during DLL
- with the help of this we can achieve multi-tasking.

Loading: The memory is divided into smallest unit. i.e. byte called as cell & size of 1 byte.

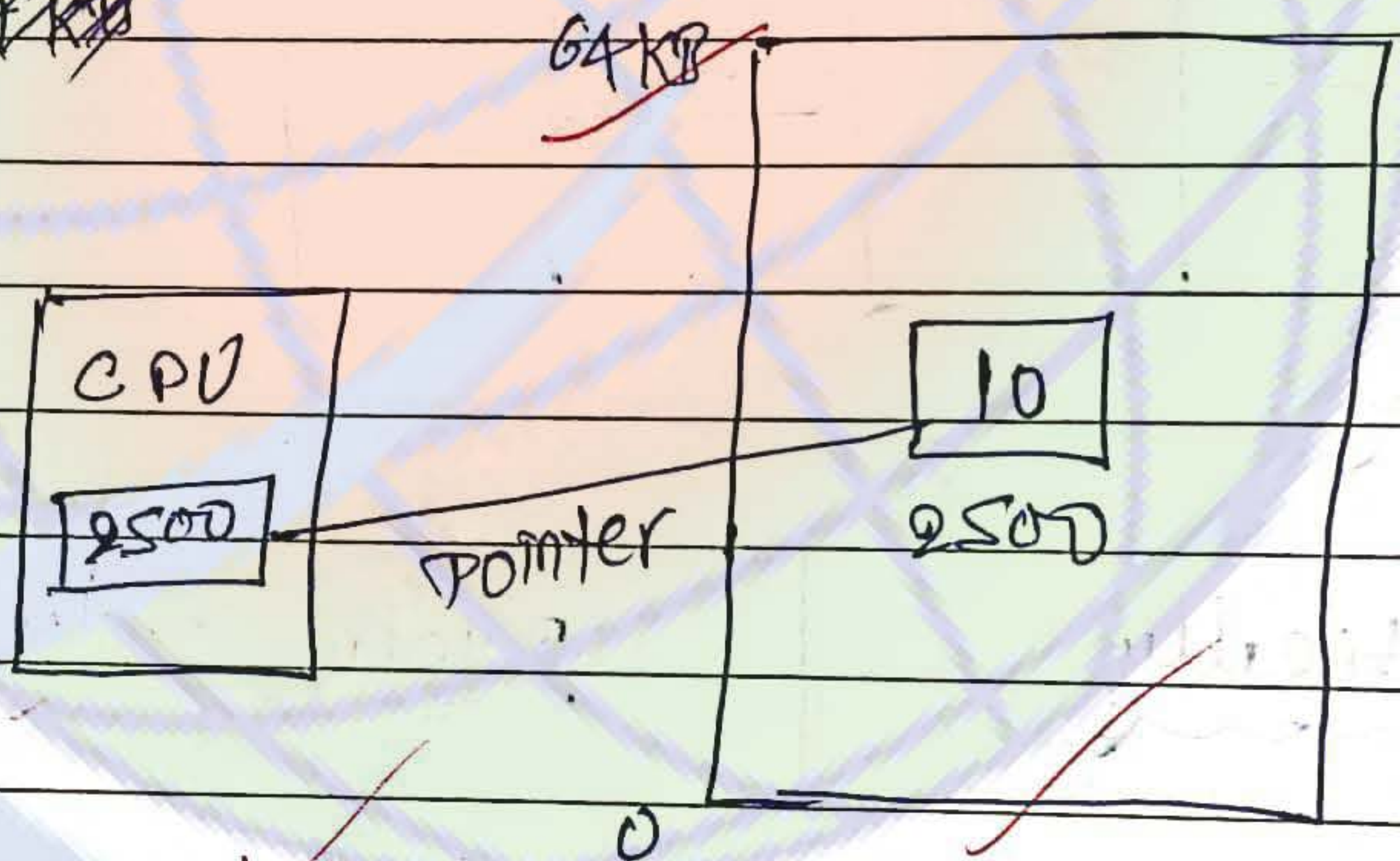
- Address are linear
- Every byte is having it's address
- Every byte is accessed with the help of it's address



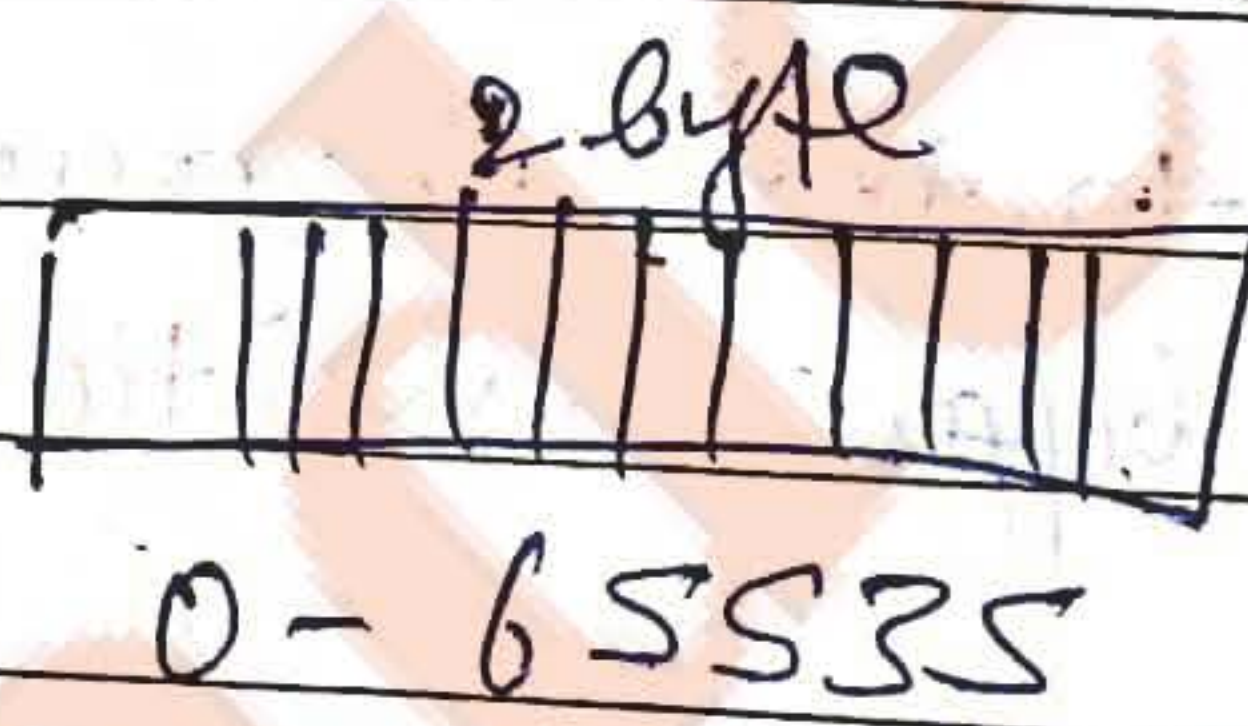
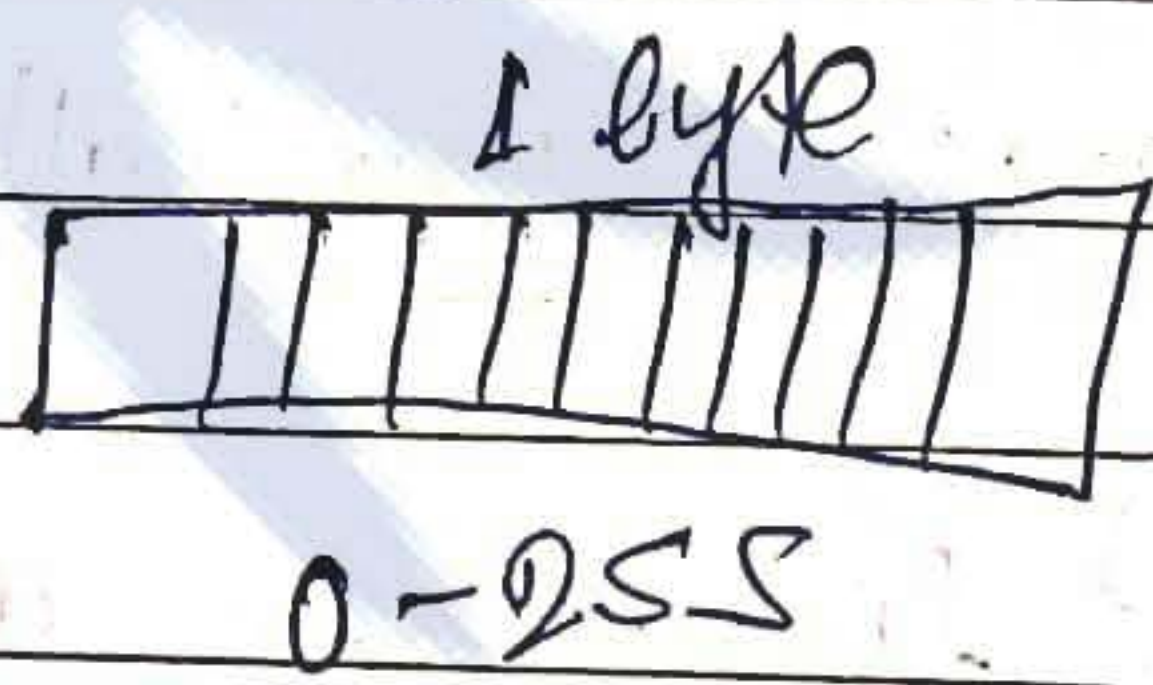
Sequential access →

Random access →

Earlier, 8085 up having 64KB memory, why ~~64KB~~

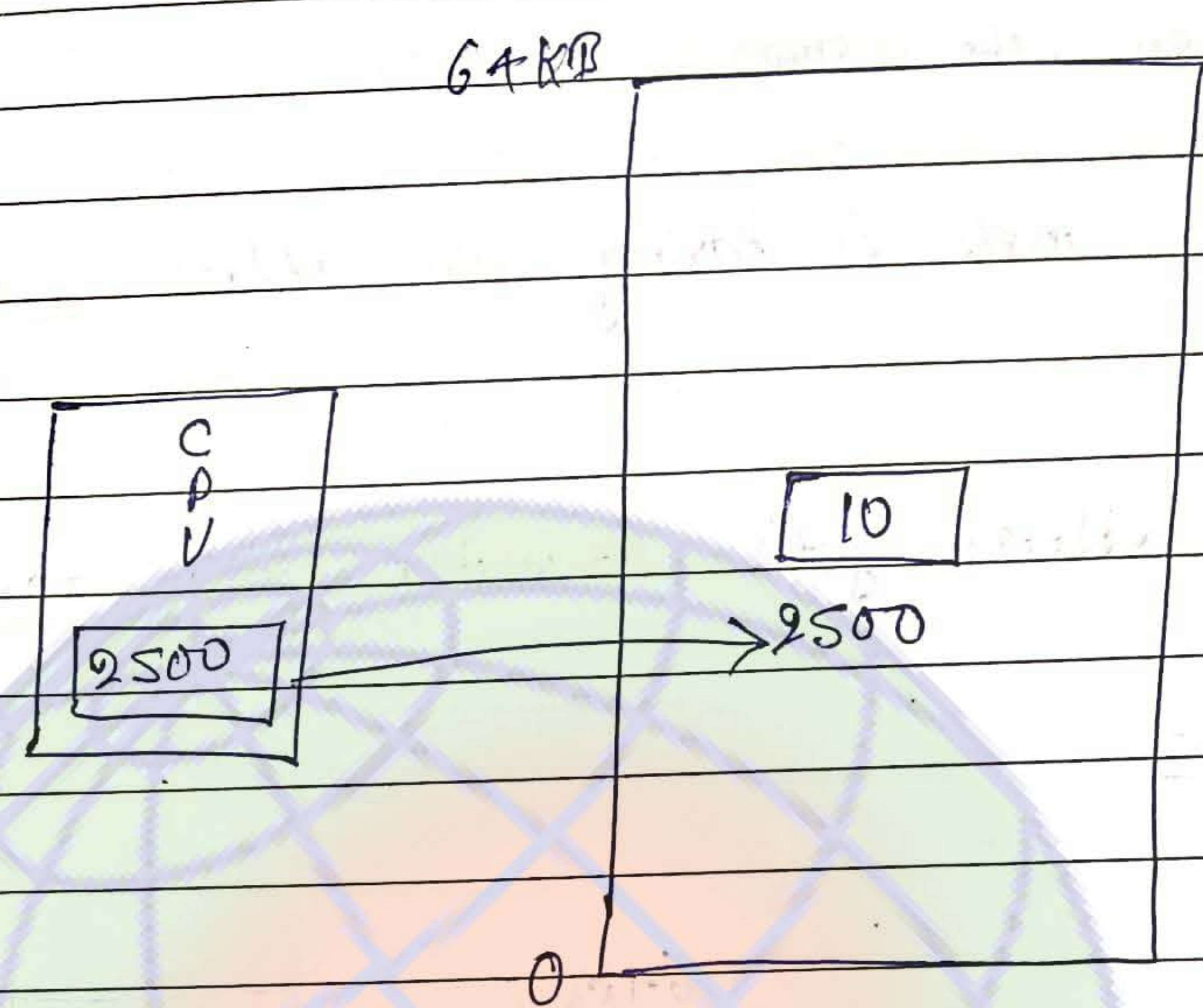


Memory
16
2

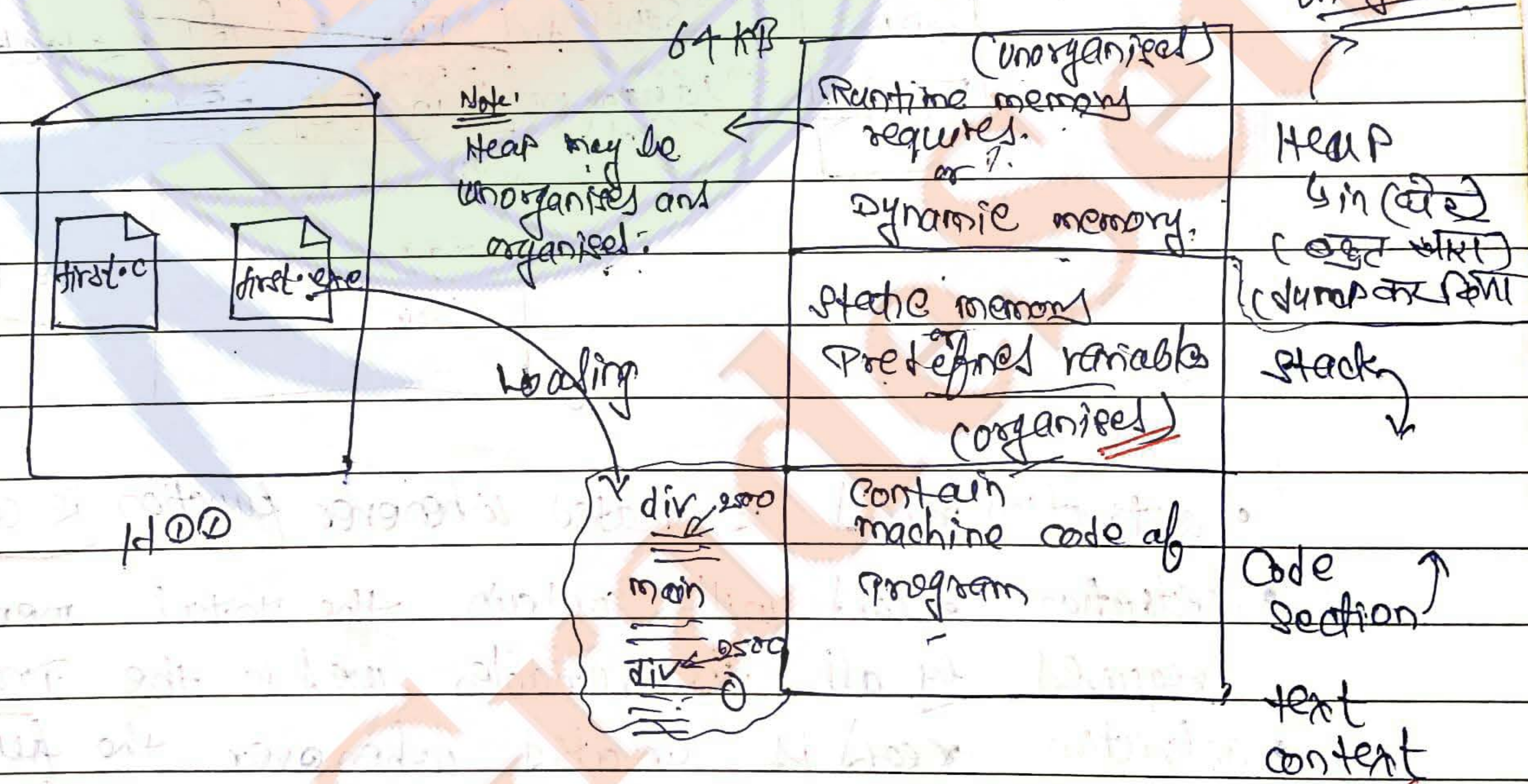


- To store the address of any location we need 2 Bytes. i.e. pointer of 2 Bytes from 0-64 kilobytes.
- when a program is loaded into main memory every instruction is having it's address.
- At the place of function call writing the address of function at the place of function call.

so, relocatable address areas then converted into absolute address



To store the address of any location, we require two bytes.
So, we require pointer of 2 bytes to indicate



So, main memory is divided into three major sections -

- (a) Code section ✓
- (b) Stack section ✓
- (c) Heap section ✓

(1) when the prog

(2) every inst is having the address in main memory.

* Relative address gets converted into absolute address.

Execution:-

```

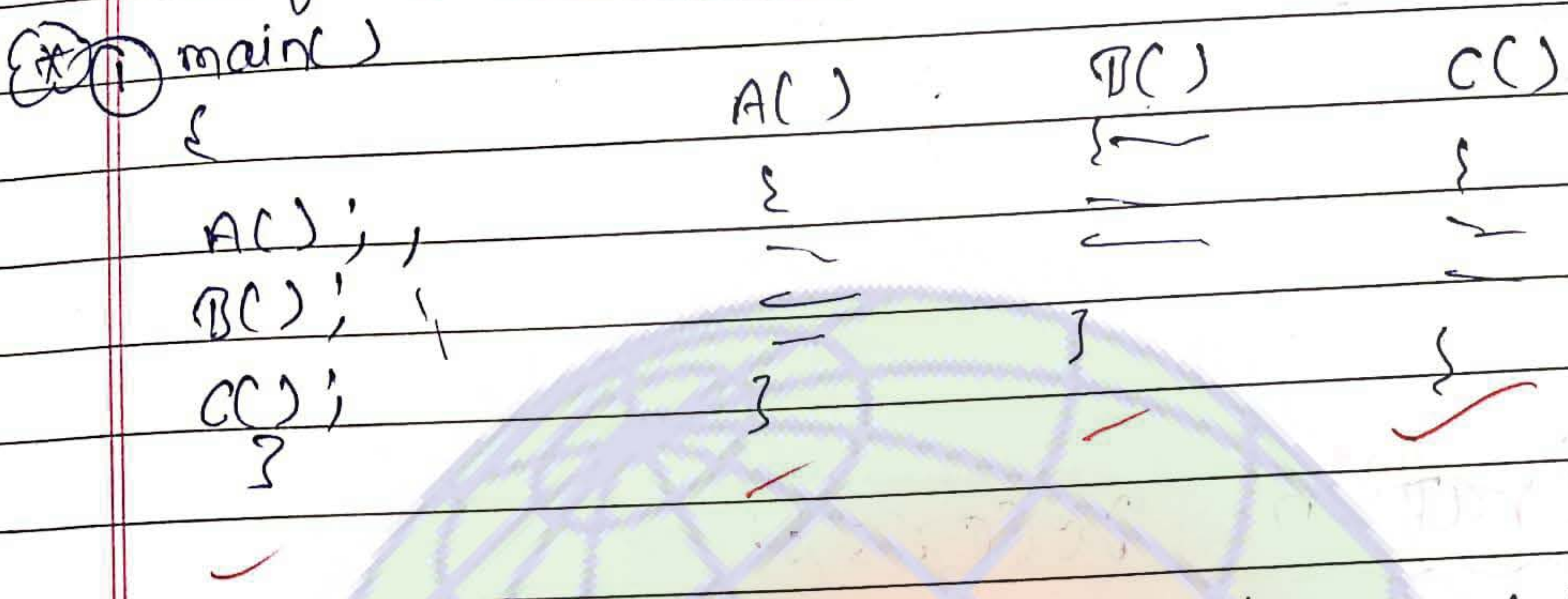
#include <

```

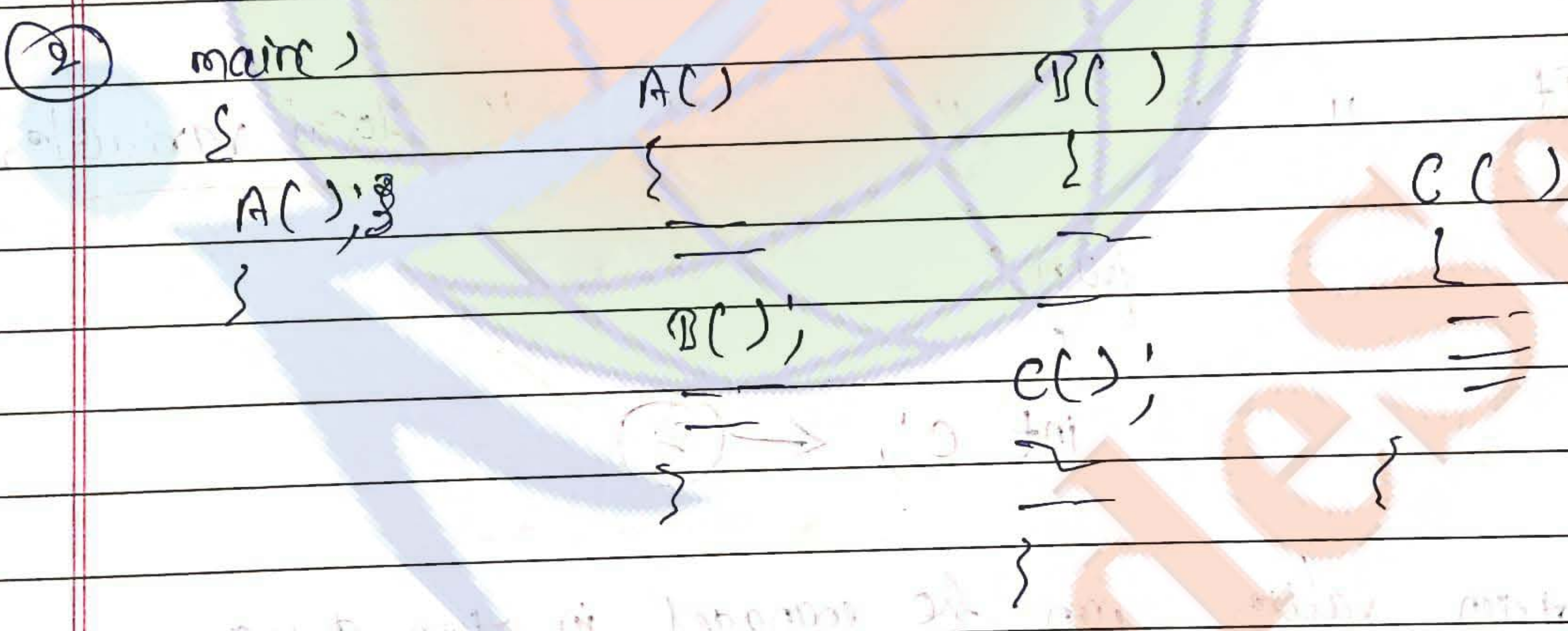
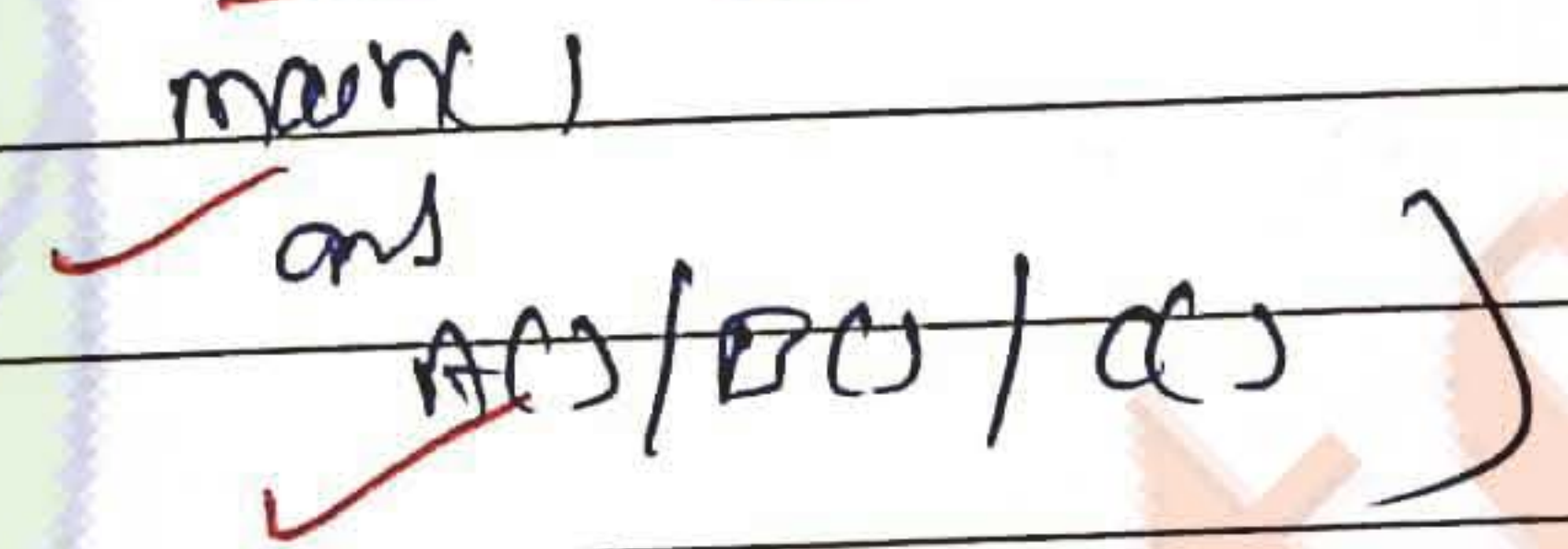


- activation record is created whenever function is called.
- Activation record will contain the total memory required by all the variables used in the program.
- activation record is created whenever the function is called.
- Activation record is deleted when the function terminate.
- Topmost activation records belongs to currently executing function.

- stack of activation records or stack frames.
- ~~one~~ one function can not access the activation record of another function.



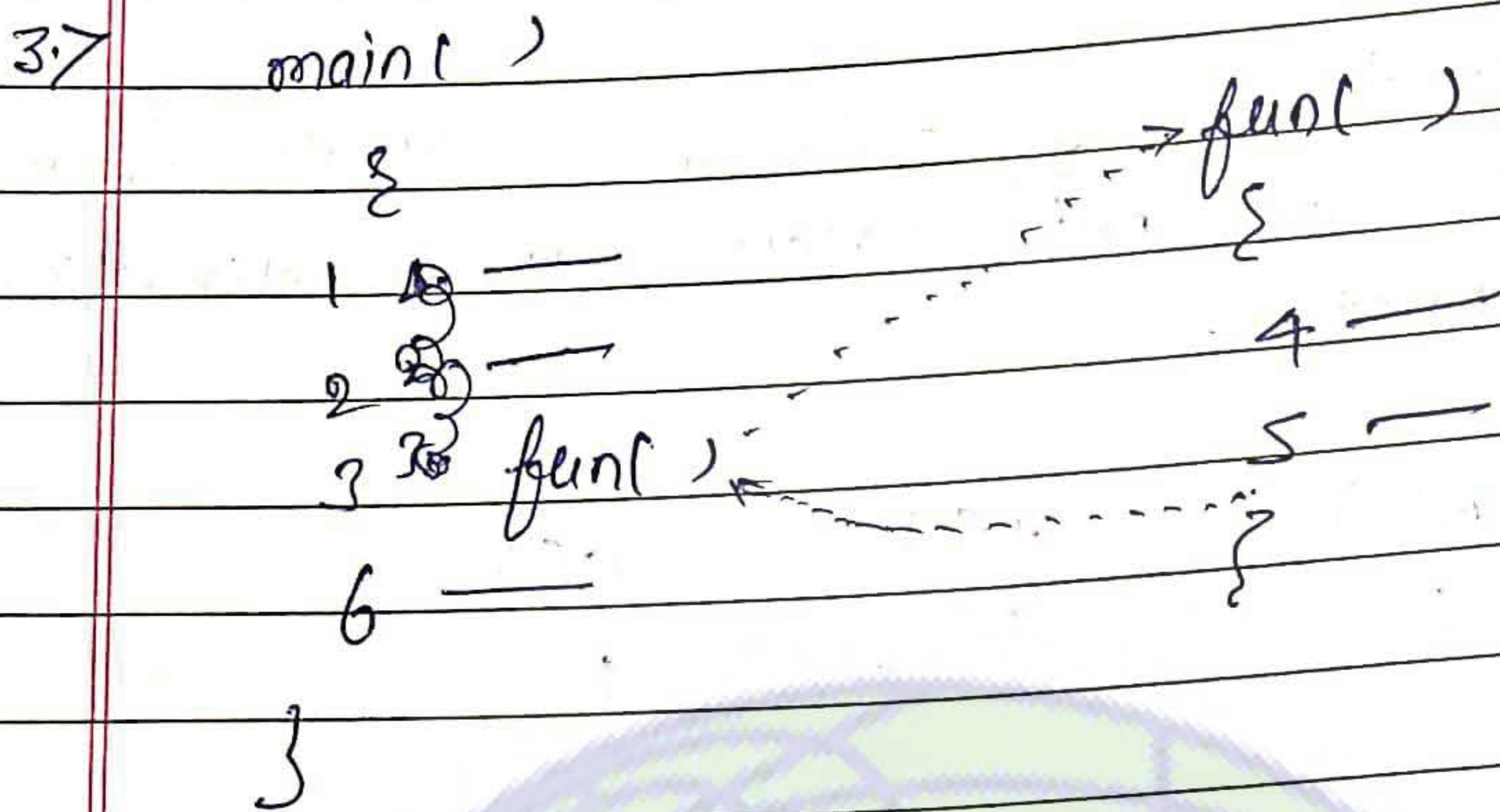
⇒ Total activation records created = 4
 ⇒ maximum activation record at a time = 2



⇒ Total Activ records created = 4 ✓
 maximum " " " at a time = 4 ✓

Note: maximum depends on maximum chain of calls or maximum depth of calls.

2 ✓



★ Activation records:

(1) It will contain the memory for parameter

```
fun (int a, int b) ← (1)
```

(2) It " " " " " local variables

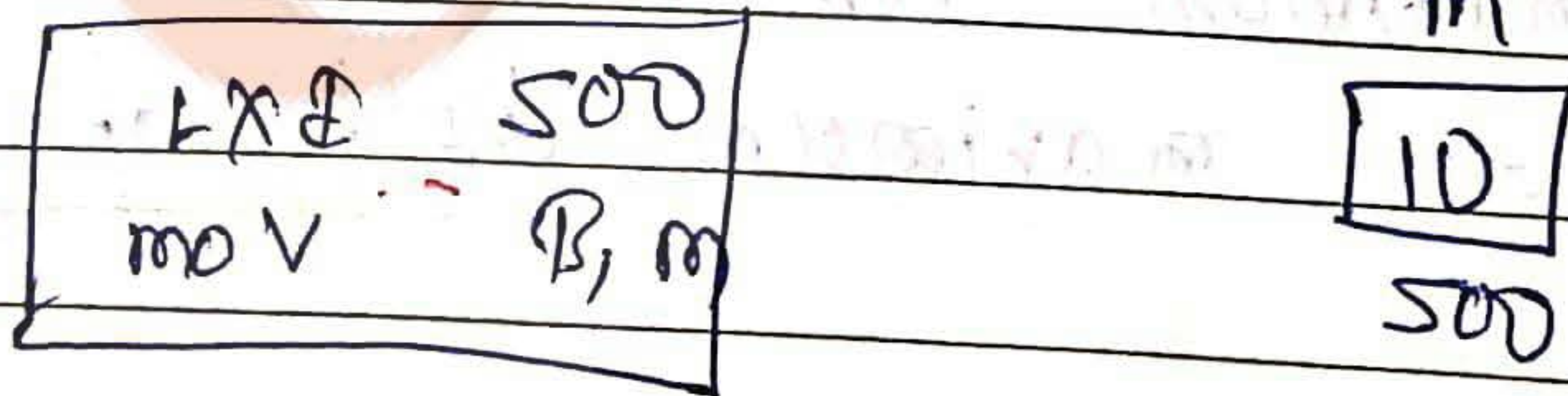
```
fun ( )  
{  
  int c; ← (2)
```

(3) constant values can be managed in two ways

(1) Immediate access

```
mov $10, %eax      mov $10, %eax
```

(2) Direct access



CS = 2 * a + 3 * b' + constant's

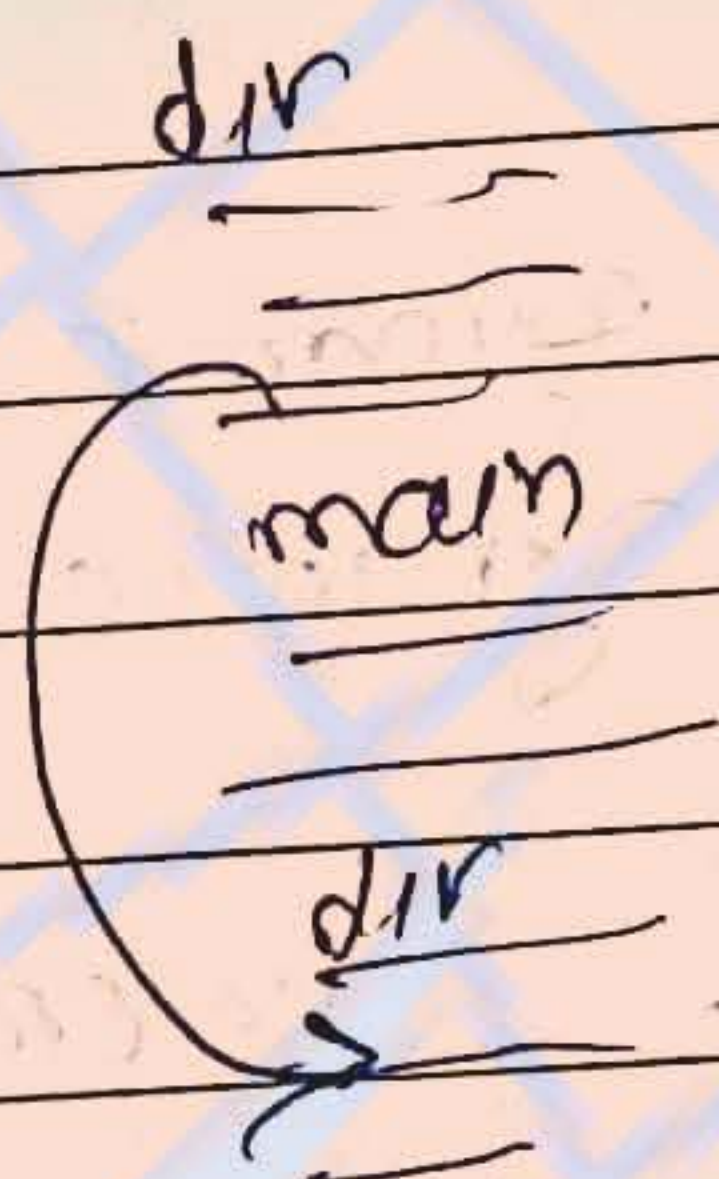
so, it will contain the memory for constants.

(4) it will contain the memory for result of expression

$$c = 2 * a + 3 * b;$$

↖ 4

Return address



Note!

```

    ①
    fun ( int a, int b )
    {
        ② int c;
        ④ c = 2 * a + 3 * b;
        ③ return(c);
    }
    
```

Activation record

- ① Parameter ✓
- ② local variables ✓
- ③ constants ✓
- ④ result of expression ✓
- ⑤ Return address ✓

Q.7 main ()

```

    {
        int x, y, z;
    }
    
```

← ~~dynamic~~
This is static variables ✓
but, the memory allocation is dynamic in nature ✓

Note! memory is not allocated at compile time.

★ Attributes of variable:-

- 1. Name
 - 2. Type/size
 - 3. value
 - 4. Address
 - 5. scope
 - 6. lifetime/ extent
- name ✓
 - int, float ✓
 → garbage value, initialize ✓
 → memory address ✓
 → main, dir → variable ✓
 → life time - how long it is alive ✓

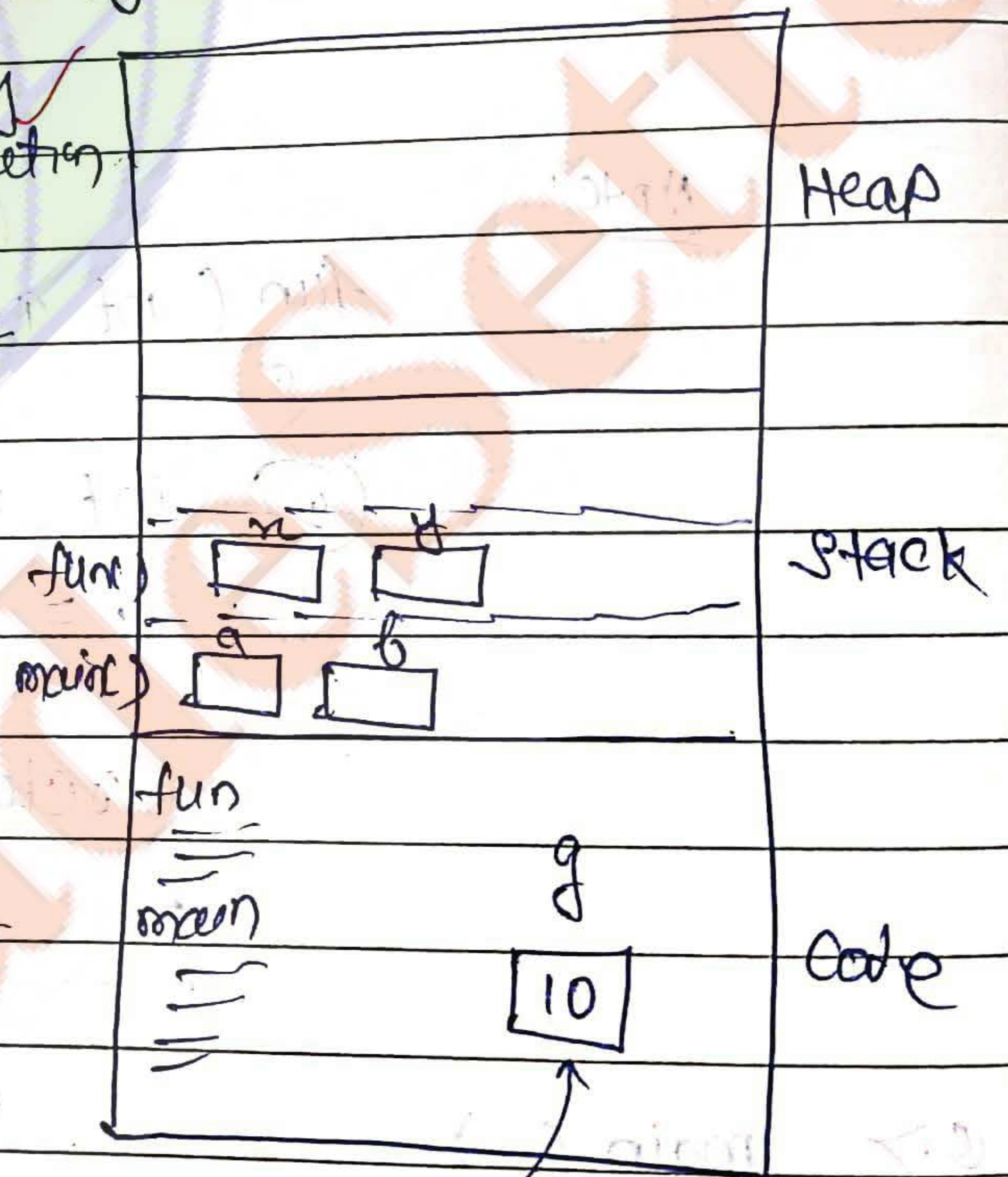
★ Methods of memory allocation:-

- 1. static
 - 2. stack dynamic
 - 3. Heap dynamic
- ← we studied in our previous page,

(1) Static method of memory allocation:-

```

global variable → int g = 10; ← static memory allocation
    fun()
    {
        int x, y;
        pf(g);
        g++;
    }
main()
{
    int a, b;
    g = g + 2;
    pf(g);
    fun();
    pf(g);
}
    
```



• memory is allocated at the loading time in the code section. This is static memory allocation.

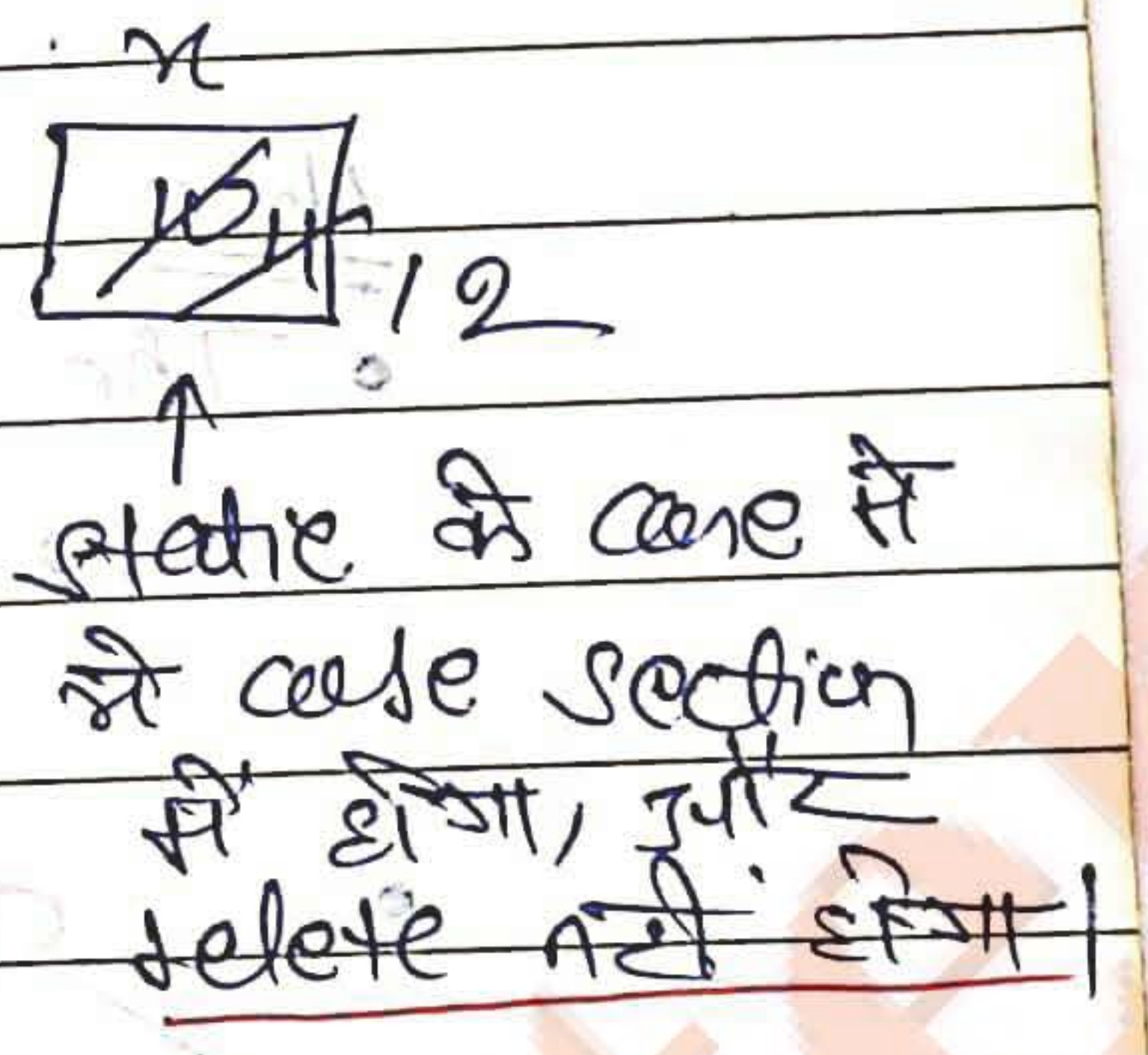
• 'C' language supports static method of memory allocation for
 (a) Global variables ✓
 (b) static variable. ✓

```

    fun()
    {
        static int x=10; ✓
        x++;
        pf(x); ✓
    }
    
```

```

    main()
    {
        fun(); — 11 ✓
        fun(); — 12 ✓
    }
    
```



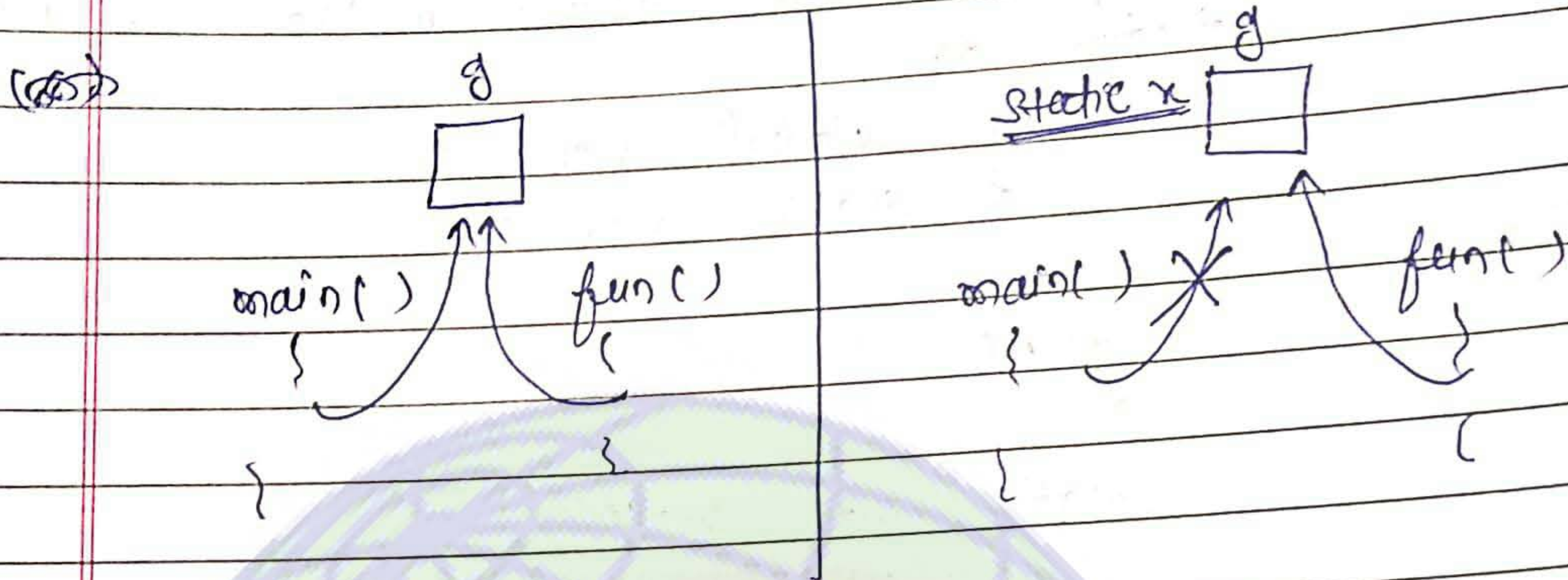
Note: (a) fun()

```

    int x=10; ✓
    x++; ✓
    pf(x); ✓
}
main() ✓
{
    fun(); — 11 ✓
    fun(); — 11 ✓
}
    
```

Global	static
some loading time • for all • accessible by all functions	code section • loading time • only for local ✓ • accessible by <u>only one function</u> .

Imp. \rightarrow वैश्व का कक्षा में क्या बात है? सबके में होगा

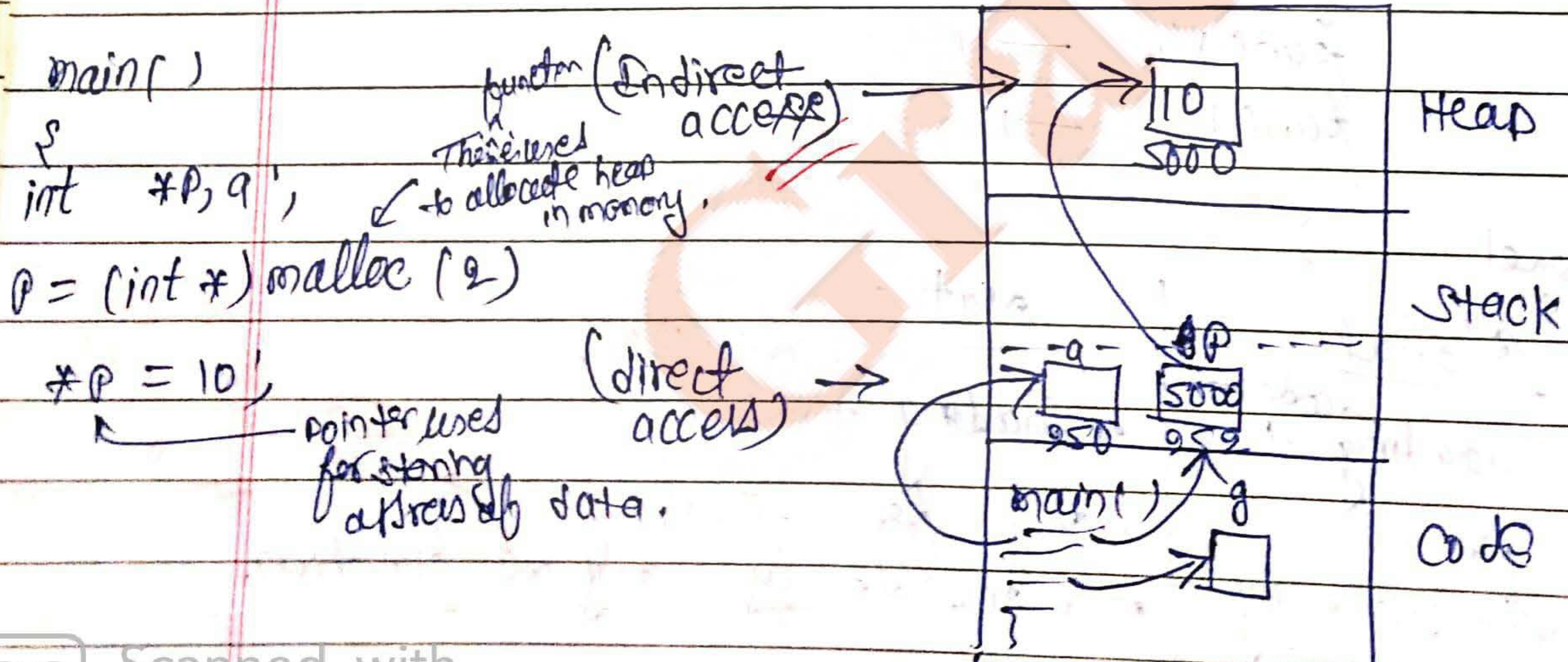


Note:

- The memory which are allocated in code section is automatically initialize to zero(0).
- Code section = initialize to zero ← बूकी
 Stack section = garbage value.

global and static variables of c are initialize to zero.//

(3) Heap method of memory allocation.

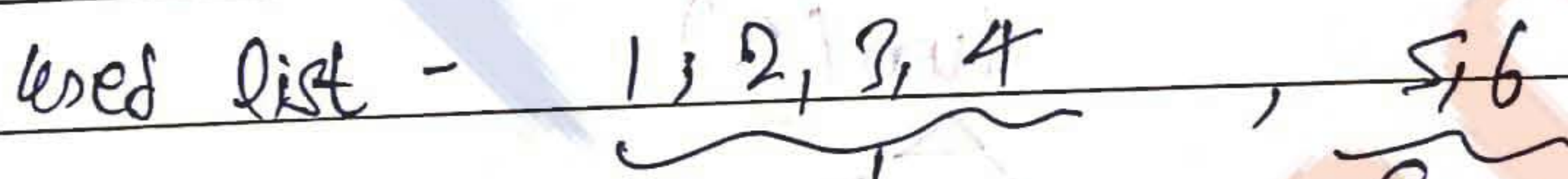
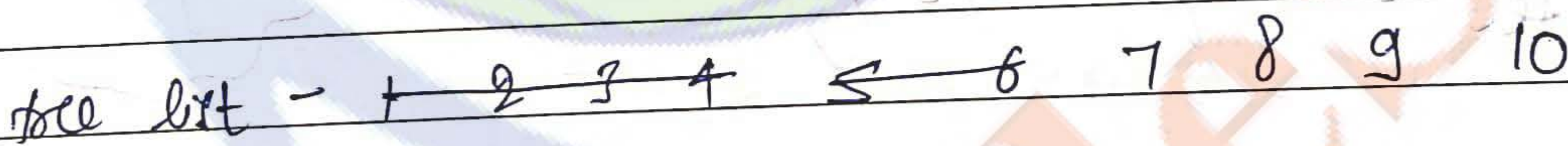


```
main ( )
{
    int *p, a;
    cout << "enter size";
    cin >> a;
    p = (int *) malloc (a);
    *p = 10;
```

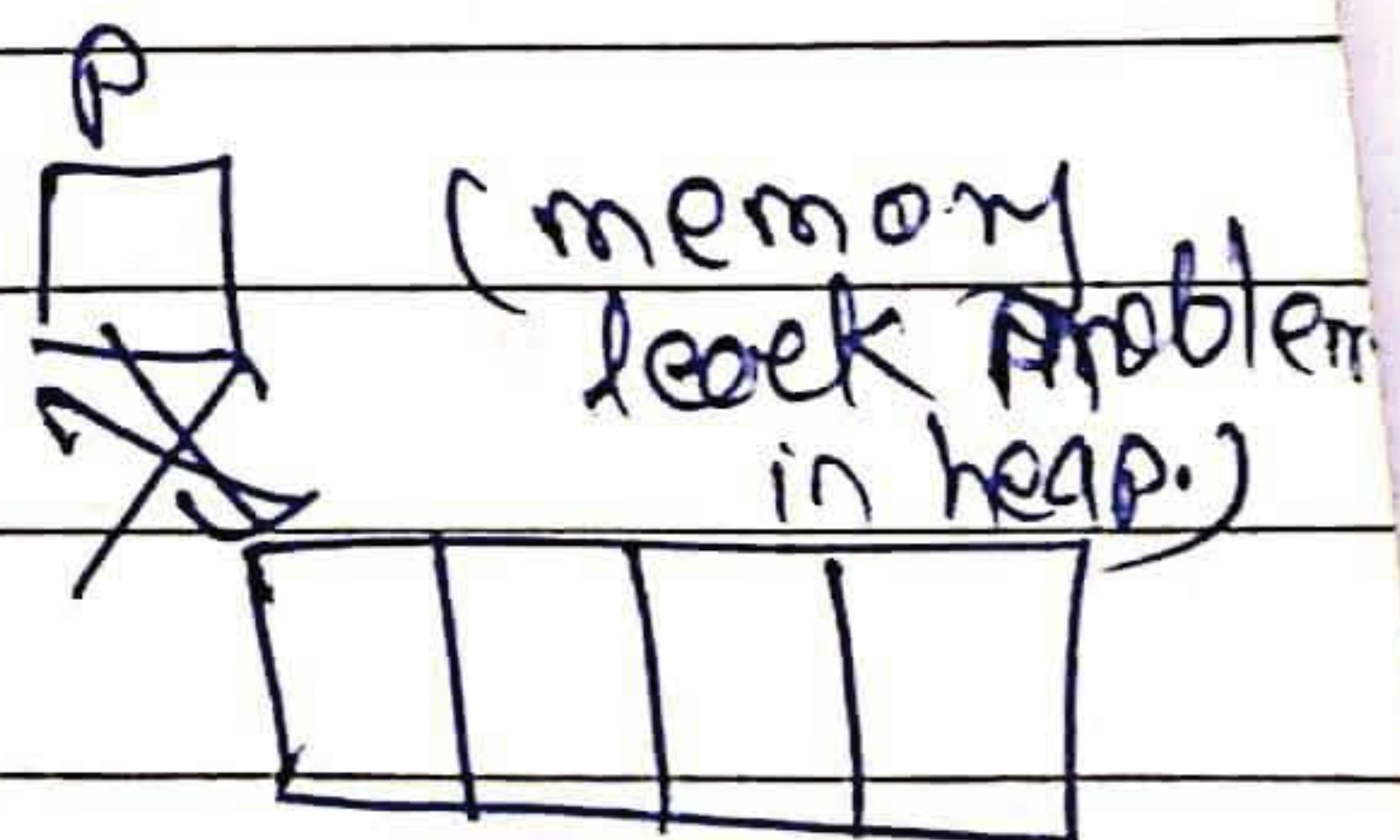
* Heap management

```
p = malloc (n);    ← to allocate
free (p);         ← to deallocate/release
```

Heap memory is managed by two list
 malloc ← when we allocate the memory ✓
 free ← when we free the memory. ✓



```
main
{
    p = malloc (4);
    q = malloc (2);
    free (p);
    p = NULL;
```



Note: Every program has its own code section, stack and heap.

RECURSION:-

90% question of C are either recursion or pointers.

Tail Recursion:

```
void fun (int n)
```

```
{
  if (n > 0)
  {
```

```
    printf ("%d", n);
```

```
    fun (n-1);
```

```
  }
```

```
}
```

```
main ()
```

```
{
```

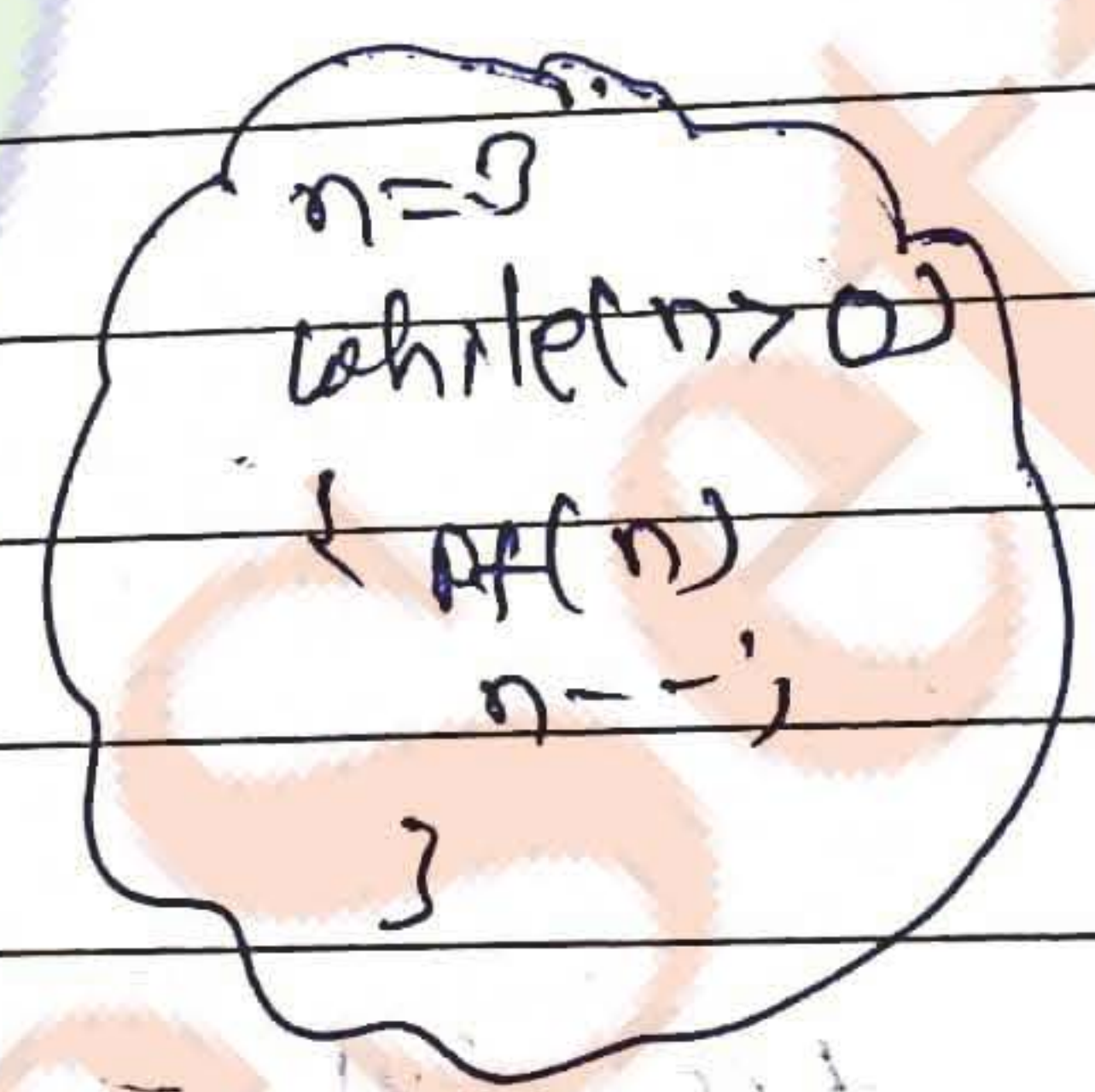
```
  int a = 3;
```

```
  fun (a);
```

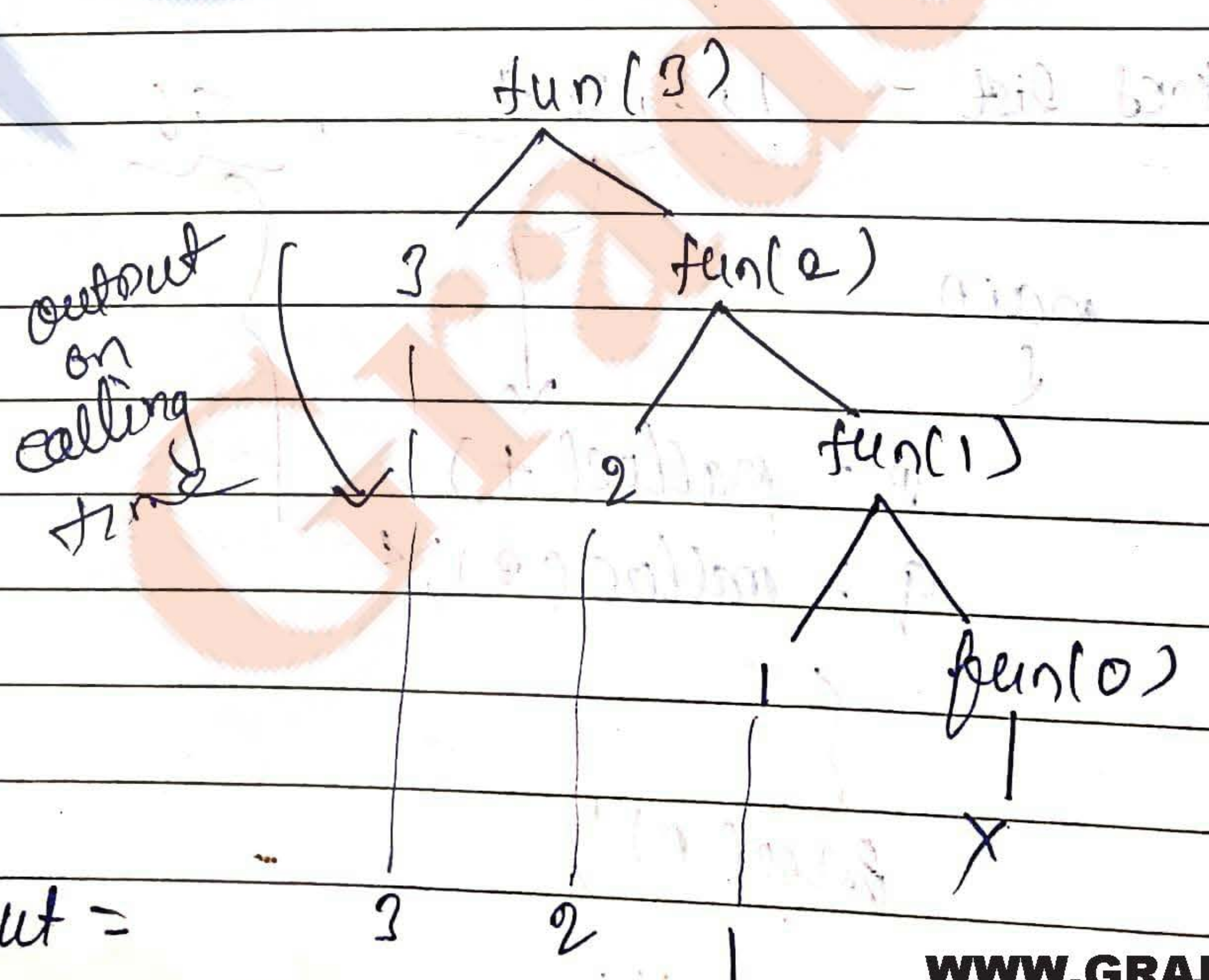
```
}
```

Base condition or termination condition.

tail of function calling



tail recursion can be easily converted to loop.



Output =

3 2 1

Note: For supporting recursion stack is introduced.

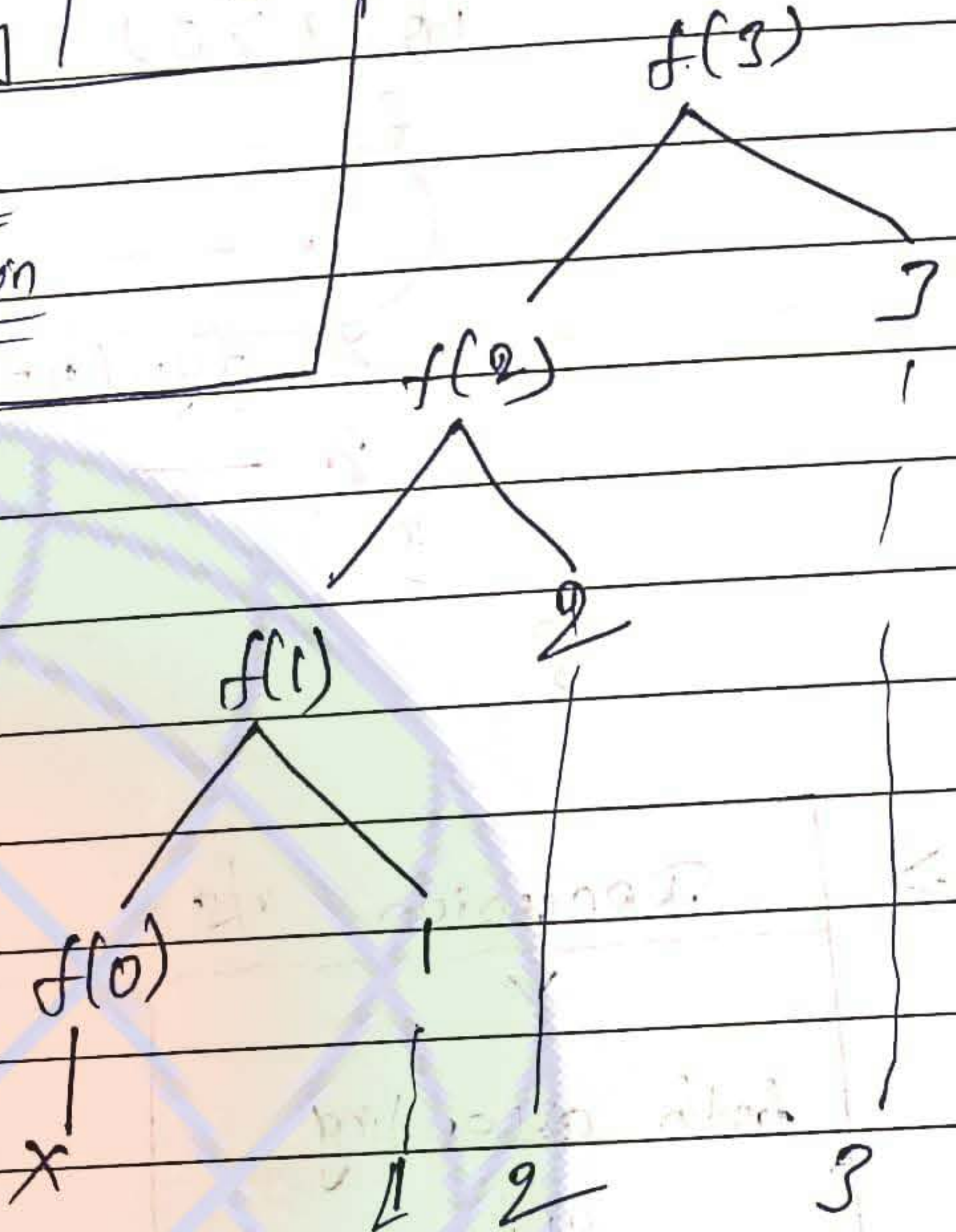
Head Recursion

```
1-> fun (int n)
```



```
n = 3
while (n > 0)
{
}
```

function calling
if (n > 0)
fun(n-1);
of(n);



```
main()
{
  int a = 3;
  fun(a);
}
```

O/p: -

using modified recursion concepts

"अगर बाई में प्रिंट होता है
returning time में प्रिंट होता है" उपरोक्त

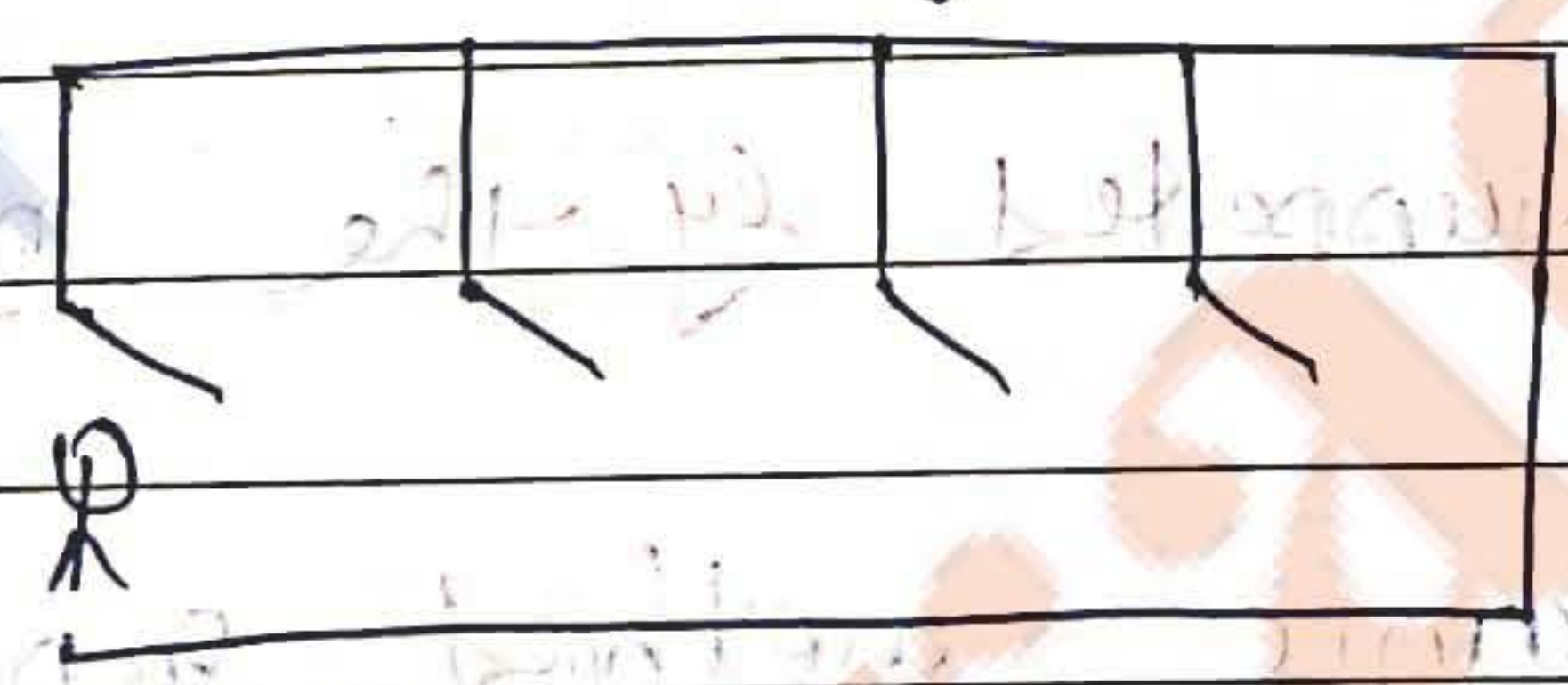
output on returning time

output = 1 2 3

होता है सब function

Note:

- Two phases in recursion
 - (1) calling time / increasing time / ascending
 - (2) Returning time / decreasing time / descending



- 1-> scotch on bulb
 - 2-> Goto next room
 - 1-> Goto next room
 - 2-> switch on bulb
- O/p -> 1, 2, 3, 4
- O/p -> 4, 3, 2, 1

2.7* fun (int n)

{

if (n > 0)

{

1. —

2. fun(n-1);

3. —

}

}

before recursive function

calling time ✓

otherwise returning time ✓

3.2	Recursion	vs	loop
	both ascending and descending		only ascending ✓

4.2 recursion and loop are both converted to each other and vice versa are also true

Recursion \rightleftharpoons loop

5.2 Recursion is supported by the mathematics

6.2 Stack dynamic method supports recursion.

7.2 In recursion always activation record in stack is created.

8.2 mostly in recursion, ~~to~~ head recursion is used, because it uses fully

* $n! = 1 * 2 * \dots * n$

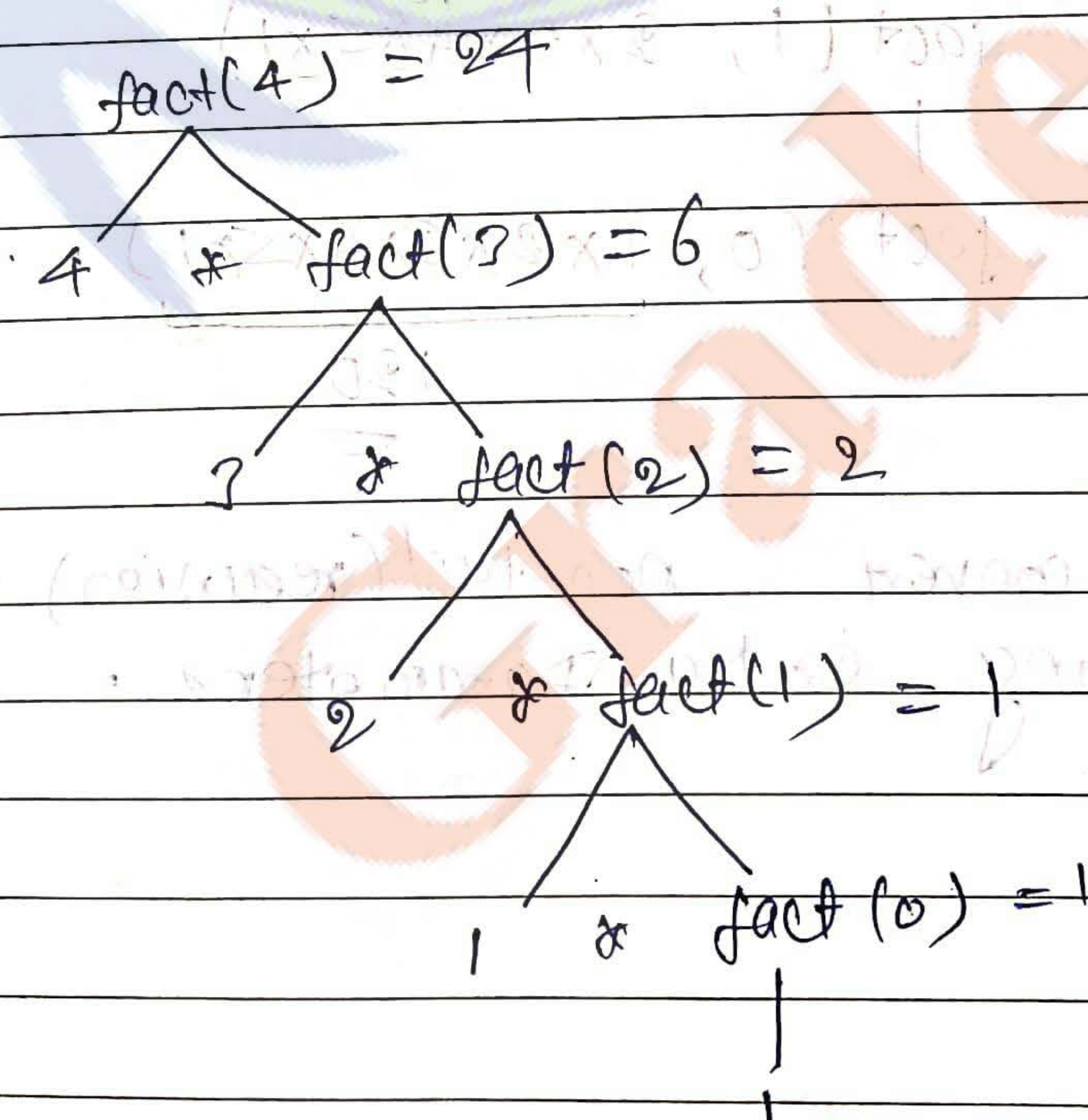
$n! = n * (n-1) * \dots * 2 * 1$

$n! = n * (n-1)!$

$$\text{fact}(n) = \begin{cases} 1 & n=0 \\ n * \text{fact}(n-1) & \text{if } n > 0 \end{cases}$$

```
int fact(int n)
{
    if (n == 0)
        return 1;
    else
        return n * fact(n-1);
}
```

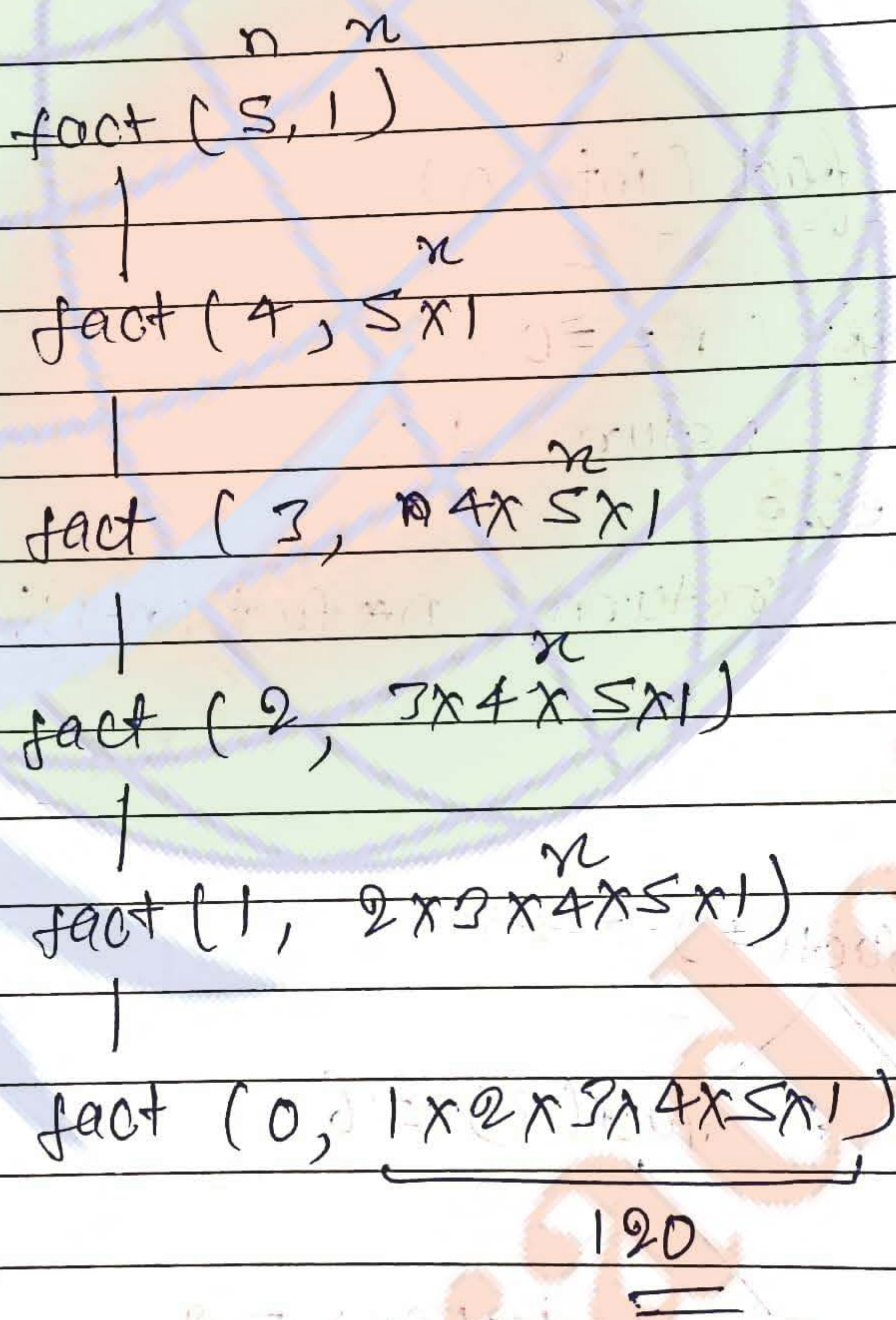
eg: >



returning time of multiplication
है है है

★ Converting recursion into tail recursion using auxiliary variables.

```
int fact (int n, int x)
{
    if (n == 0)
        return 1;
    else
        return fact (n-1, n*x);
}
```

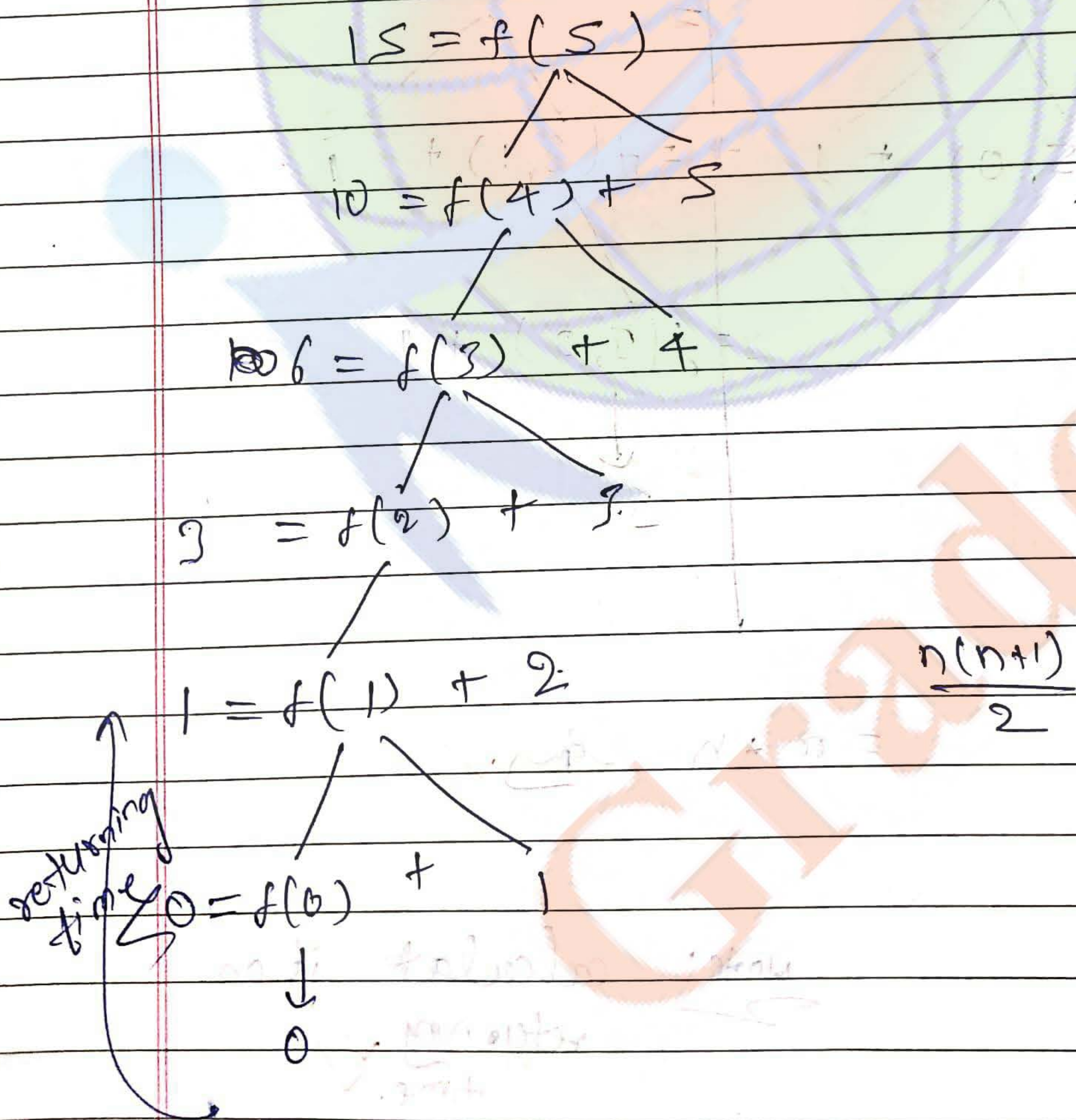


• we convert non-tail (recursion) to tail using extra parameters ~

```

*
int f(int n)
{
  if (n == 0)
  {
    return 0;
  }
  else
  {
    return f(n-1) + n;
  }
}

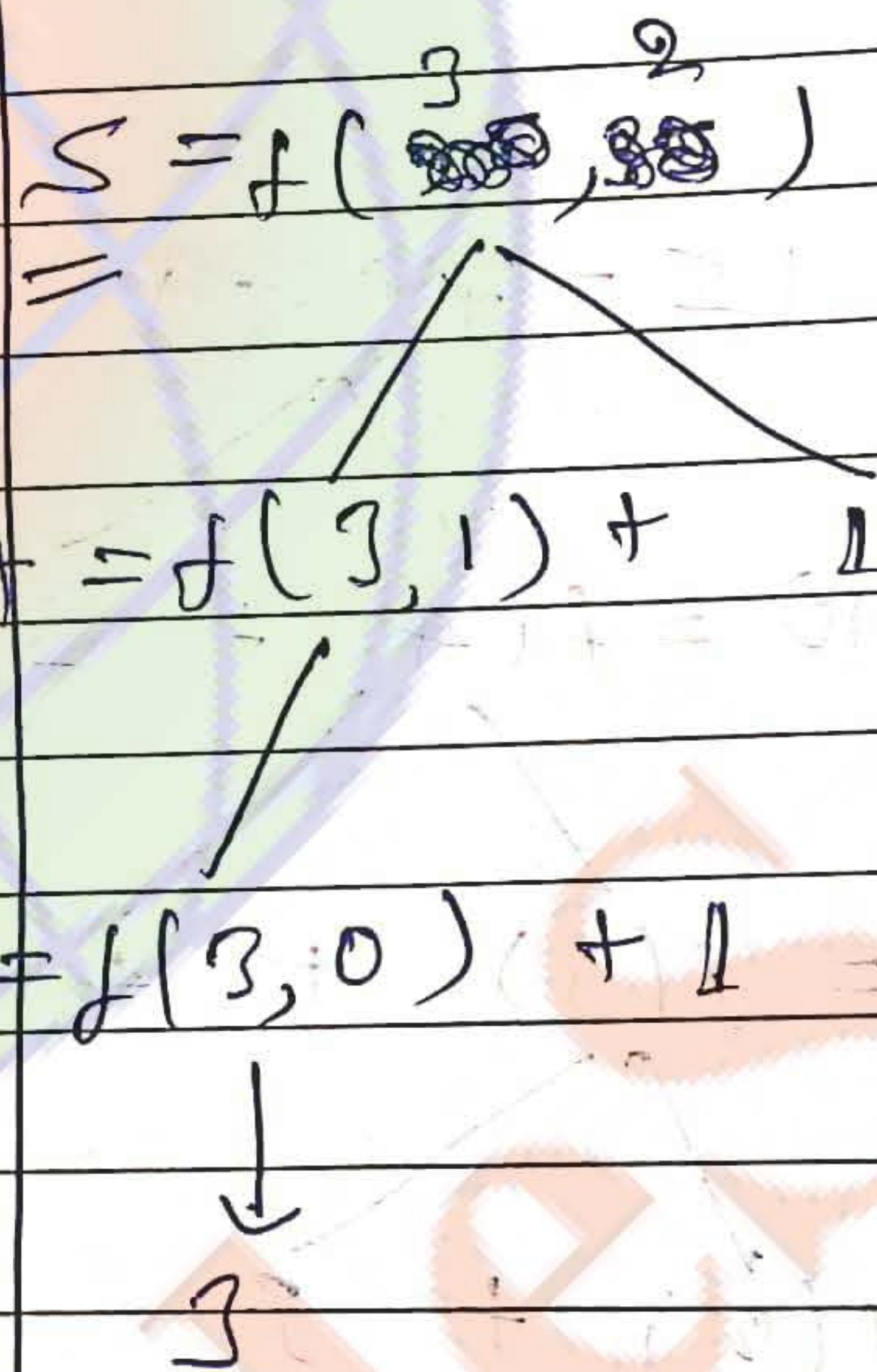
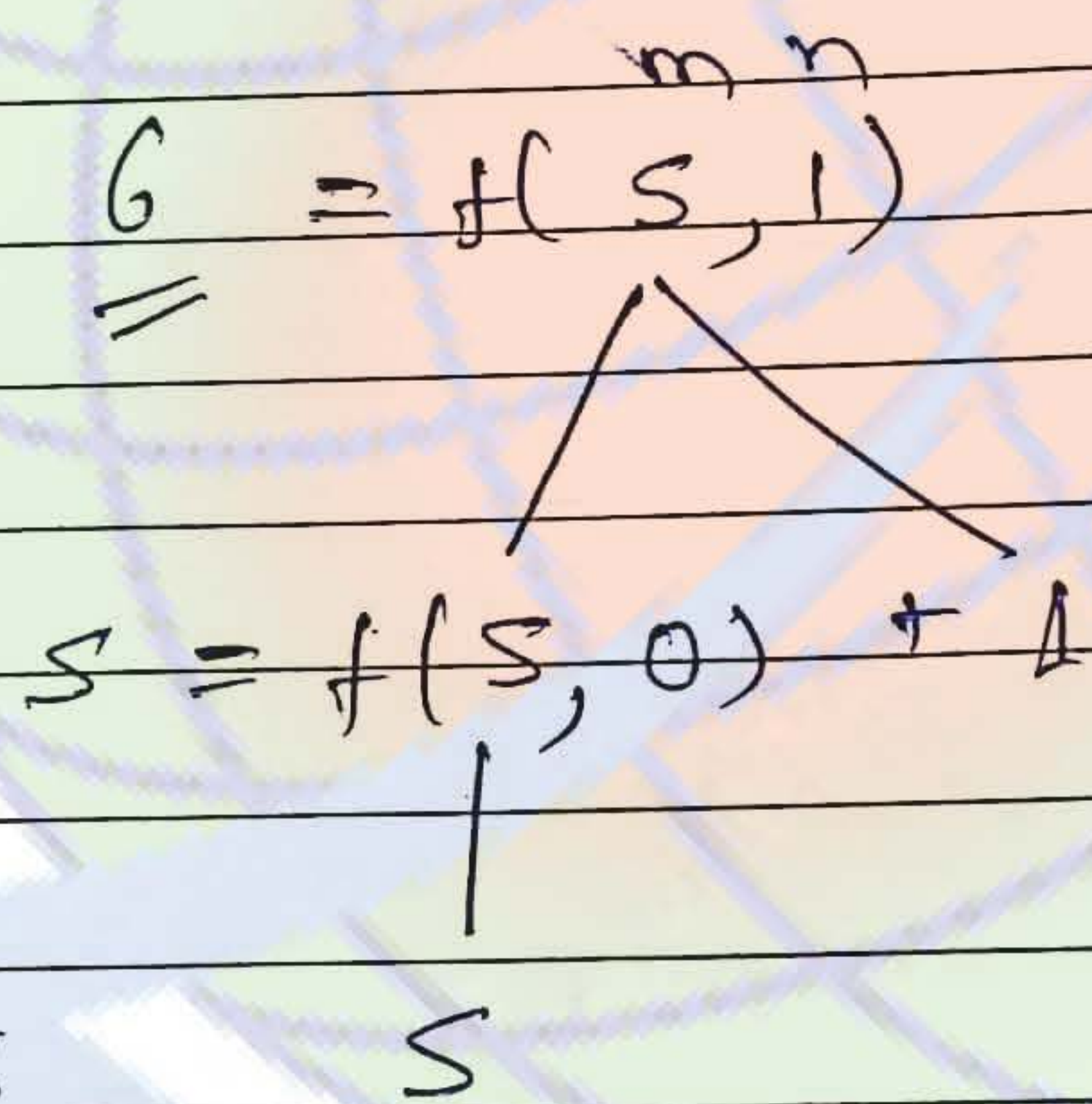
```



```

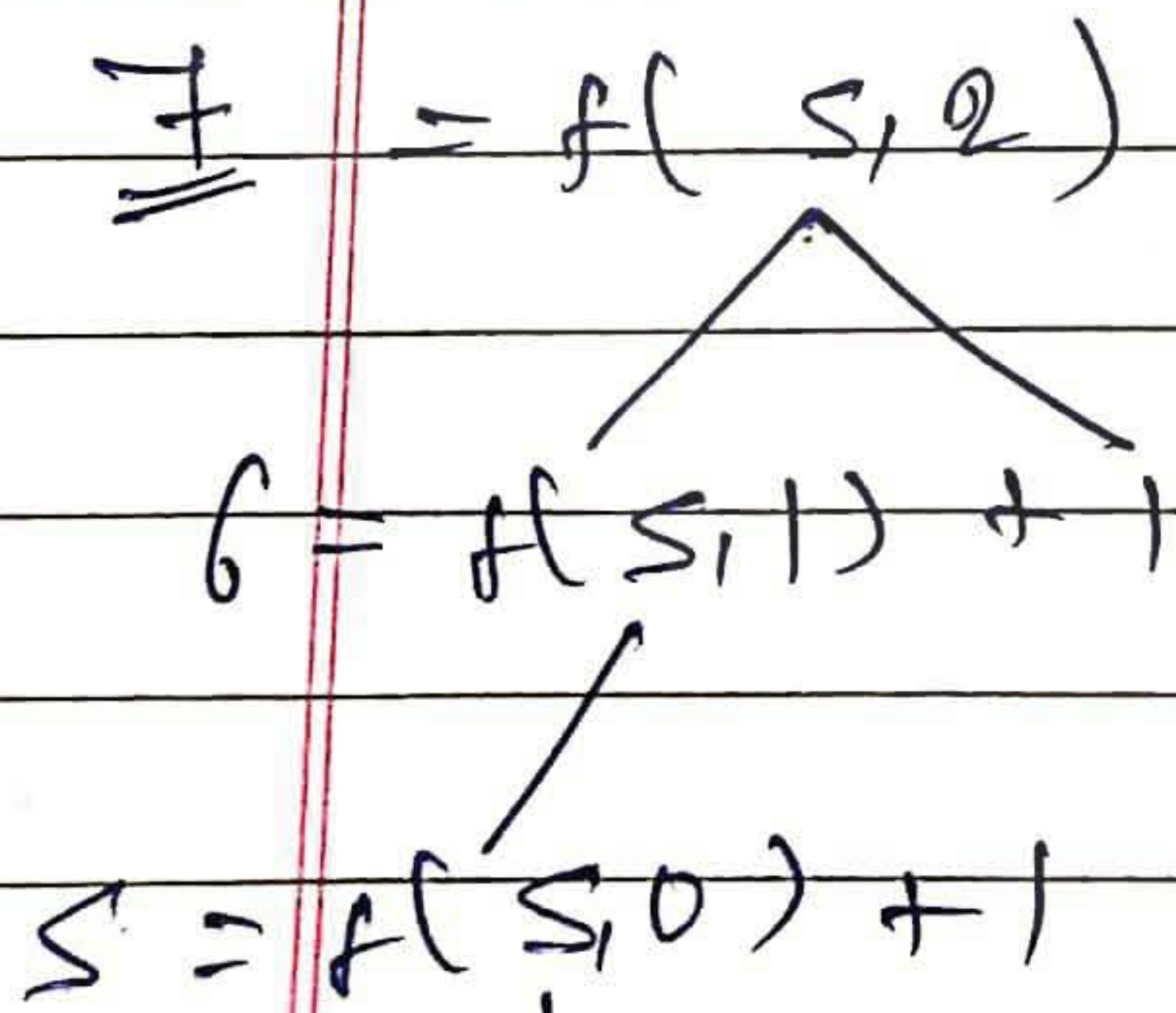
1) int f(int m, int n)
   {
     if (n == 0)
     {
       return m;
     }
     else
     {
       return f(m, n-1) + 1;
     }
   }

```



Choose any random number and try to find the number.

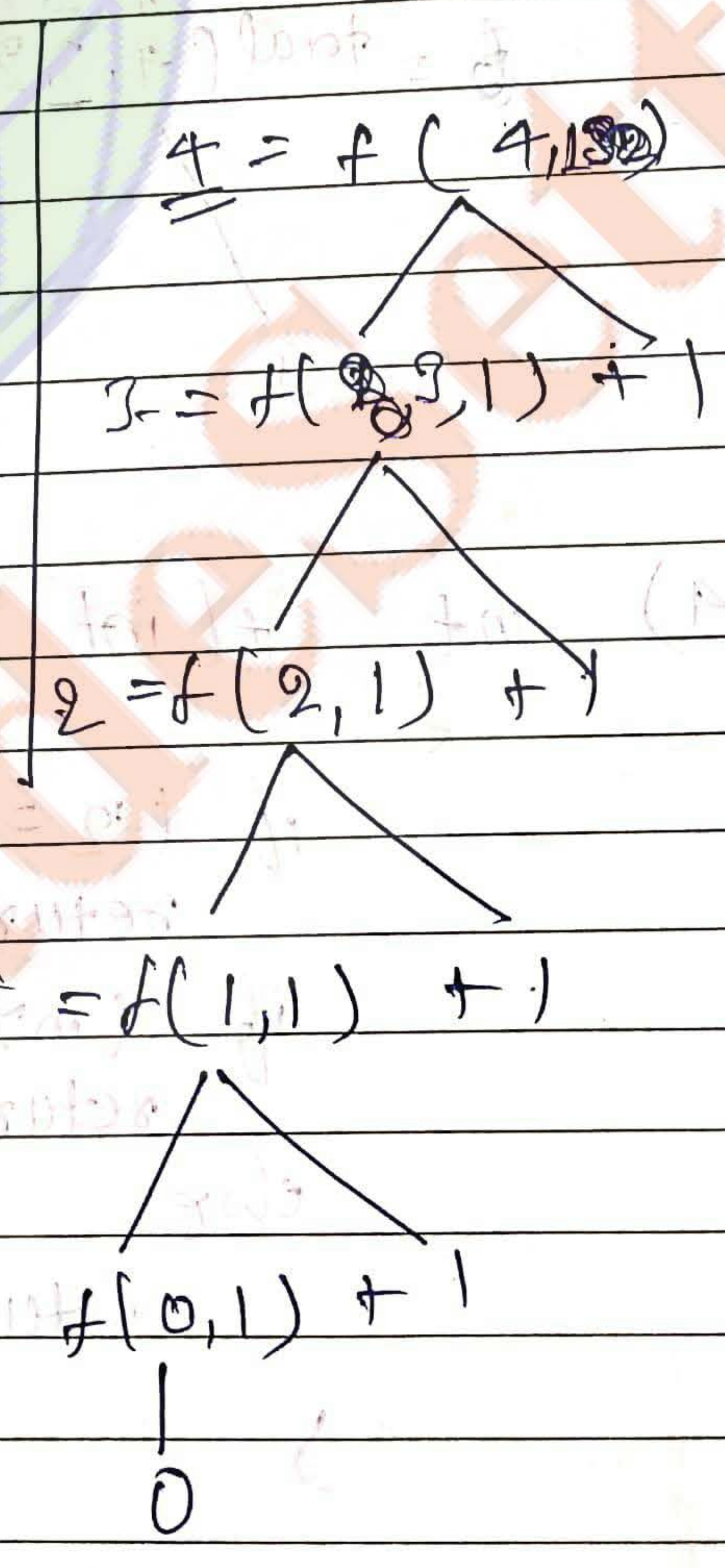
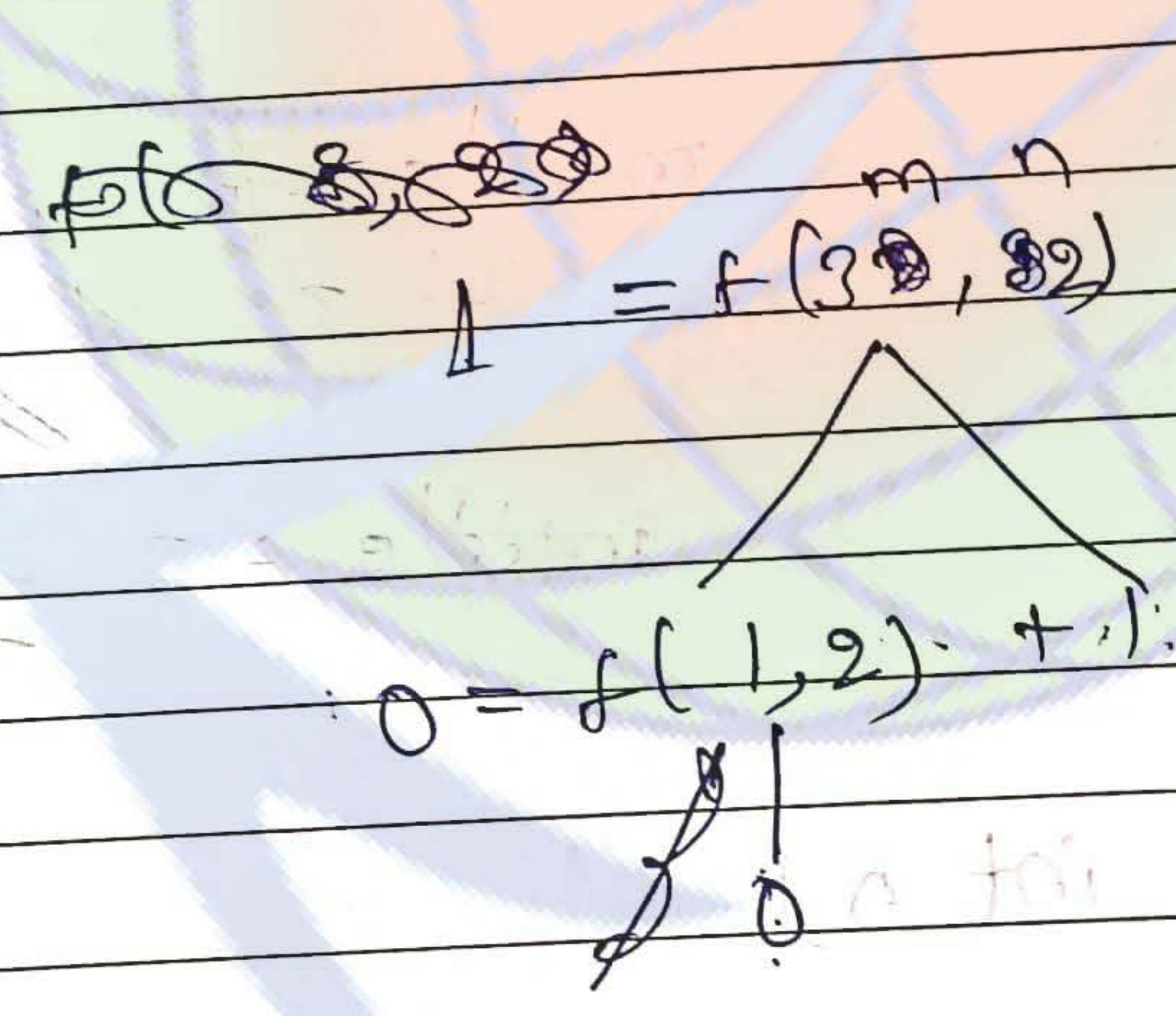
$S = m + n$ Ans ✓



Note: calculate it on returning time. ✓

```

    9. A
    int f(int m, int n)
    {
        if (m < n)
        {
            return 0;
        }
        else
        {
            return f(m-n, n) + 1;
        }
    }
    }
    
```

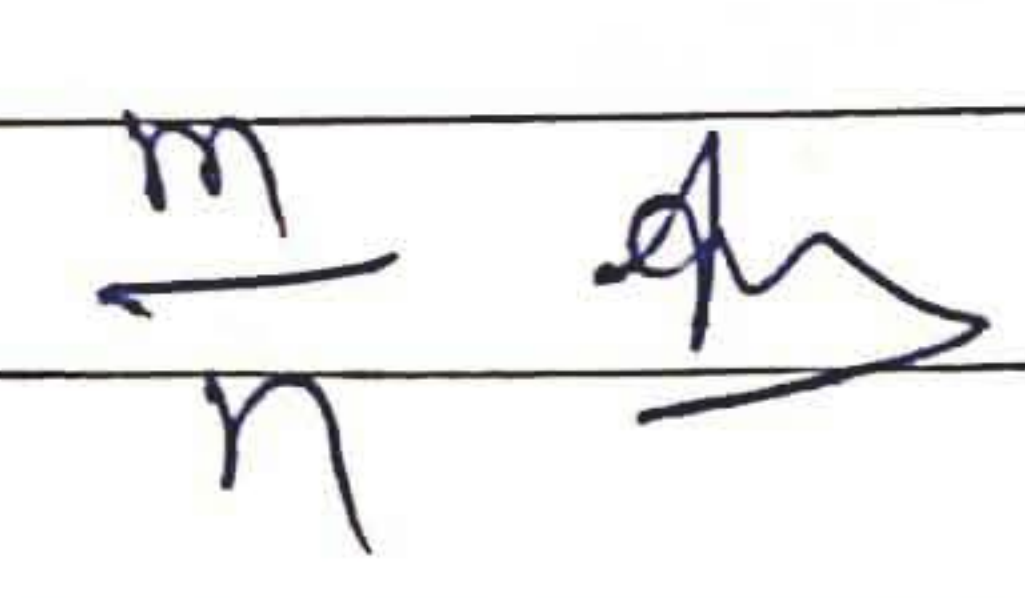


integer division

$3 = 1 \cdot 1$

$2 = 1$

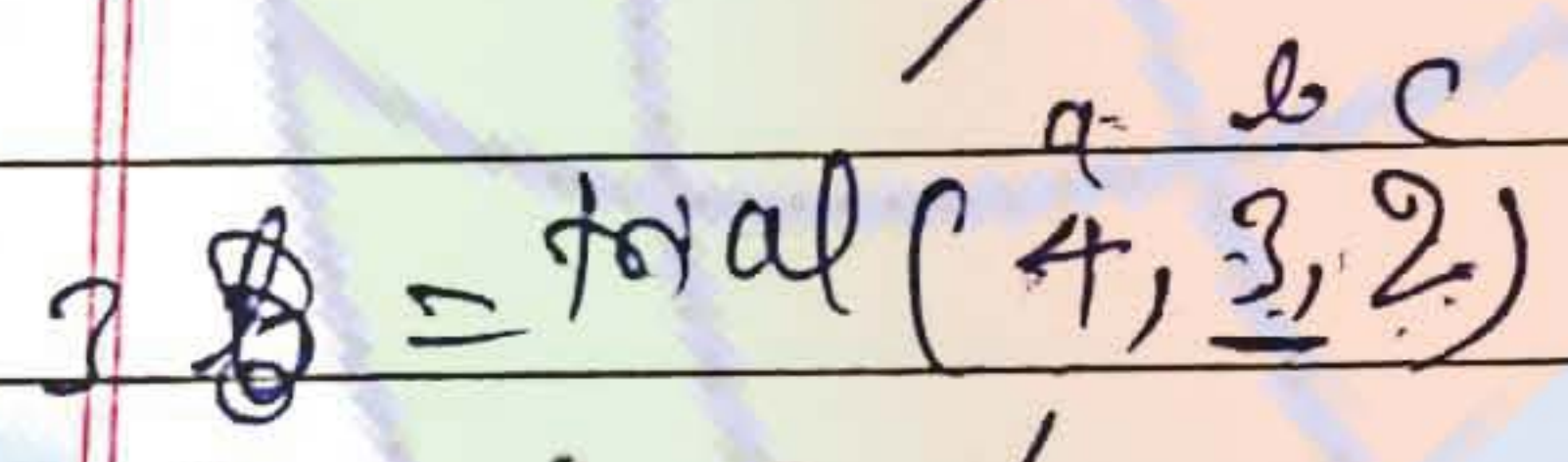
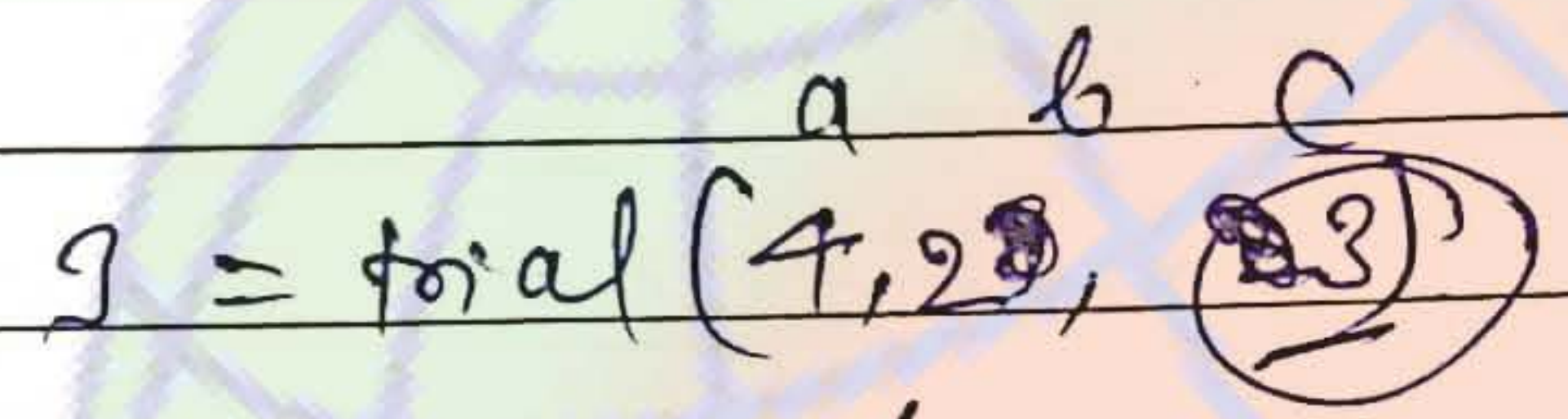
(integer division)



```

(3) int Total (int a, int b, int c)
    {
    if ( (a >= b) && (c < b) )
        return b;
    else if (a >= b) return Total (a, c, b);
    else return Total (b, a, c);
    }
    
```

middle element



middle of 2, 3, 4

is 3

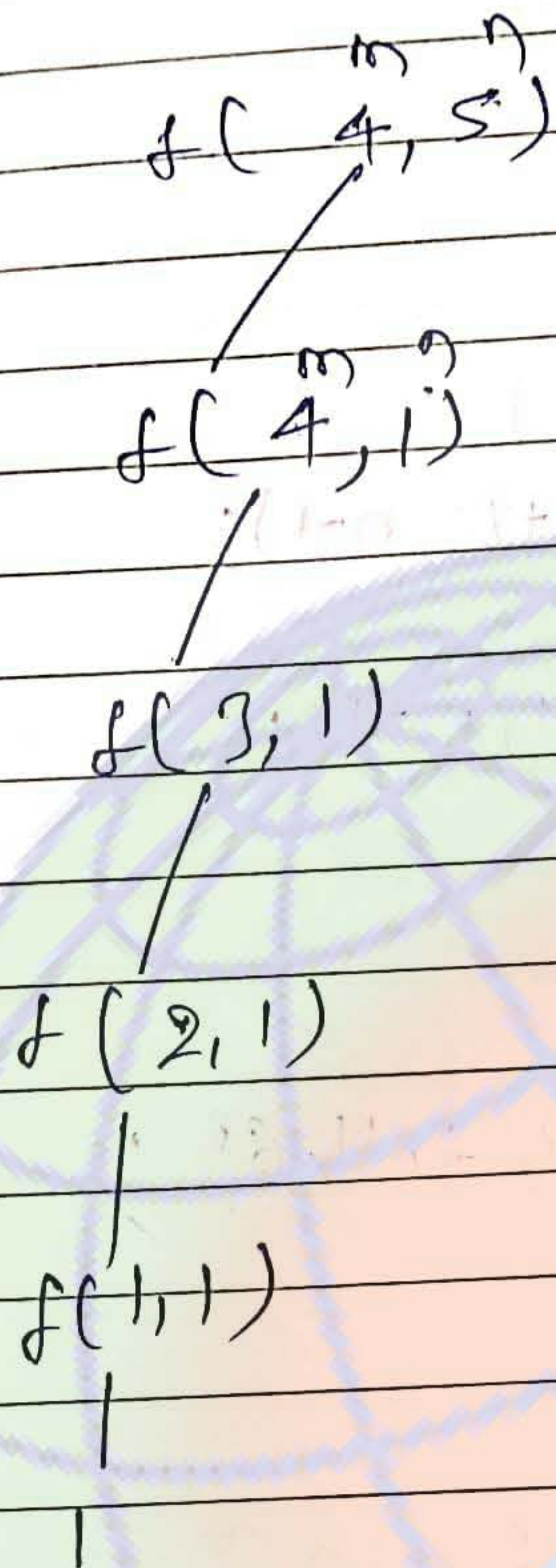
middle = 3

```

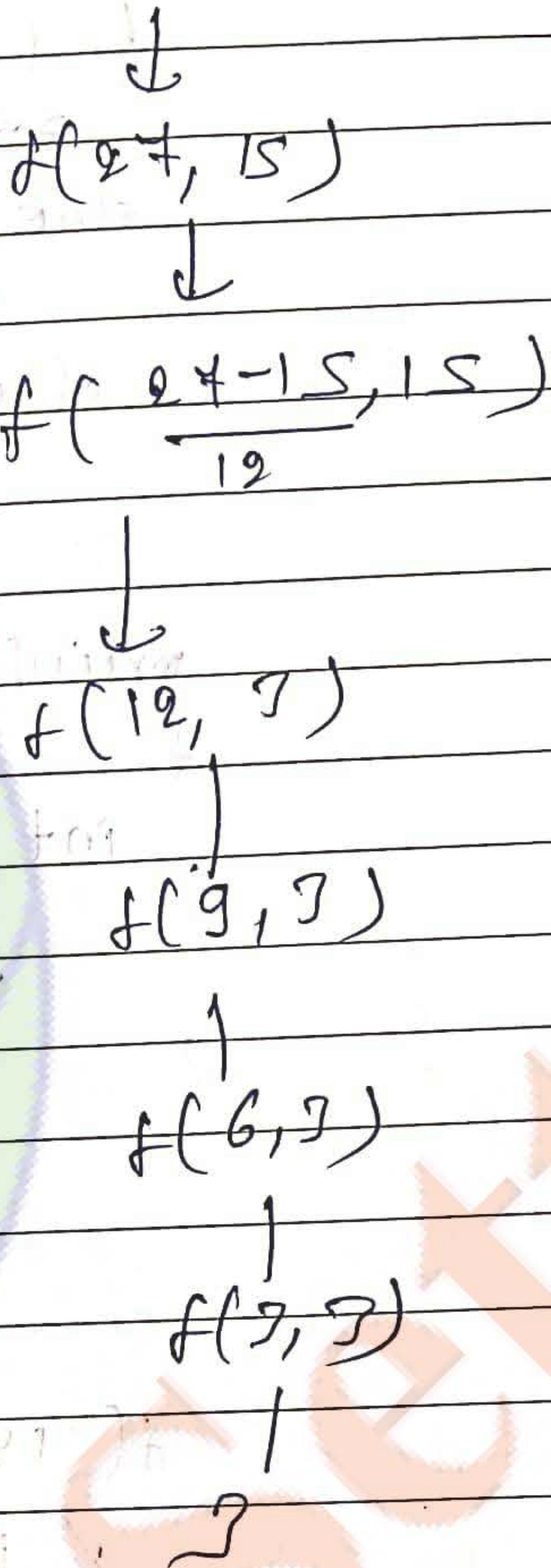
4) int f (int m, int n)
    {
    if (m == n)
        return m;
    if (m > n)
        return f (m-n, n);
    else
        return f (m, n-m);
    }
    
```

Ans GCD

Q1



$$f(27, 15) = 3$$



Ans Q1

egs) int f(int n)

static int s=0;
if (n <= 0) return 1;
if (n > 2) return f(n-2)+2;
return f(n-1)+s;
}

static code set
if n <= 0
if n > 2
return f(n-2)+2
return f(n-1)+s
return

```

static int s=0;
if (n <= 0) return 1;
if (n > 2) return f(n-2)+2;
return f(n-1)+s;
}

```

$$s = 0 \quad s = f(3) = 10$$

$$6 = f(3) + 2 = 10 + 2 = 18$$

$$1 = f(2) + s = 11 + 5 = 16$$

$$f(1) + s = 6 + 5 = 11$$

$$f(0) + s = 1 + 5 = 6$$

only write
s in
calling
time
not
write
final
value


```

eg: int f(int a, int n)
    {
        if (n <= 0)
            return 0;
        else if (a % 2 == 0)
            return a + f(a+1, n-1);
        else
            return a - f(a+1, n-1);
    }
    
```

```

main()
{
    int a[] = {12, 7, 13, 4, 11, 6};
    pf ( f(a, 6) );
}
    
```

$$f(12, 6) = 15$$

$$12 + f(7, 5) = 12 + 3 = 15$$

$$7 - f(13, 4) = 7 - 4 = 3$$

$$13 - f(4, 3) = 13 - 9 = 4$$

$$4 + f(11, 2) = 4 + 5 = 9$$

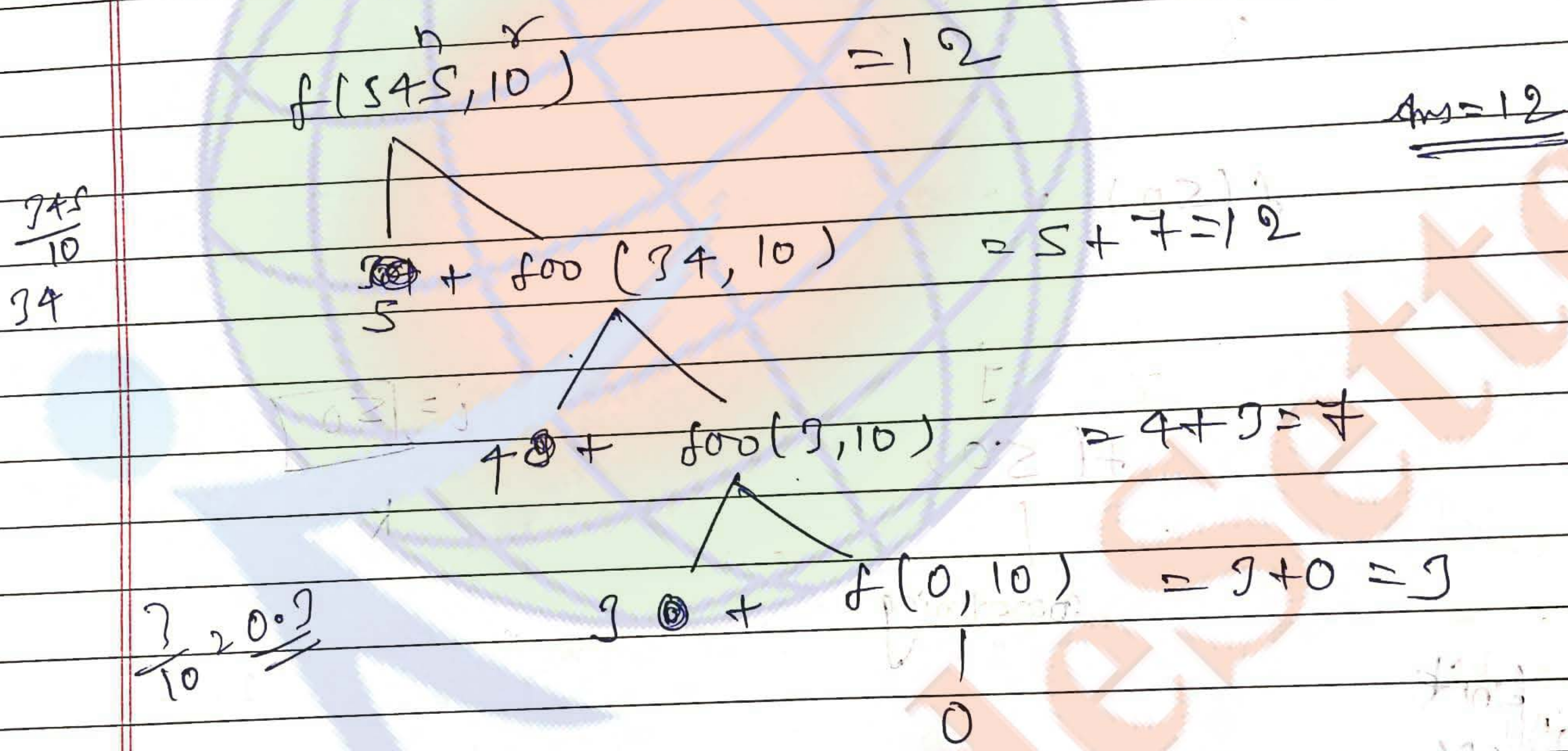
$$11 - f(6, 1) = 11 - 6 = 5$$

$$6 + f(0, 0) = 6 + 0 = 6$$

```

eg+> foo (int n, int r)
    {
    if (n > 0)
        return n % r + foo (n / r, r);
    else
        return 0;
    }
    
```

foo(545, 10); - ?



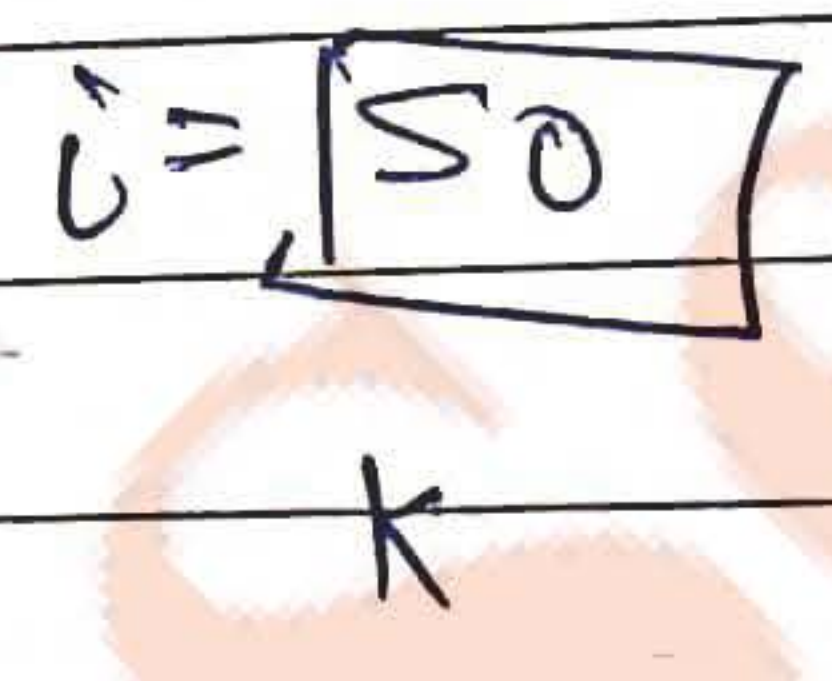
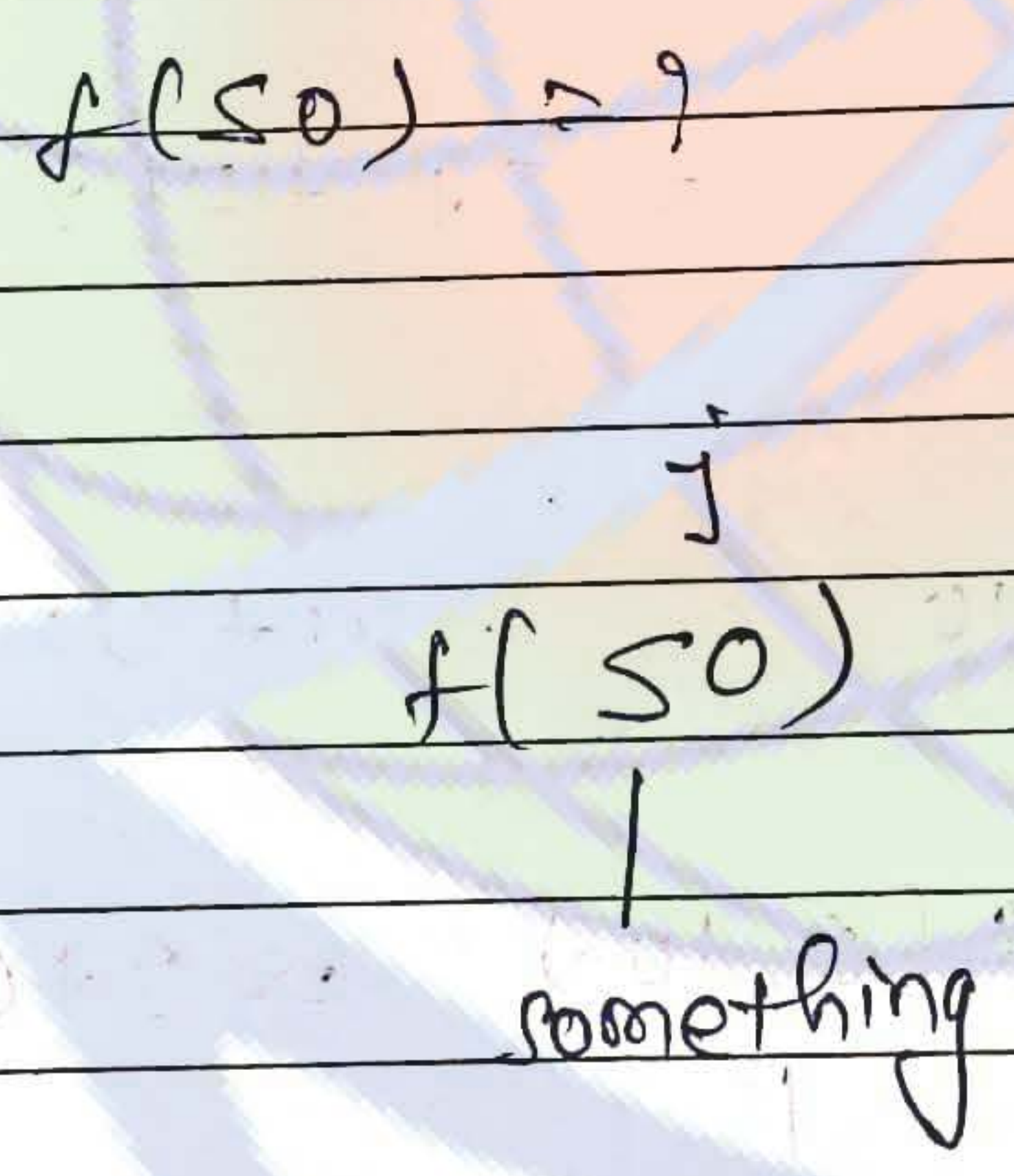
Note:

$n \% r = \text{remainder}$ ✓
 $\frac{n}{r} = \text{integer division}$ ✓

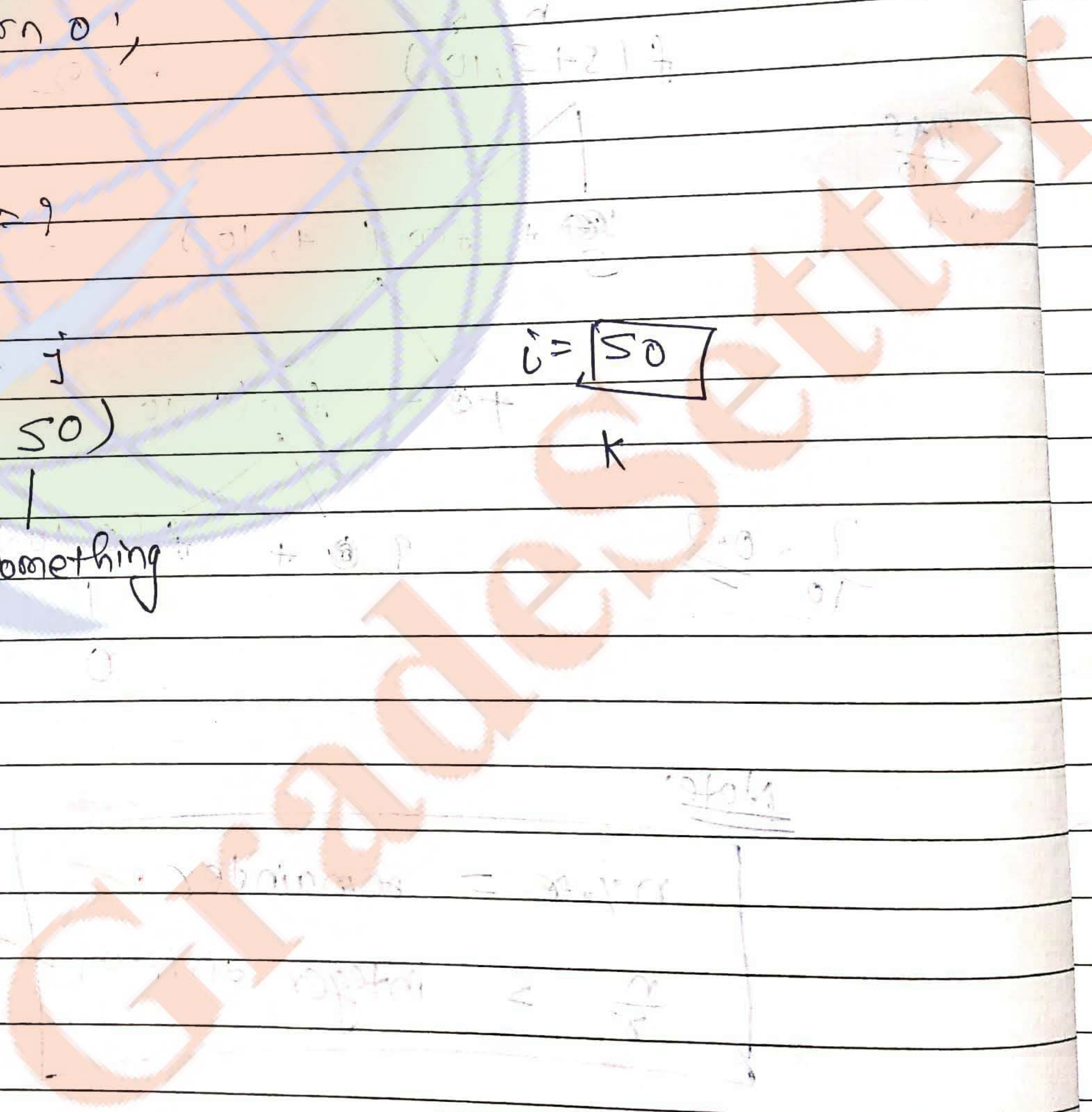
```

eg: int f(int i)
{
  static int i = 50;
  int k;
  if (i == 1)
  {
    pf("something");
    k = f(i);
    return 0;
  }
  else
  {
    return 0;
  }
}

```



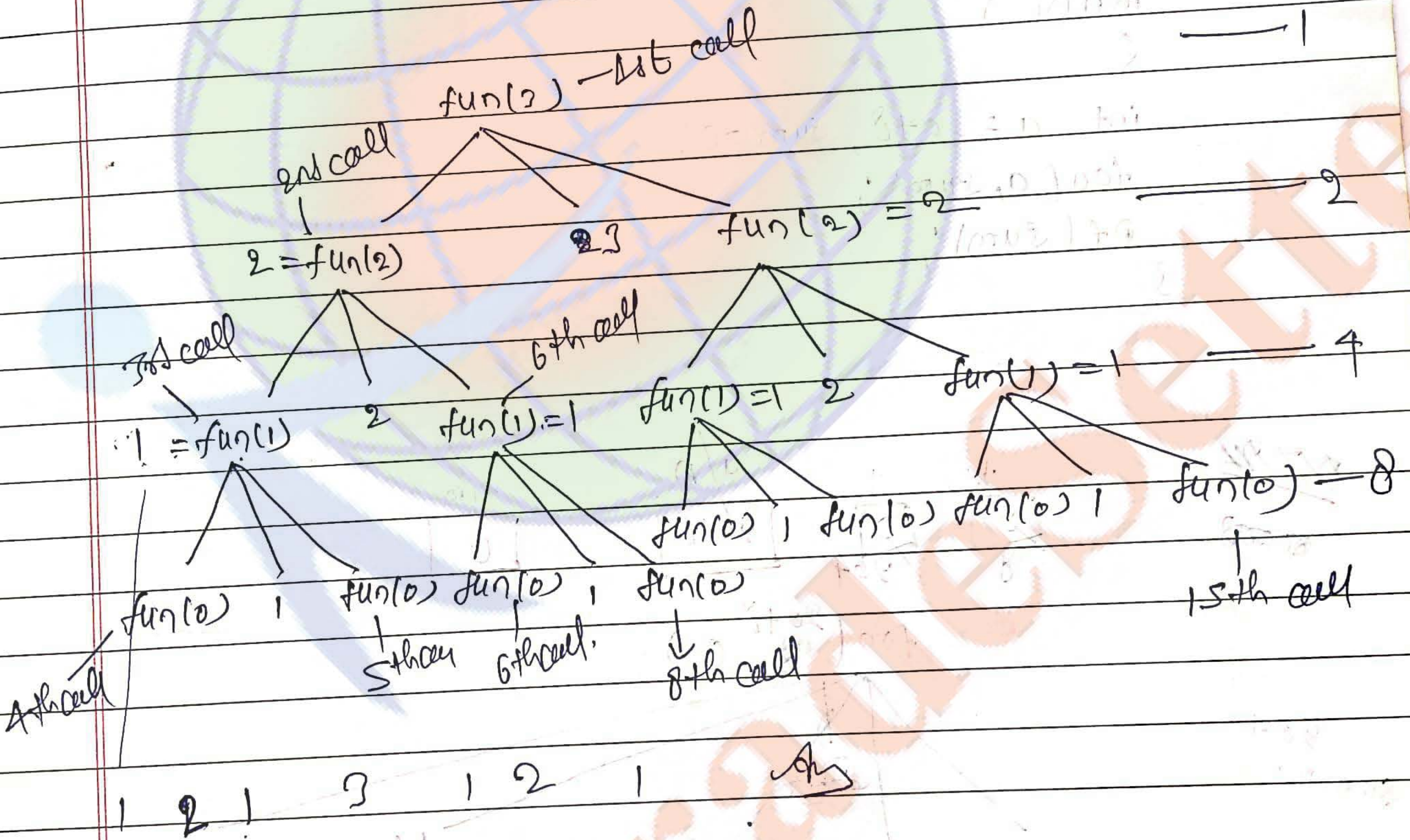
~~is infinite loop~~



4/06/17

```

eggs -> fun (int n)
{
    if (n > 0)
    {
        fun(n-1);
        pf(n);
        fun(n-1);
    }
}
fun(3)
    
```



if	call
$n=2$	7
$n=3$	$15 = 1 + 2 + 2^2 + 2^3 = 2^4 - 1 = 16 - 1 = 15$
so for n	$2^{n+1} - 1 = O(2^n)$

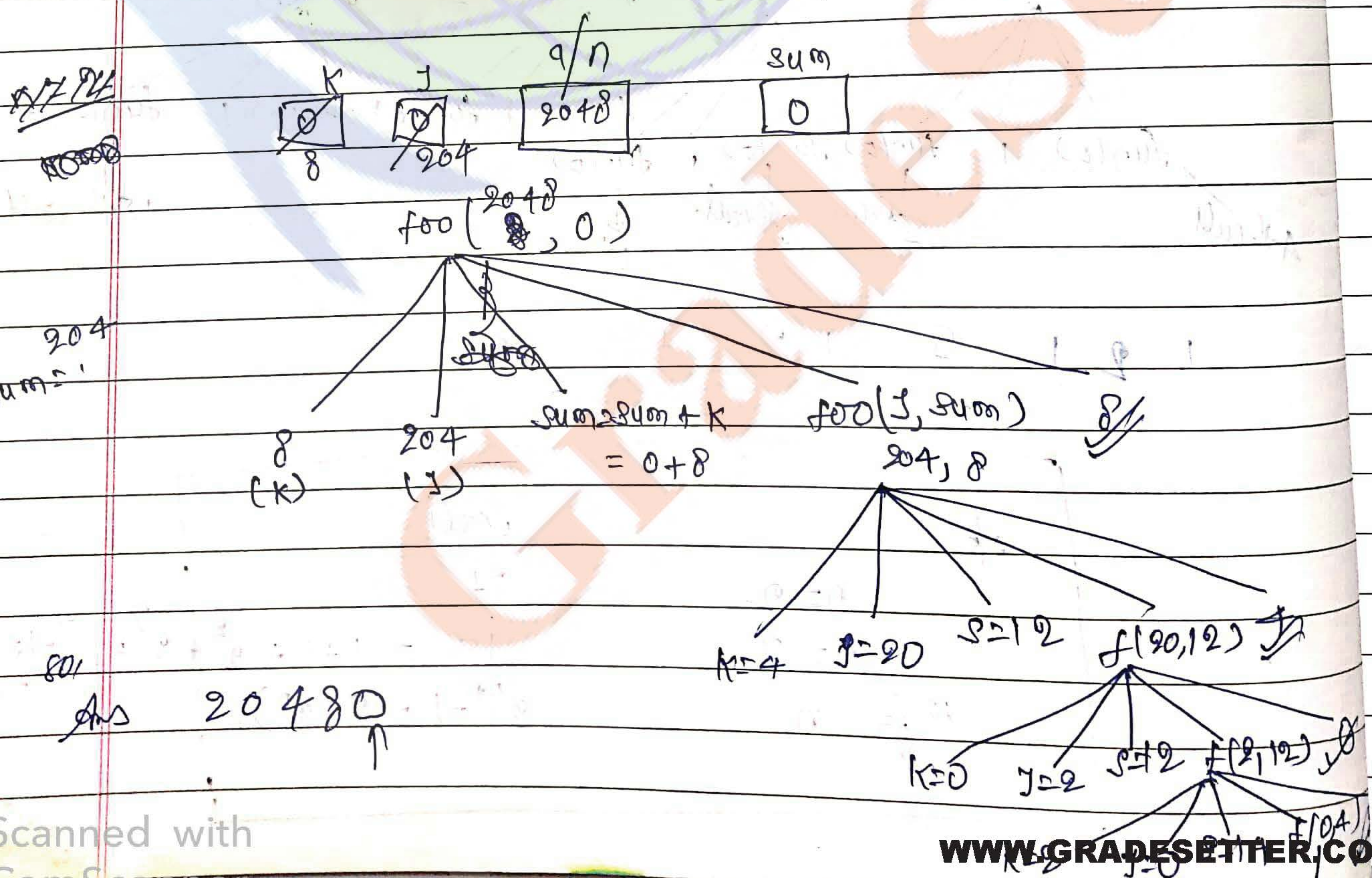
gate
qs.

gate

```

    02. > foo (int n, int sum)
    {
        int k=0, i=0;
        if (n==0)
            return;
        k = n%10;
        i = n/10;
        sum = sum+k;
        foo (i, sum);
        Pf (k);
    }

    main ( )
    {
        int a = 2048, sum = 0;
        foo (a, sum);
        Pf (sum);
    }
    
```



call by value, call by reference,
call by address.

classmate

Date _____

Page _____

gate
9/1

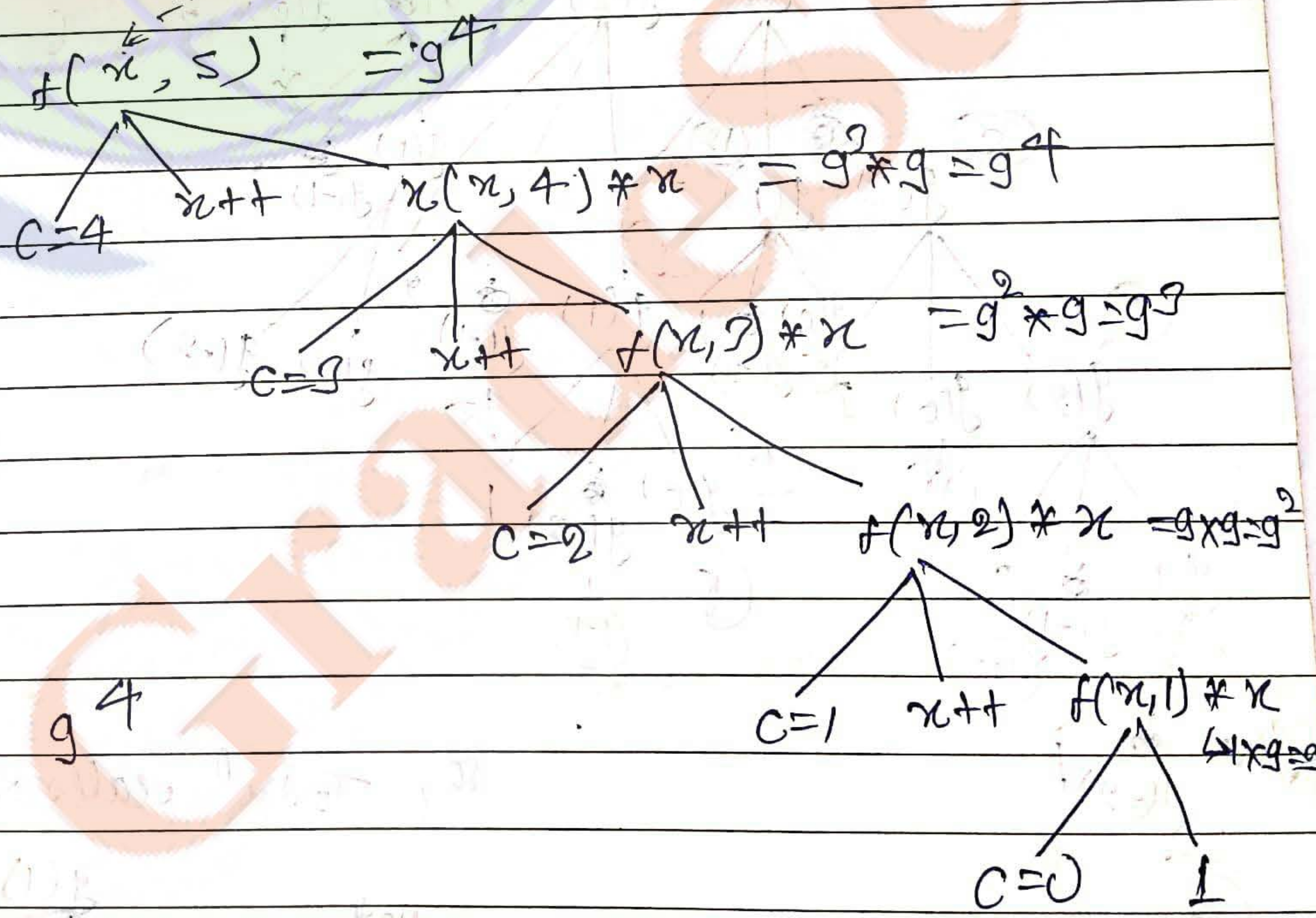
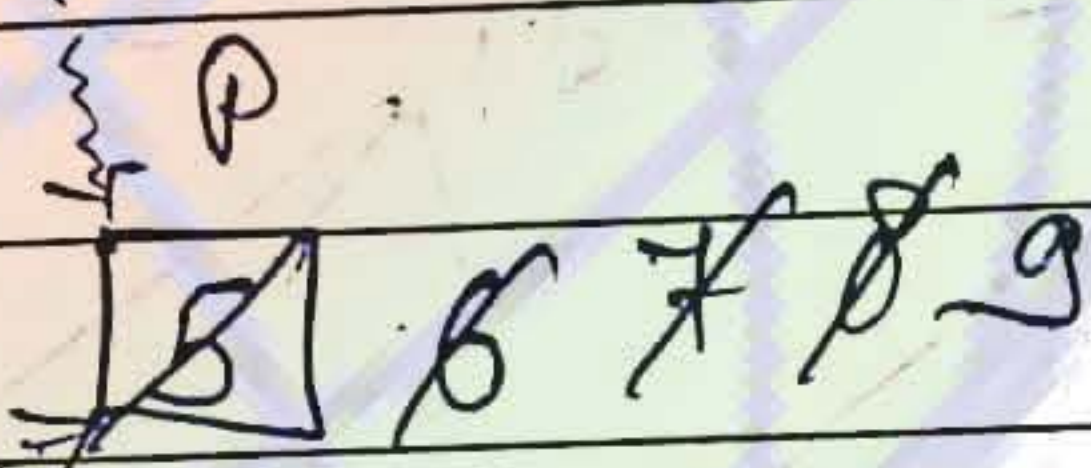
```
int f(int x, int c)
```

```
{
    c = c - 1;
    if (c == 0)
        return 1;
    x = x + 1;
    return f(x, c) * x;
}
```

```
main ()
```

```
{
    int p = 5;
    f(p, p);
}
```

reference variable

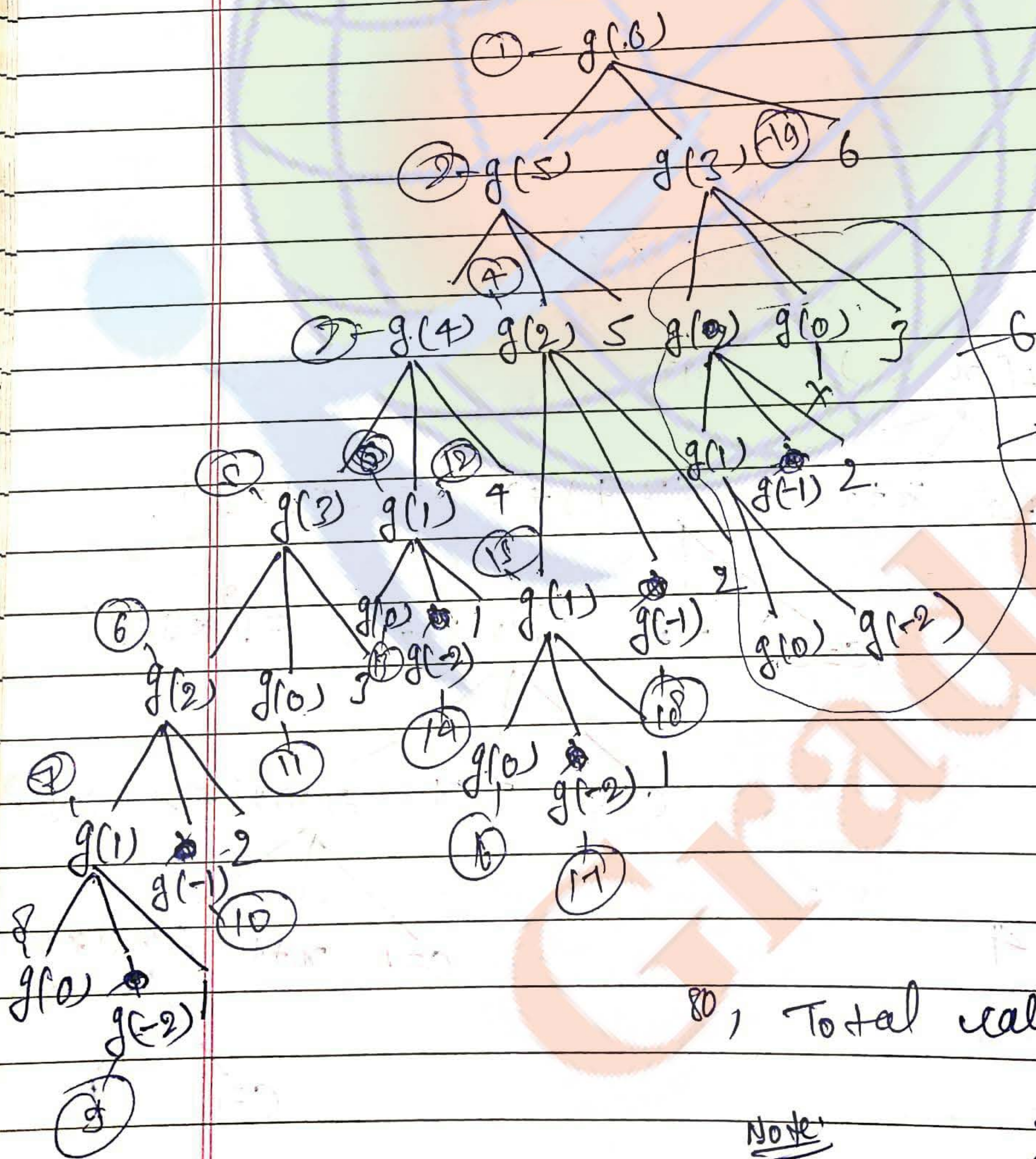


(call by reference) bases

```

4) void g(int n)
    {
        if (n < 1) return;
        g(n-1);
        g(n-3);
        pf(n);
    }
g(6)
    
```

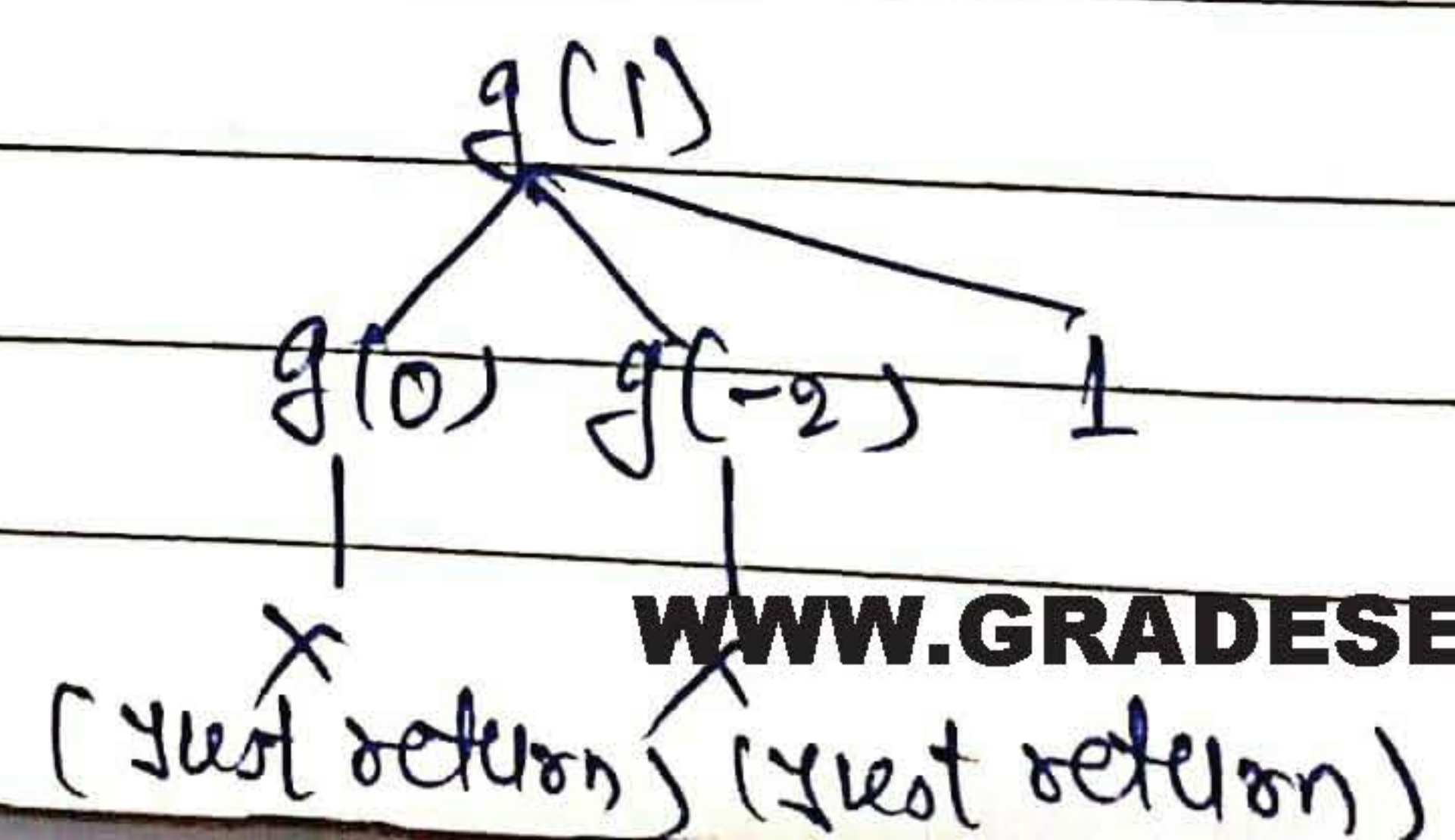
find the no. of calls.



→ simply take it from previous

∴ Total calls = 19 + 6 = 25

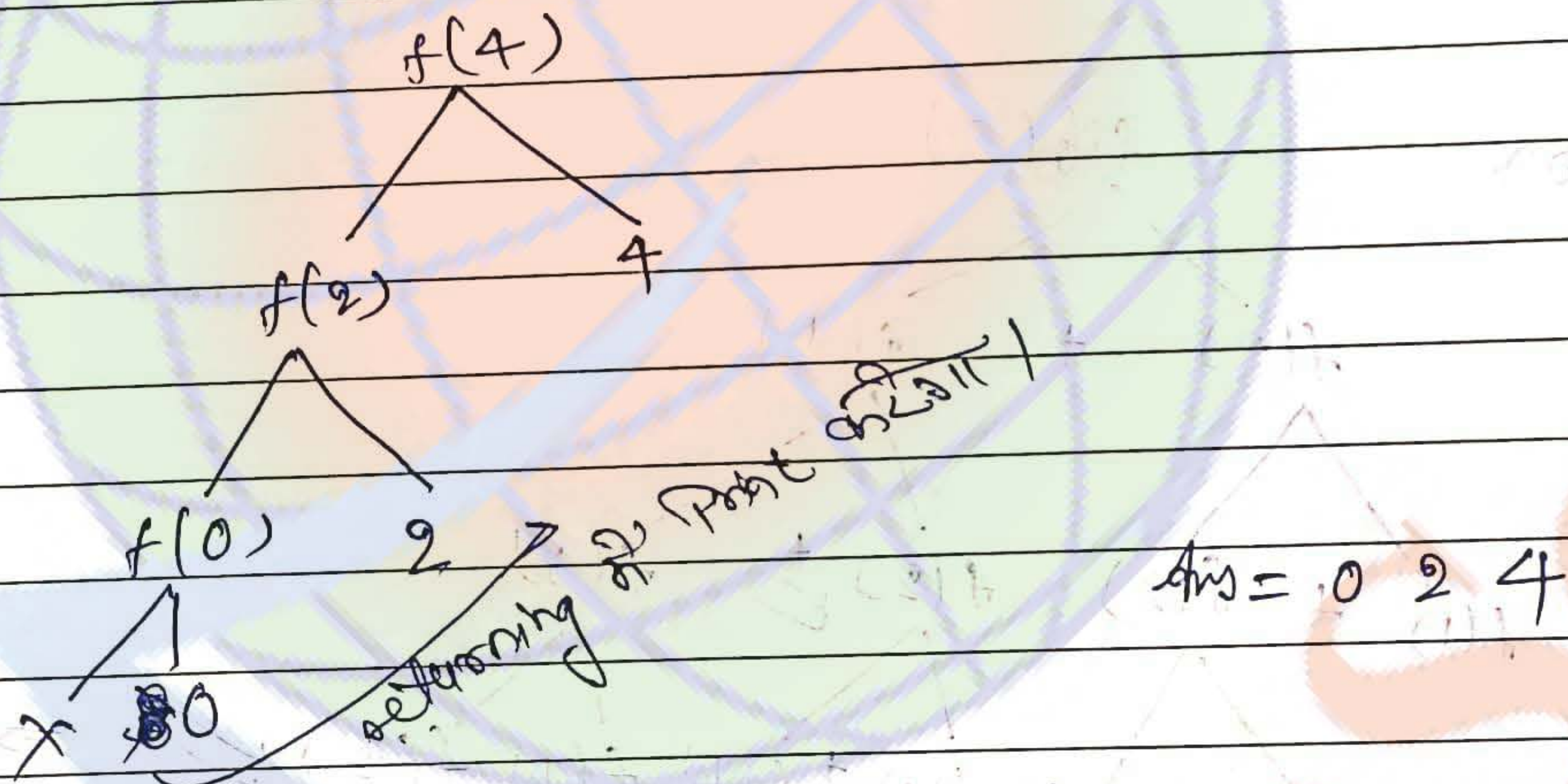
Note:



```

eg5: > f(int n)
        if (n > 0)
            f(n-2);
            printf(n);
        }
        f(4);
    
```

Here, code reading is important



```

eg6: > fib(n) = {
                0 if n = 0
                1 if n = 1
                fib(n-2) + fib(n-1) if n > 1
            }
    
```

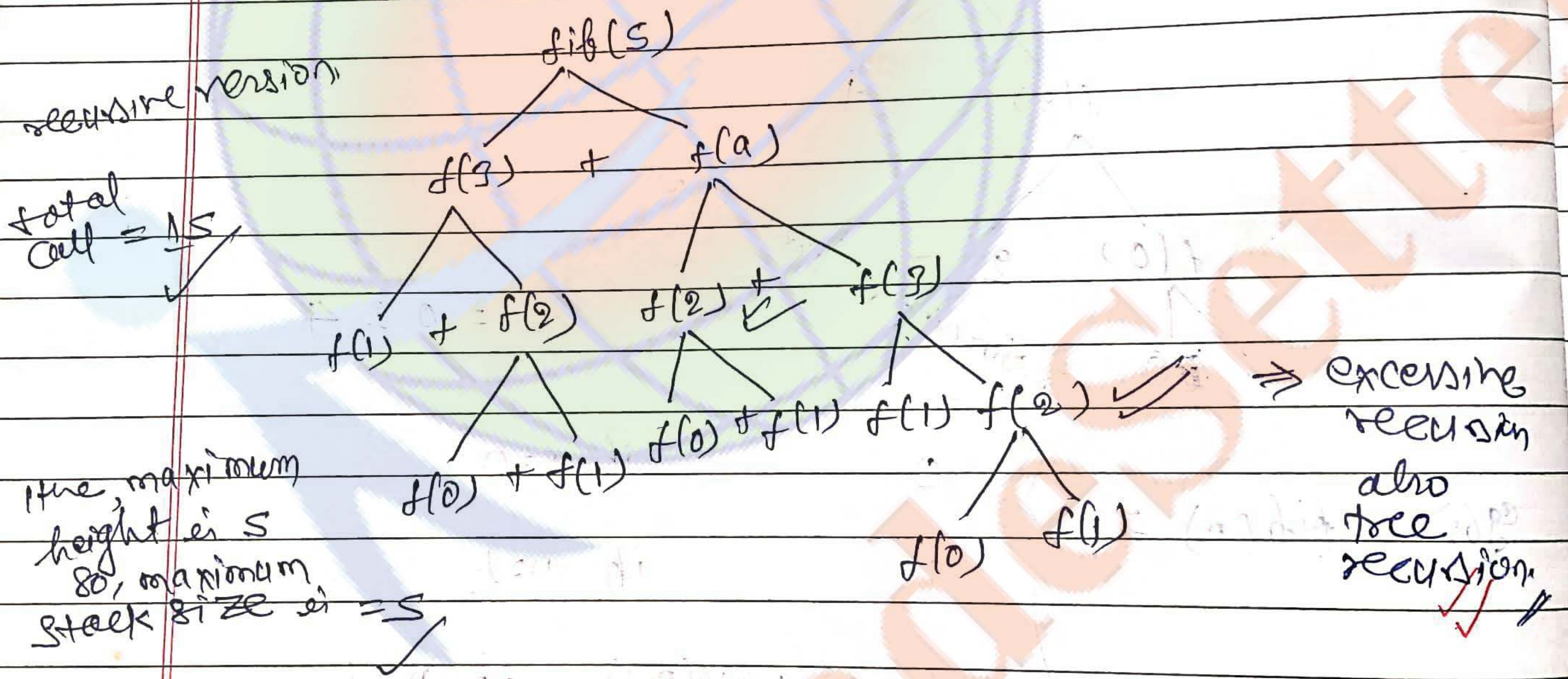
n	0	1	2	3	4	5	6	7	8
fib(n)	0	1	1	2	3	5	8	13	21

first two
number


```

int fib (int n)
{
    if (n <= 1)
        return n;
    else
        return fib (n-2) + fib (n-1);
}
    
```

eg) fib(5)



Linear recursion - if calling is only one time ✓
tree recursion - recursive function calling itself more than one times. ✓

Excessive recursion - if the recursive function is calling itself multiple times for the same parameter. ✓

Now, we are trying to remove excessive calls: -

↓
~~int~~ using memorisation

* memorisation → used to store the results of the function call to avoid excessive calls.

	0	1	2	3	4	5
F	-1	-1	-1	-1	-1	-1

```
int fib (int n)
{
```

```
  if (n <= 1)
  {
```

```
    F[n] = n;
    return n;
  }
```

```
  else
  {
```

```
    if (F[n-2] == -1)
```

```
      F[n-2] = fib (n-2);
```

```
    if (F[n-1] == -1)
```

```
      F[n-1] = fib (n-1);
```

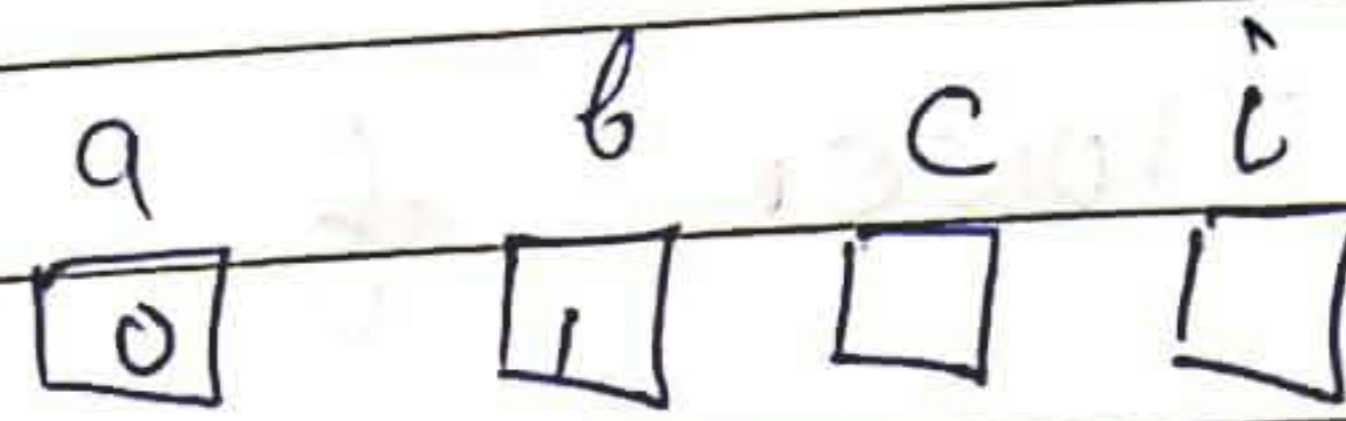
```
    return F[n-2] + F[n-1];
  }
```

```
}
```

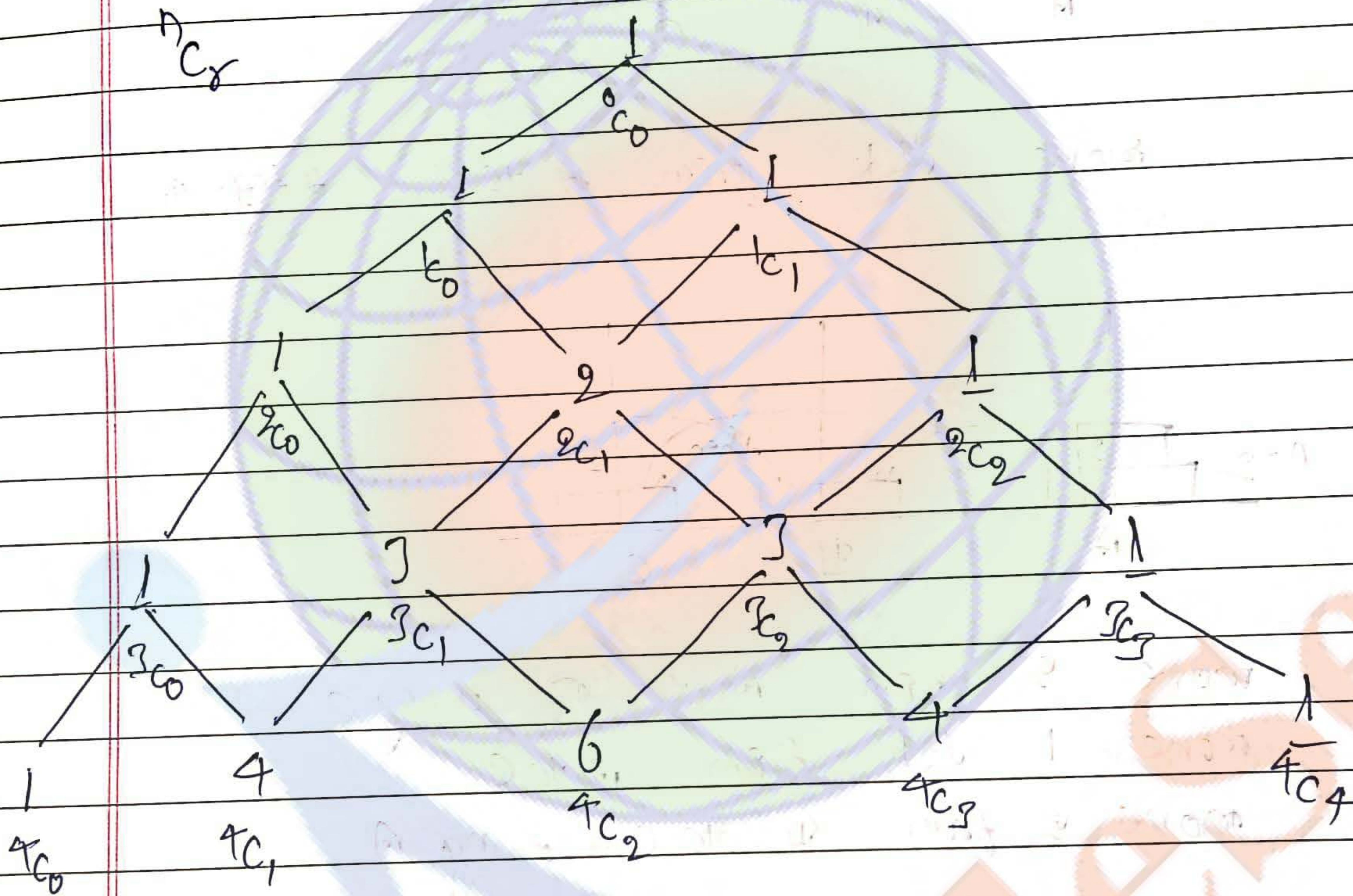
```
fib (n)
```

So, now the call is as follows.

fib(s)



★ Pascals triangle:

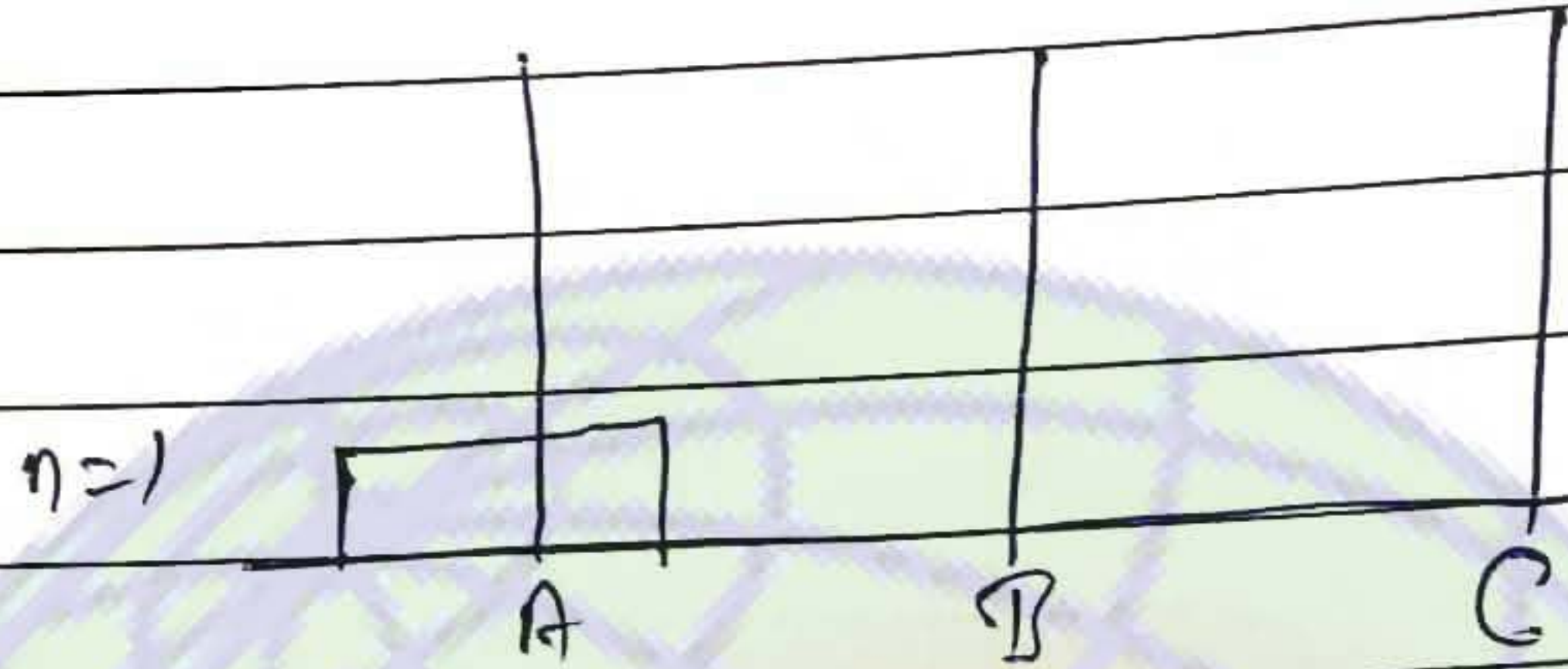


```

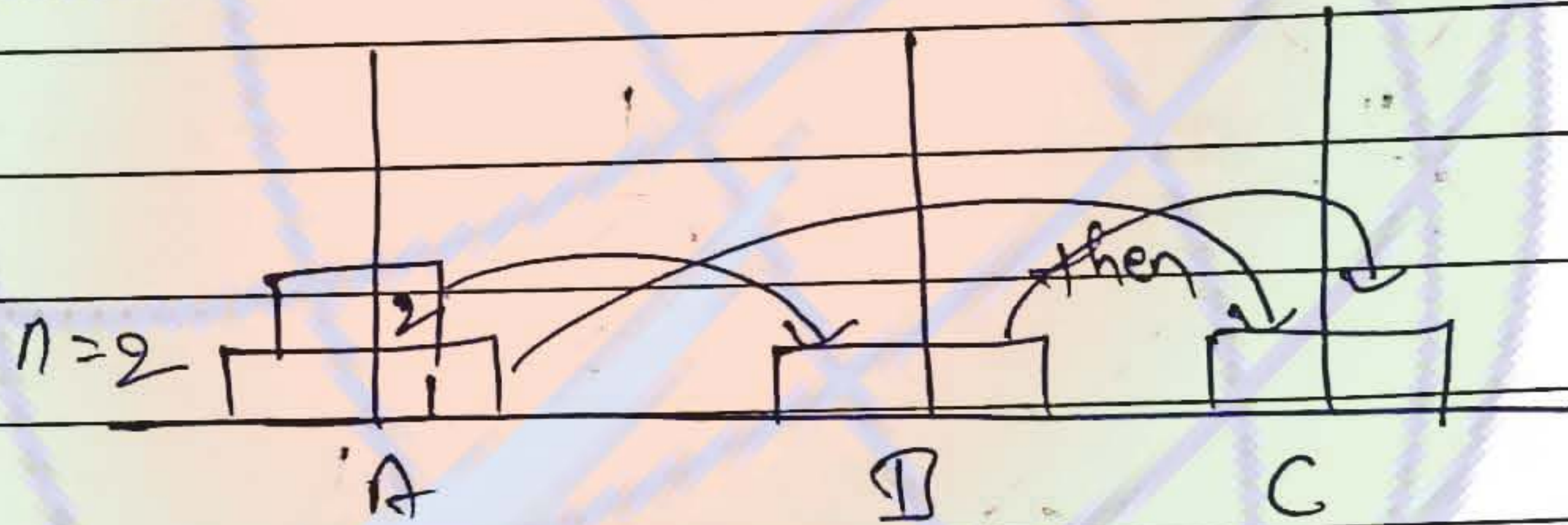
int comb (int n, int r)
{
    if (r == 0 || r == n)
        return 1;
    else
        return comb (n-1, r-1) + comb (n-1, r);
}
    
```

This is recursive definition for finding any combination value.

★ Tower of Hanoi

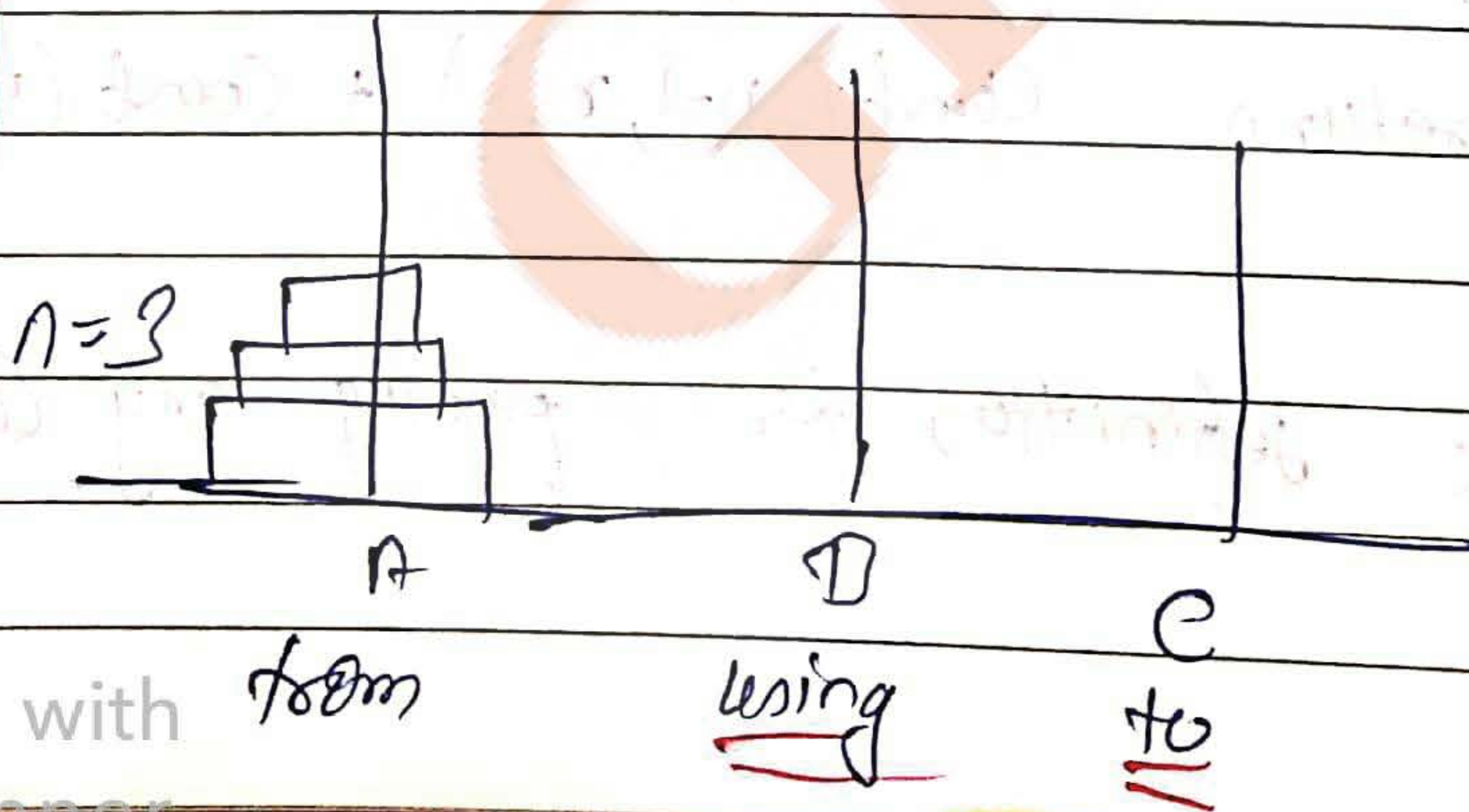


move disk from A to C using B



move 2 from A to B using C
 move 1 disk from A to C
 move 2 from B to C using A

- (i) one disk should move at a time
- (ii) larger disk should not be kept over smaller disk



1. → move 2 disks from A to B using C
2. → move a disk from A to C
3. → move 2 disk from B to C using A.

Now,

for n disks

1. → move $n-1$ disks from A to B using C
2. → move a disk from A to C
3. → move $n-1$ disks from B to C using A

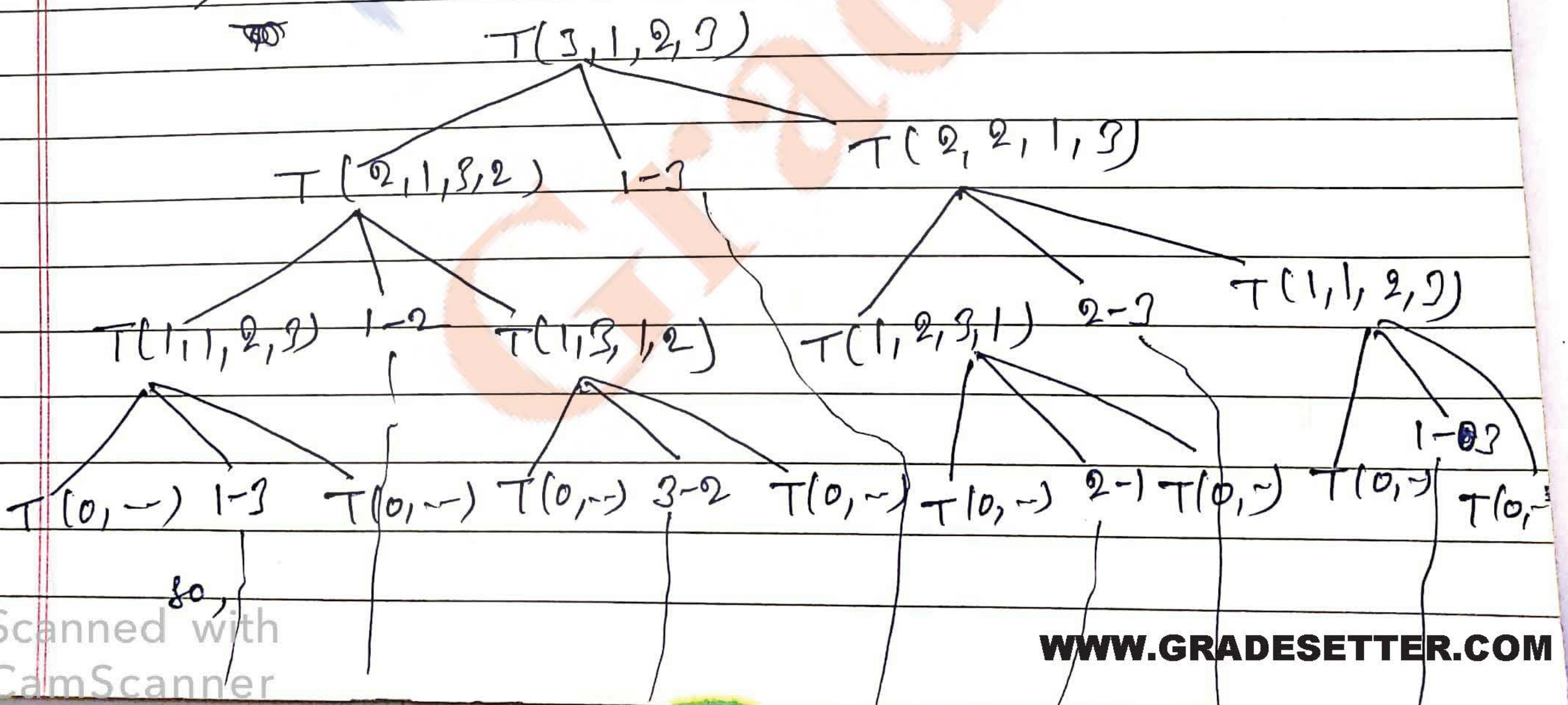
TOH (int n, int A, int B, int C)

```

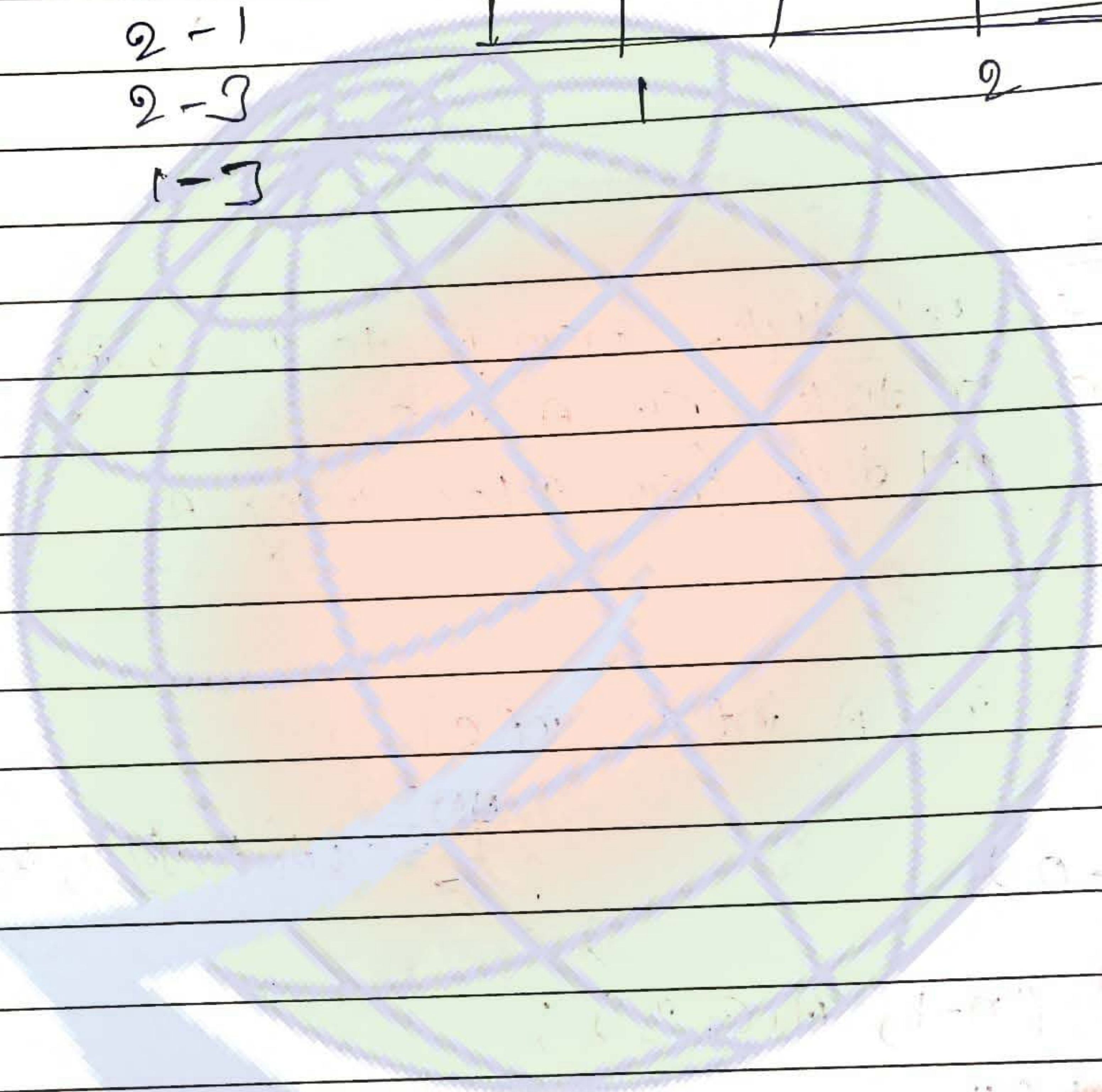
    {
        if (n > 0)
        {
            TOH (n-1, A, C, B);
            printf ("move a disk from %d to %d", A, C);
            TOH (n-1, B, A, C);
        }
    }

```

Note
TOH (n, from, using, to)



- 1-3
- 1-2
- 2-2
- 1-3
- 2-1
- 2-3
- 1-3



GradeSetter

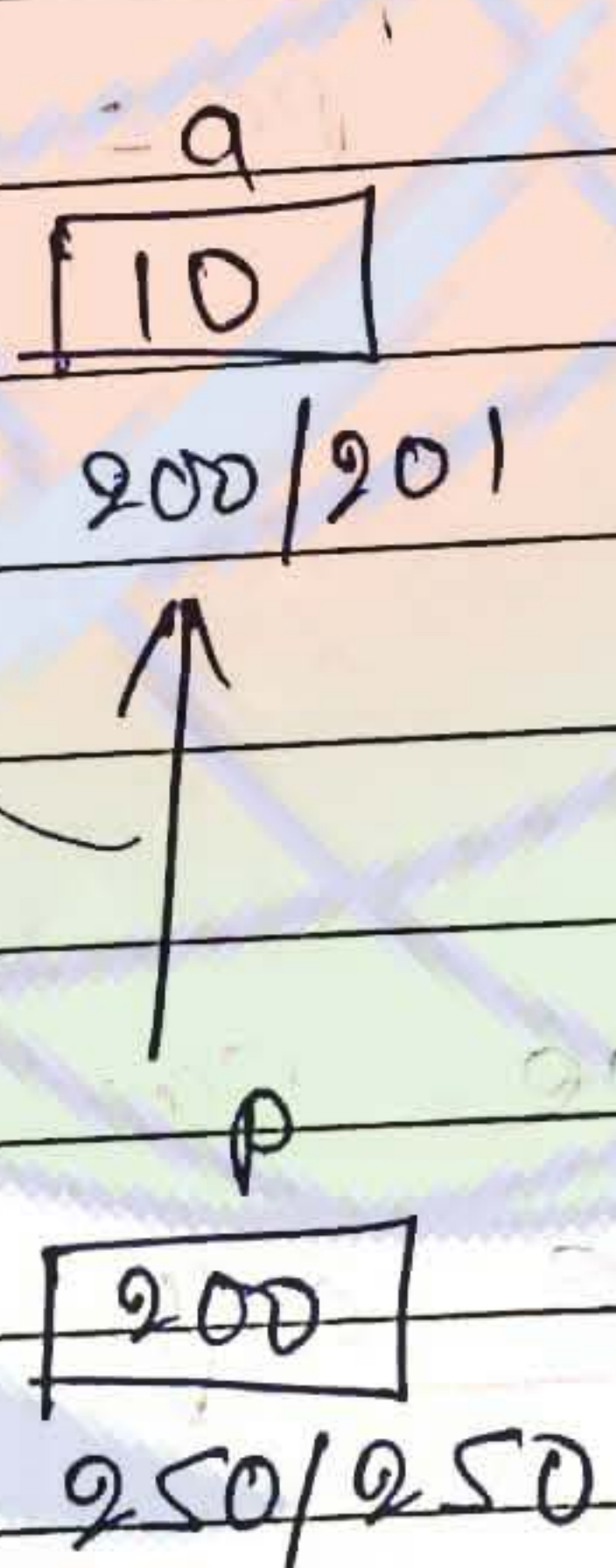
Pointers:

① data variable = int a = 10 ✓
 address variable = int *P

 a
 10
 200

2.7 #
 declaration: int a = 10;
 initialization: int *P;
 dereferencing: P = &a;
 printf ("%d", *P); — 10
 printf ("%d", P); — 200

Dereferencing means going to that address and take the value

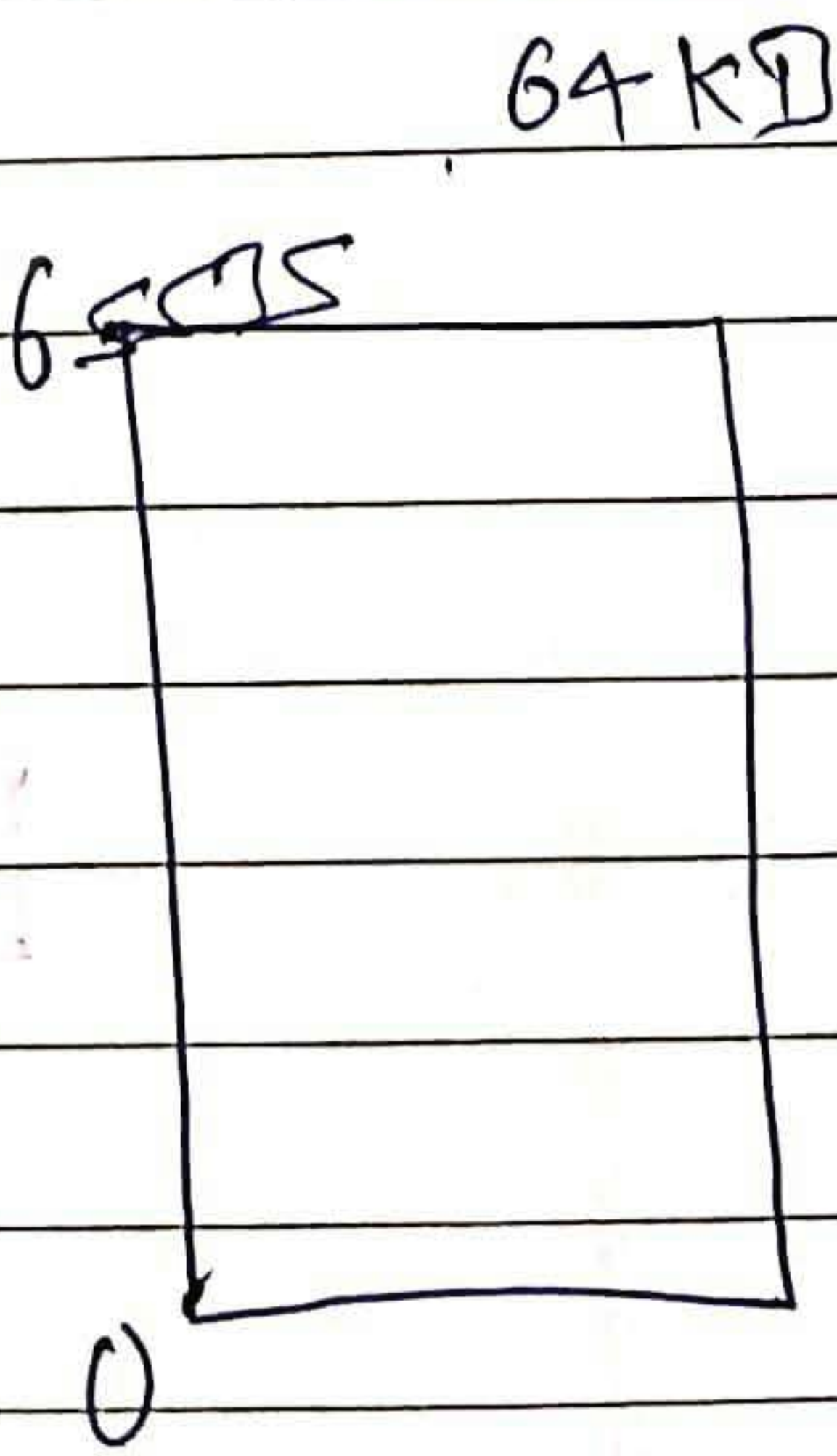
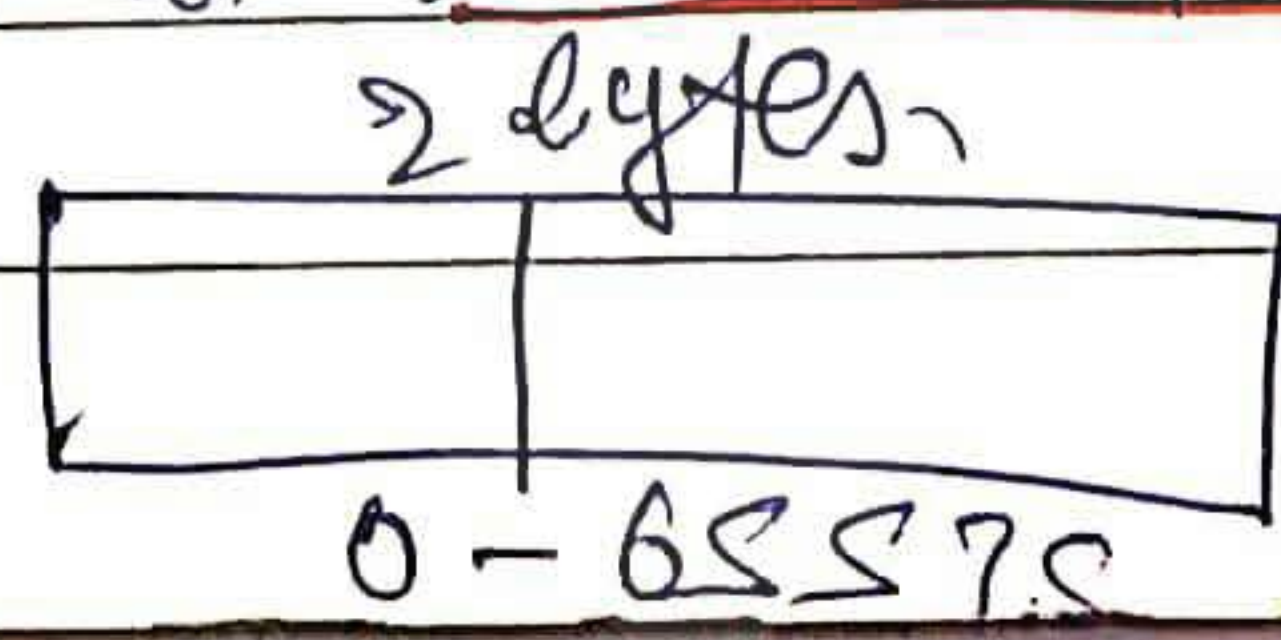


Note: Pointer will take address of 1st byte of the data

3. size of pointer

✓ int P1; — 2
 ✓ char P2; — 1
 ✓ float P3; — 4

- pointer is the address of the data
- pointer is like a key.



- Every pointers takes 2 bytes, it can refer to memory ranging to memory 64 KB.
- Pointer is only taking address not data.
- Size does not depend on the datatype of pointer
- Pointer is unsigned integer (only the value from 0 to 65535)

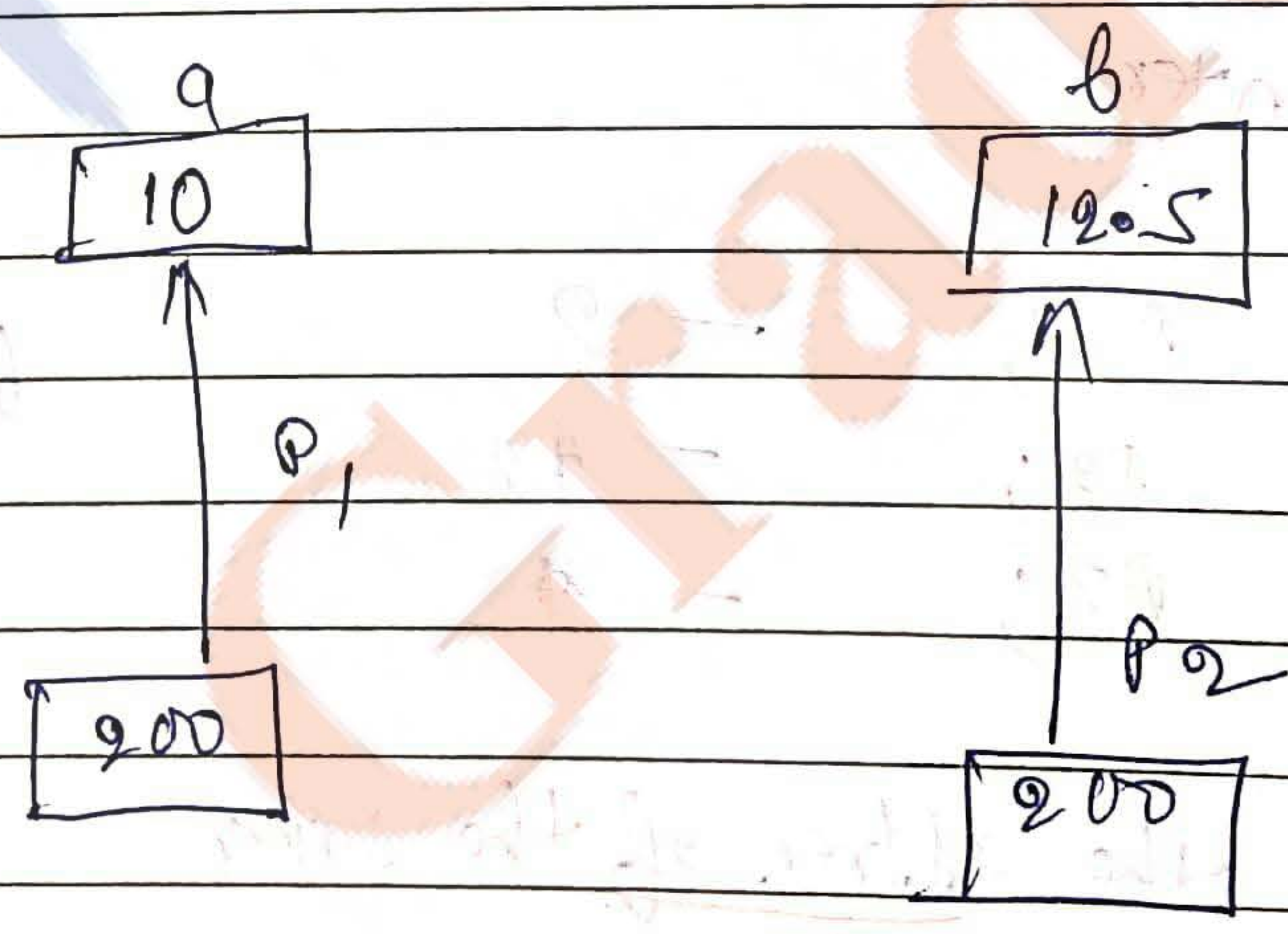
```

    > int a = 10;
      int * p1;
      p1 = &a;

      float b = 12.5;
      float * p2;
      p2 = &b;
  
```

~~p1 = &b;~~

- A pointer of one type can store the address of data of same type only.

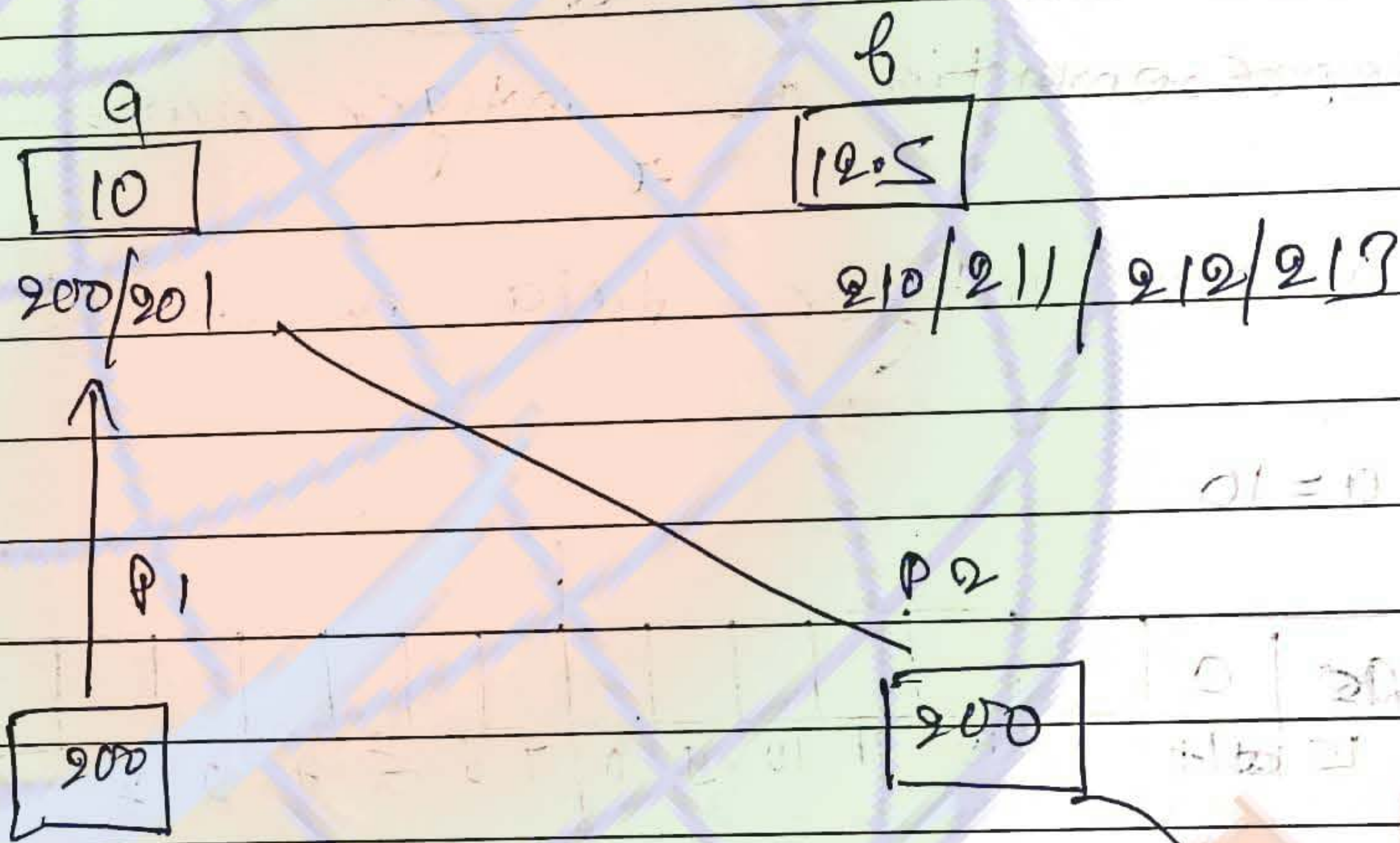


De-referencing :-

when the pointer is reference, it will access the data depending on data type of pointer.
 so, - integer pointer will access two bytes
 and - float pointer will access four bytes.

Here

P_2 is float, but accessing a.

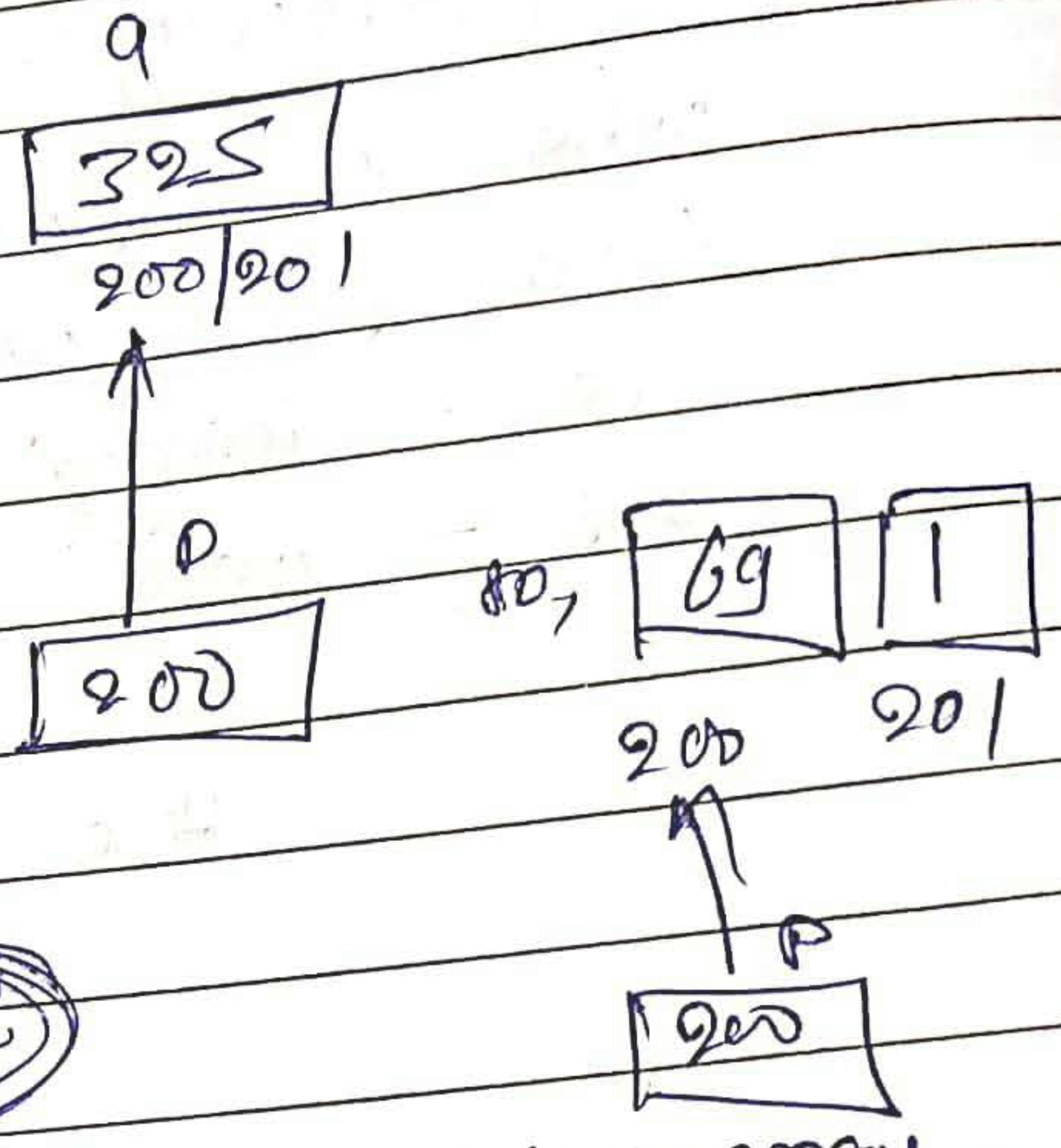


```
P2 = &a;  
printf ("%f", *P2);
```

Note: this is trying to access four bytes from **a**, but on **a** only two bytes are present. so it's not show true error.

```

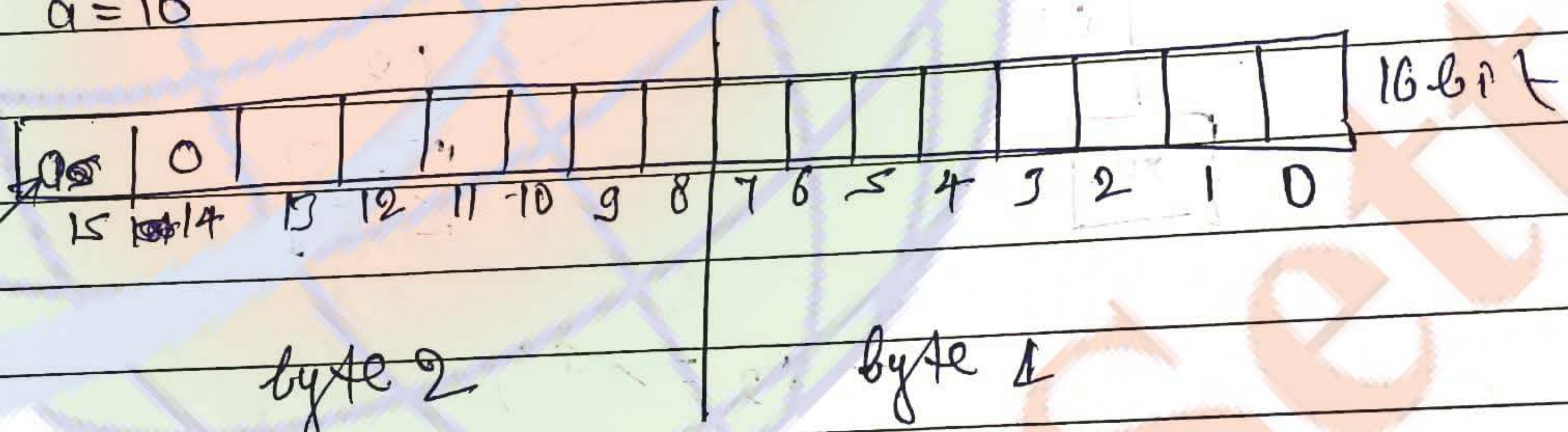
int a = 325;
char *p;
p = &a;
printf("%c", *p);
    
```



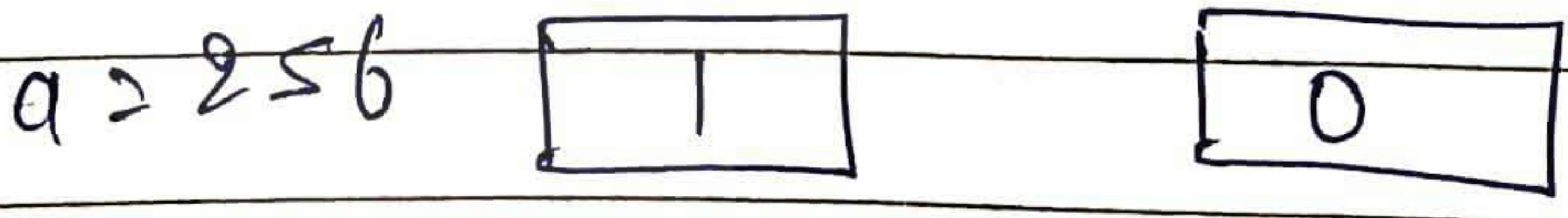
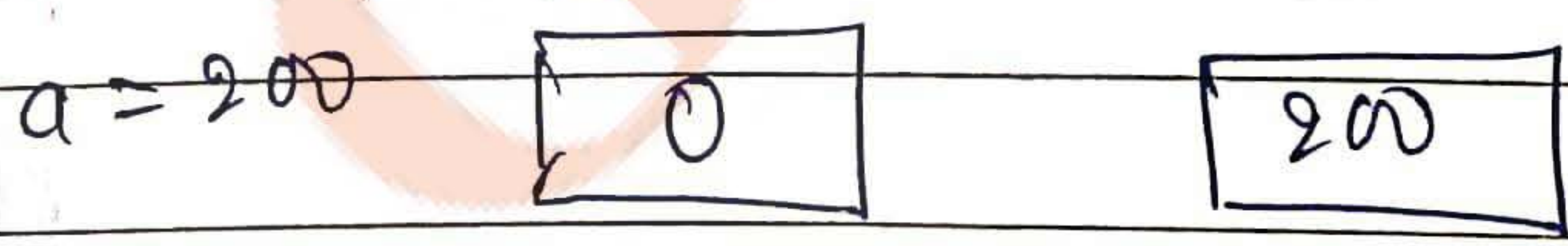
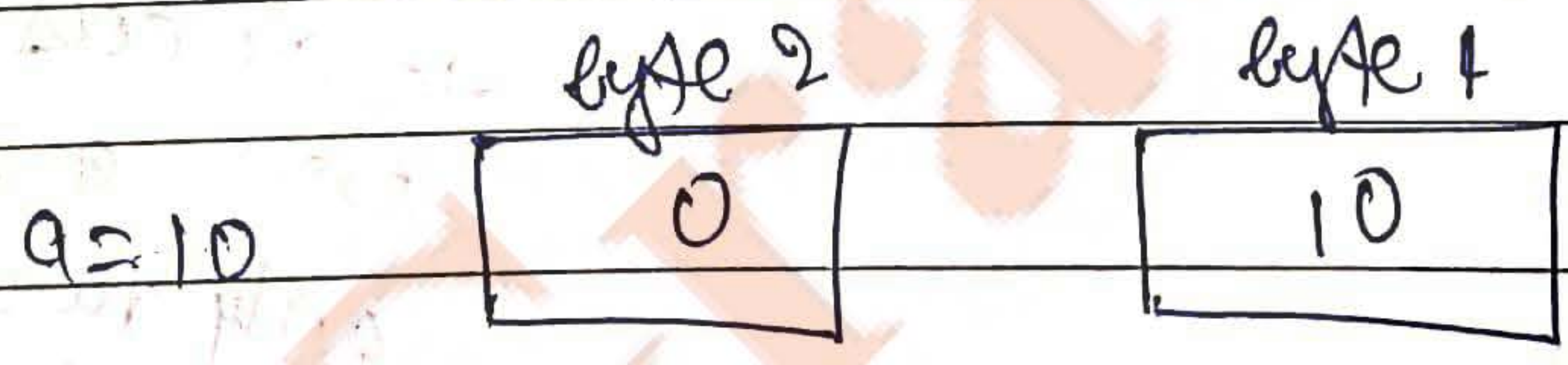
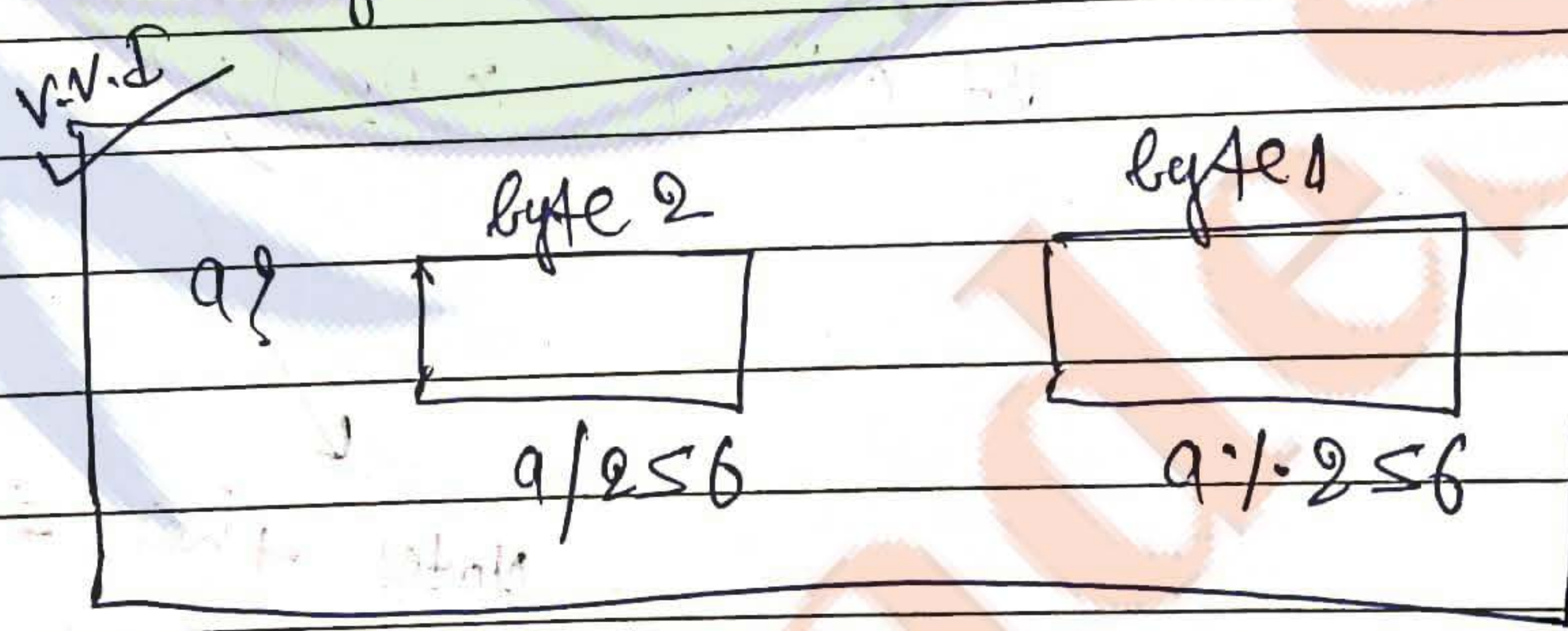
Representation of integer data into memory

How to integer data is stored in memory?

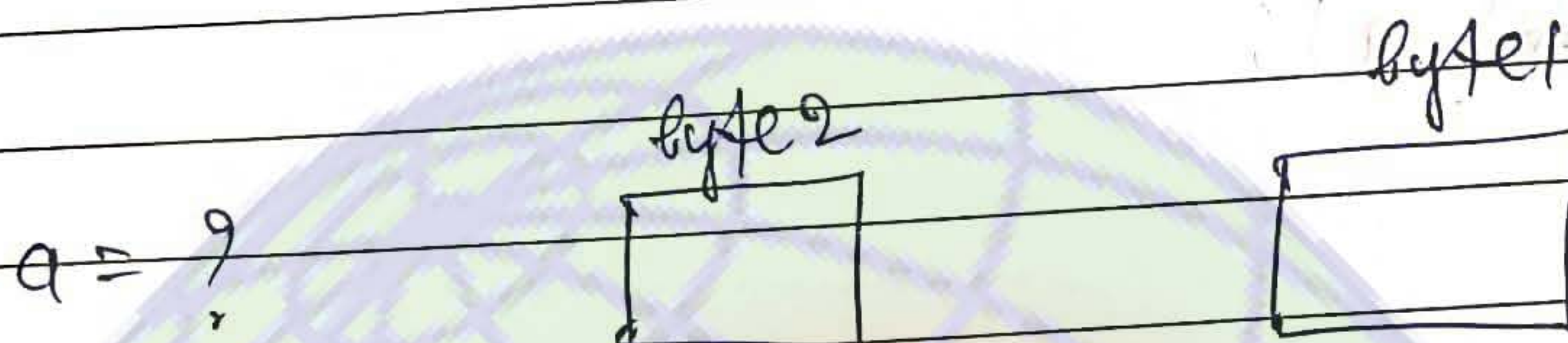
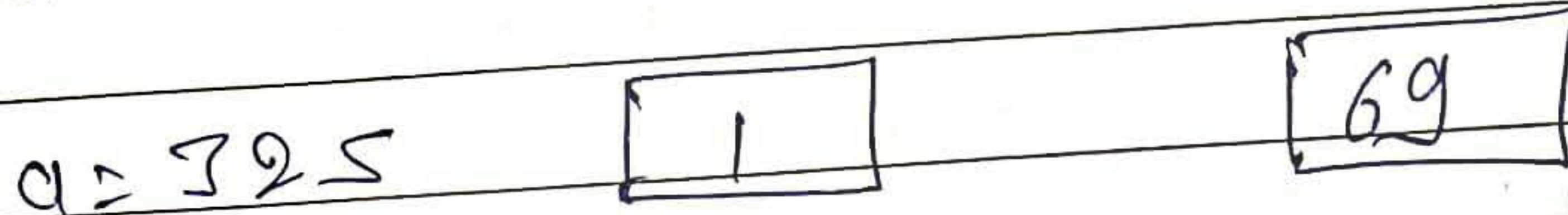
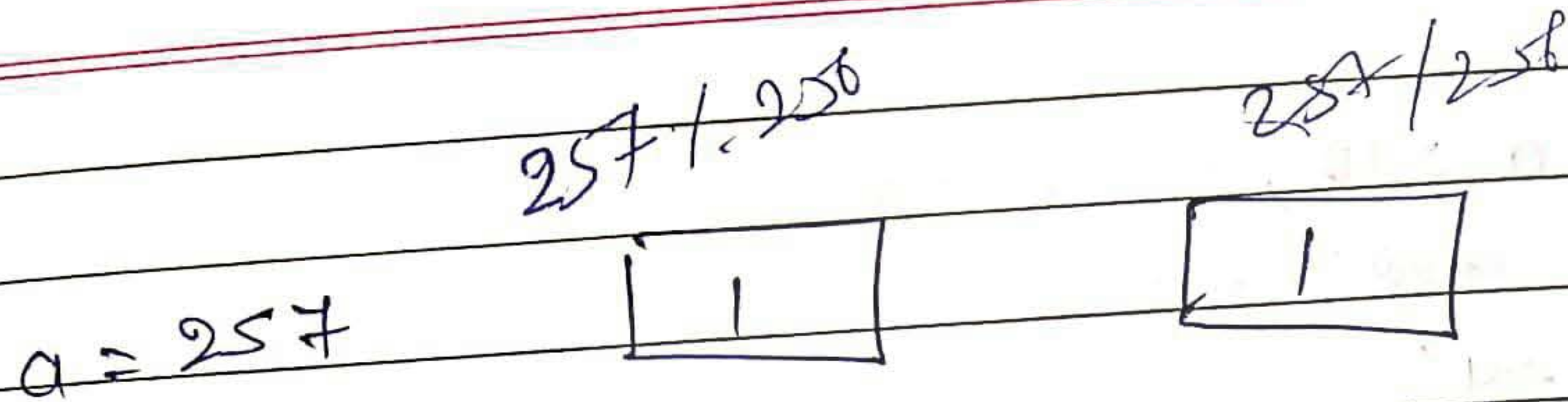
a = 10



Note:
C, C++ using signed int
convert for -ve number
Java, C# using int
is compact for -ve number.



00000000 | 00000000



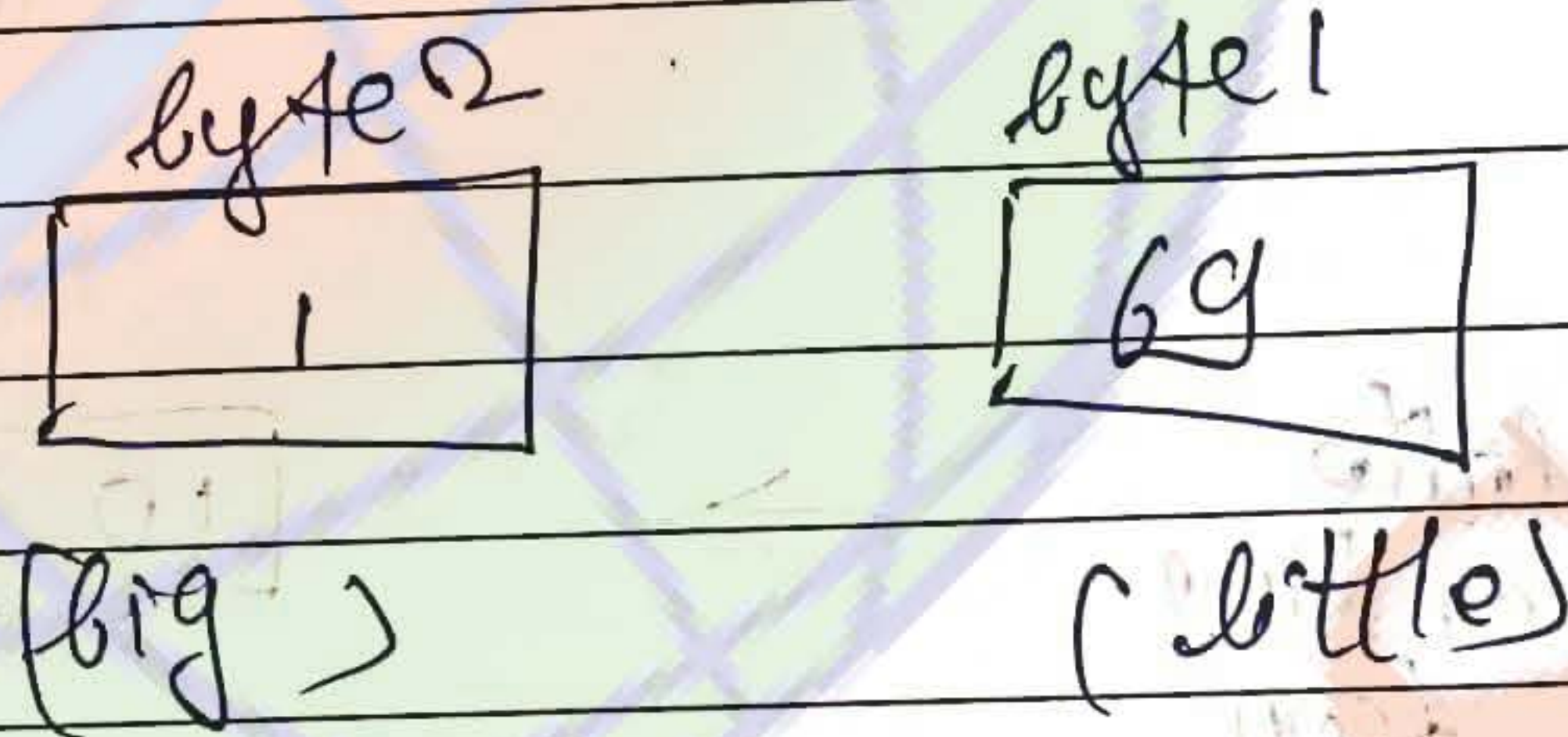
only paper work (on paper)

$a / 256$ (divide) $a \% 256$ (mod)



~~$a = 325$~~

$a = 325$

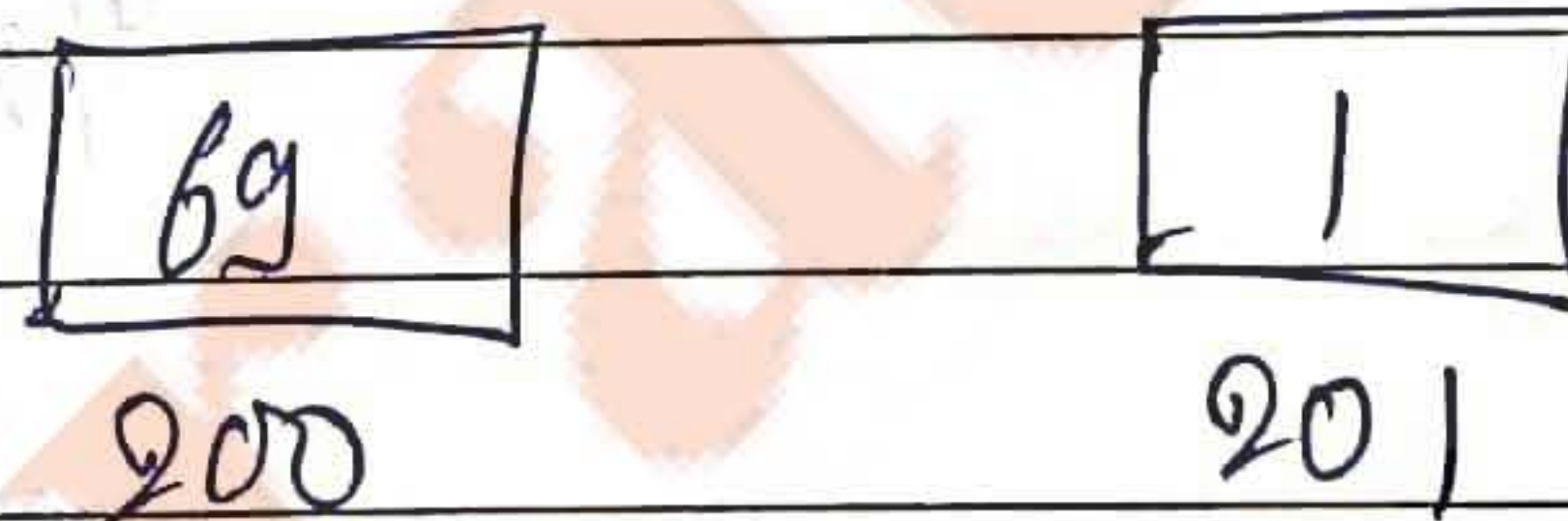


So, we are using two methods to store in the memory.

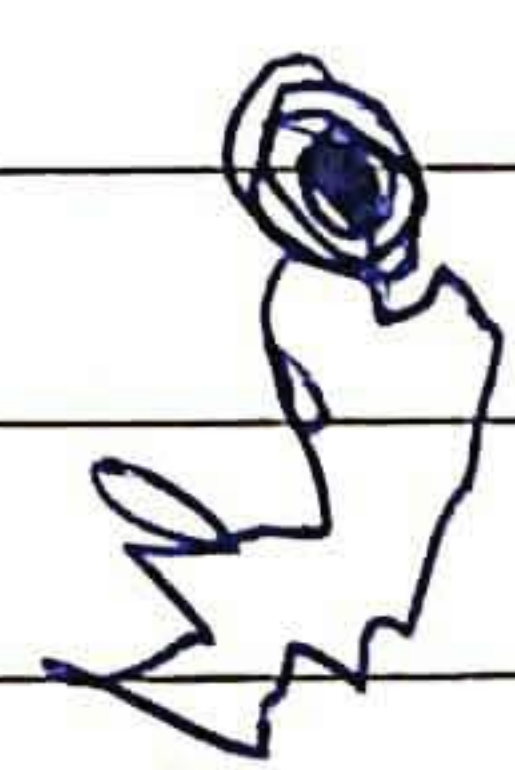
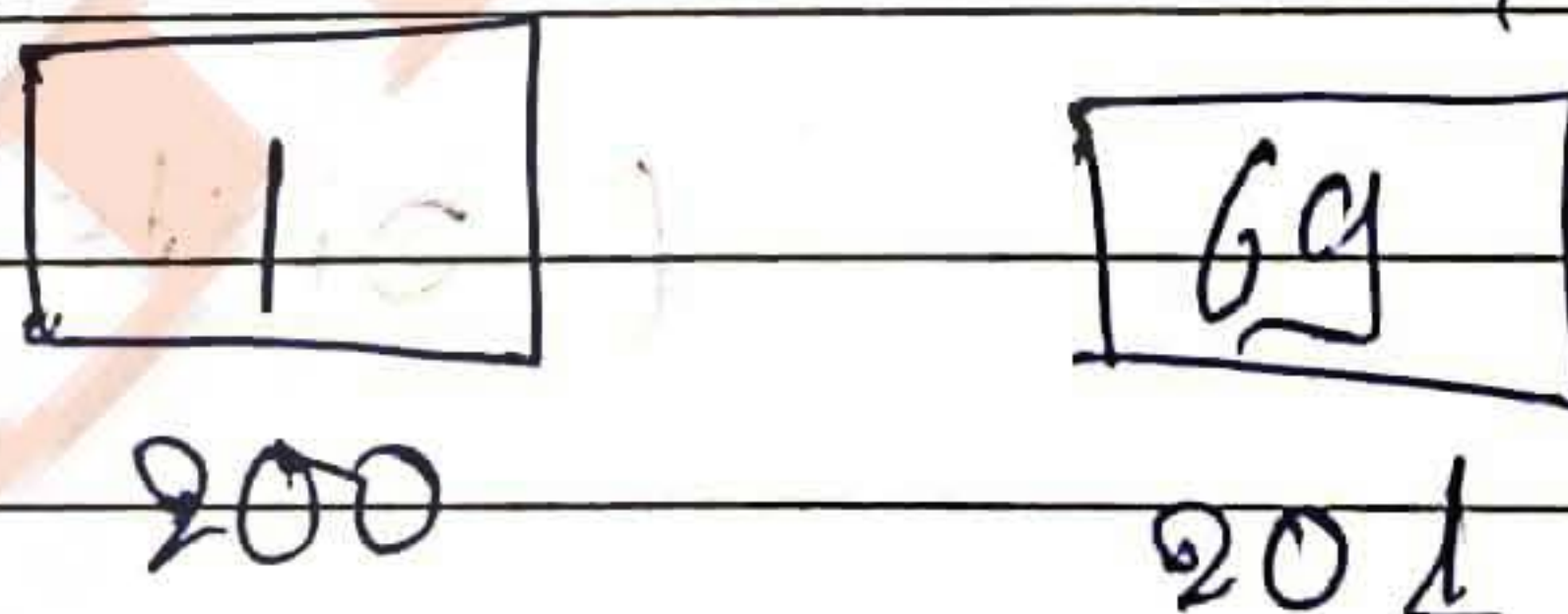
generally used

little

endian



big endian



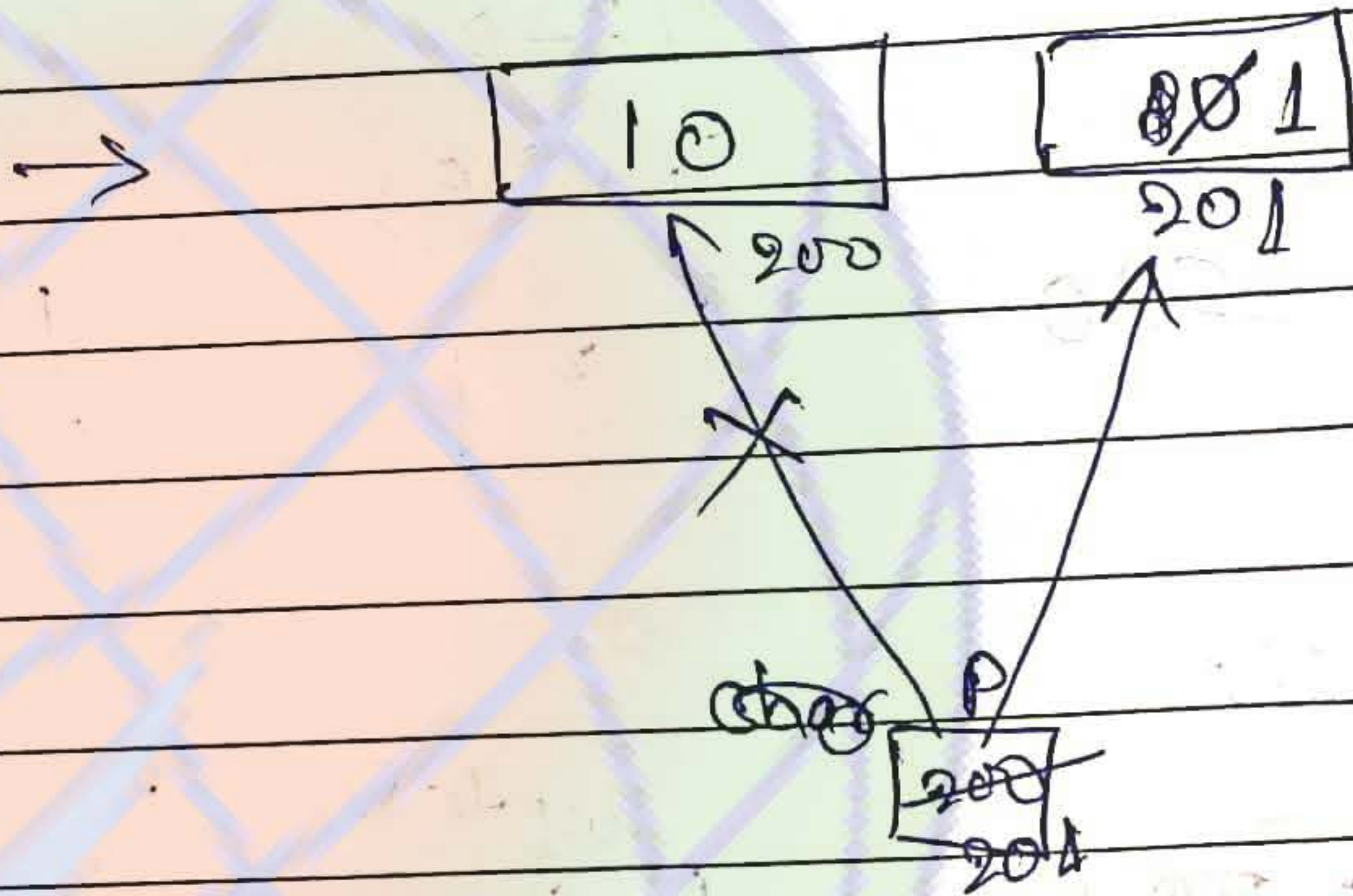
```

eg) int a = 10;
    char *p;
    p = &a;
    p++;
    (*p)++;
    printf("%d", a);

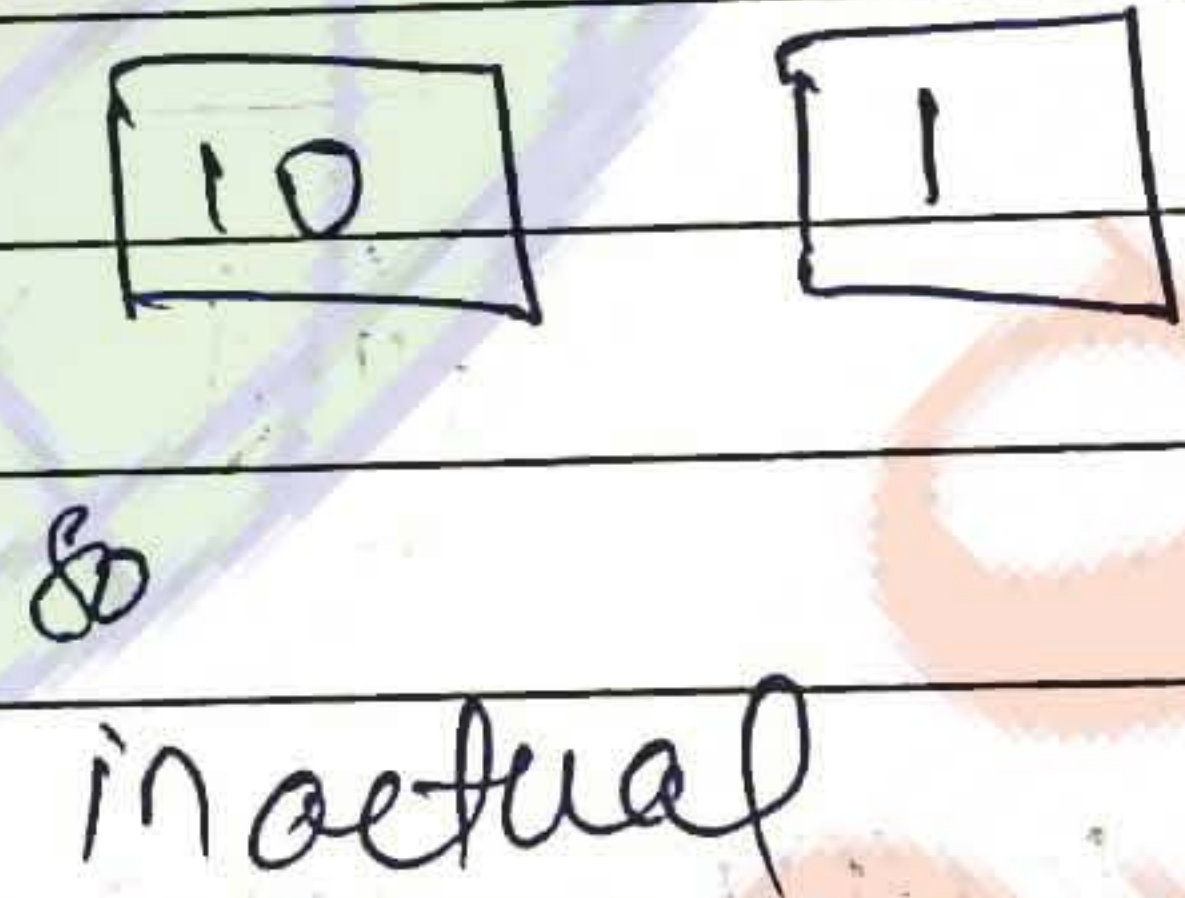
```

8421
1010

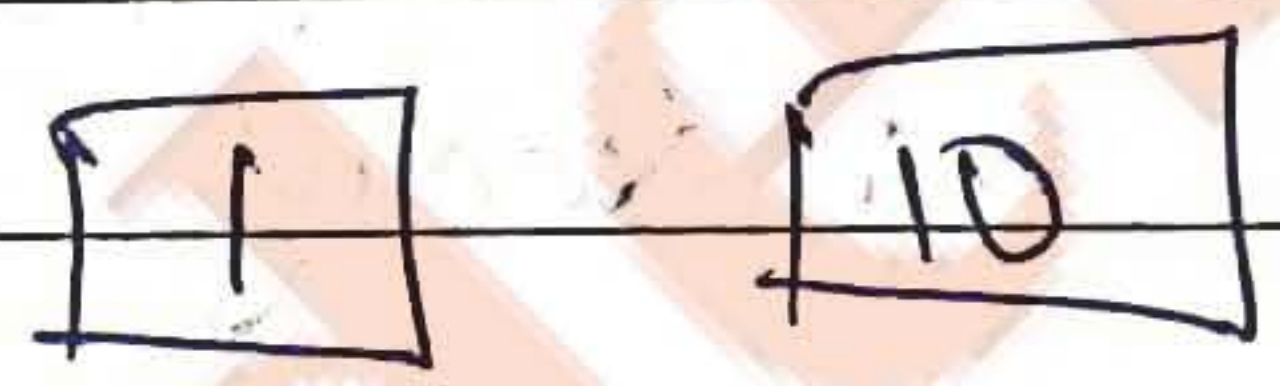
little
endian
form



little
endian
form



&
in actual



9/256 9/256

$1 \times 256 + 10 = 266$ Ans

(value ko multiply kare, uske ko sum kare)

6) Pointer arithmetic :-

(a) Pointer to an array :-

```
int A[5] = {2, 6, 8, 10, 12};
```

```
int *P;
```

```
P = A;
```

```
printf("%d", P[2]); - 8
```

A[2] — 8

9[A] — 8

*P — 2

*A — 2

P — 200

P+2 — 204

~~*P~~
*(P+2) — 8

	0	1	2	3	4
A	2	6	8	10	12

200/1 2/3 4/5 6/7 8/9



Note

P = A;
P = &A[0]; } same

→ All arithmetic operations are not allowed on pointers

1. > P++ : moving to next element

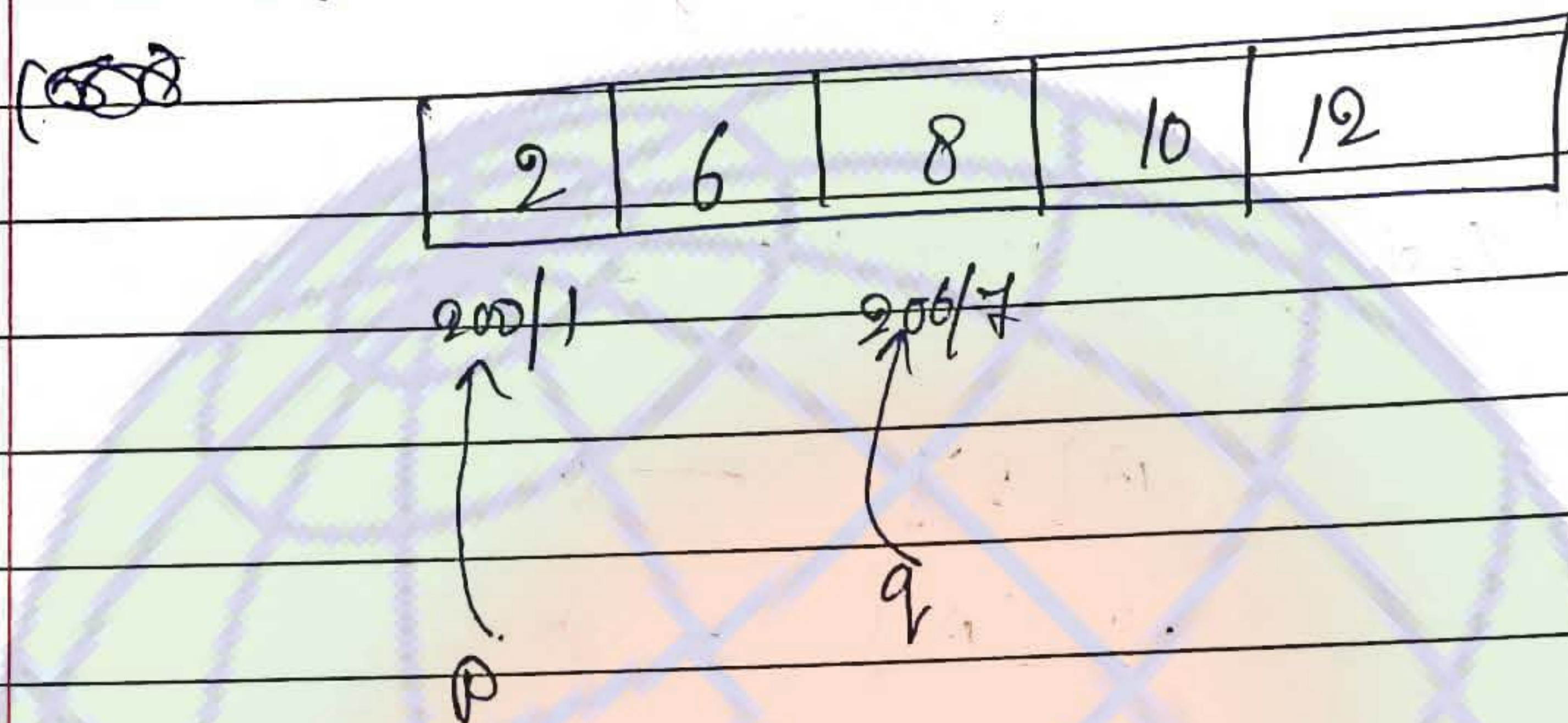
eg. if int = 2 byte increment
float = 4 byte increment

2. > P-- : moving to previous element

3. > P+3 : moving to three element away/ give address of element 3 location away

4. > P-3 : moving to three element previous, away in forward or backward direction
gives address of element 3 location away in backward direction

```
int A[5] = {
    int *p, *q;
    p = A;
    q = &A[0];
```



(S) $d = q - p$

(3) distance

↳ Indicate no. of elements

$$\begin{matrix} 200 \\ \uparrow \\ p \end{matrix} - \begin{matrix} 206 \\ \uparrow \\ q \end{matrix} = \frac{206 - 200}{2} = \frac{6}{2} = 3 \text{ (elements)}$$

Note:

only address operation allowed in pointers

~~(+)~~ $p + q$

~~(*)~~ $p * q$

~~(/)~~ p / q

(+) Note:

*P → dereferencing ✓

P++ → pointer increment ✓

(10) ^① *++P ;

← right to left

*(++P) — 6

⇒ ++*P ; — 7
←

(data increment) ++(*P) → increment the data where P is pointing. ✓

"take the data and increment the data"

most commonly used

① *P++ ;
② *P++ ;

a) *P — take the data } precedence of ++ is higher
b) P++ ; — and } post increment is higher
more the pointer.

↓
data of array, the pointer increment.

(take the data and move pointer)

eg. int A[5] = {2, 6, 8, 10, 12};

int *P, *q;

{ P = A;
*P = &A[0];

for (i=0; i<5; i++)
{


```

    printf("%d", *p); } or printf("%d", *p++)
    p++;
}

```

but print all element
and pointer will be after last element.

or

Note:

```

for (i=0; i<5; i++)

```

```

{
    printf("%d", *(p+i)); or *p p[i]
}

```

$\therefore *(p+i) \rightarrow p[i]$

print all element
and
pointer will remains on base address.

(8) why pointer's have datatype

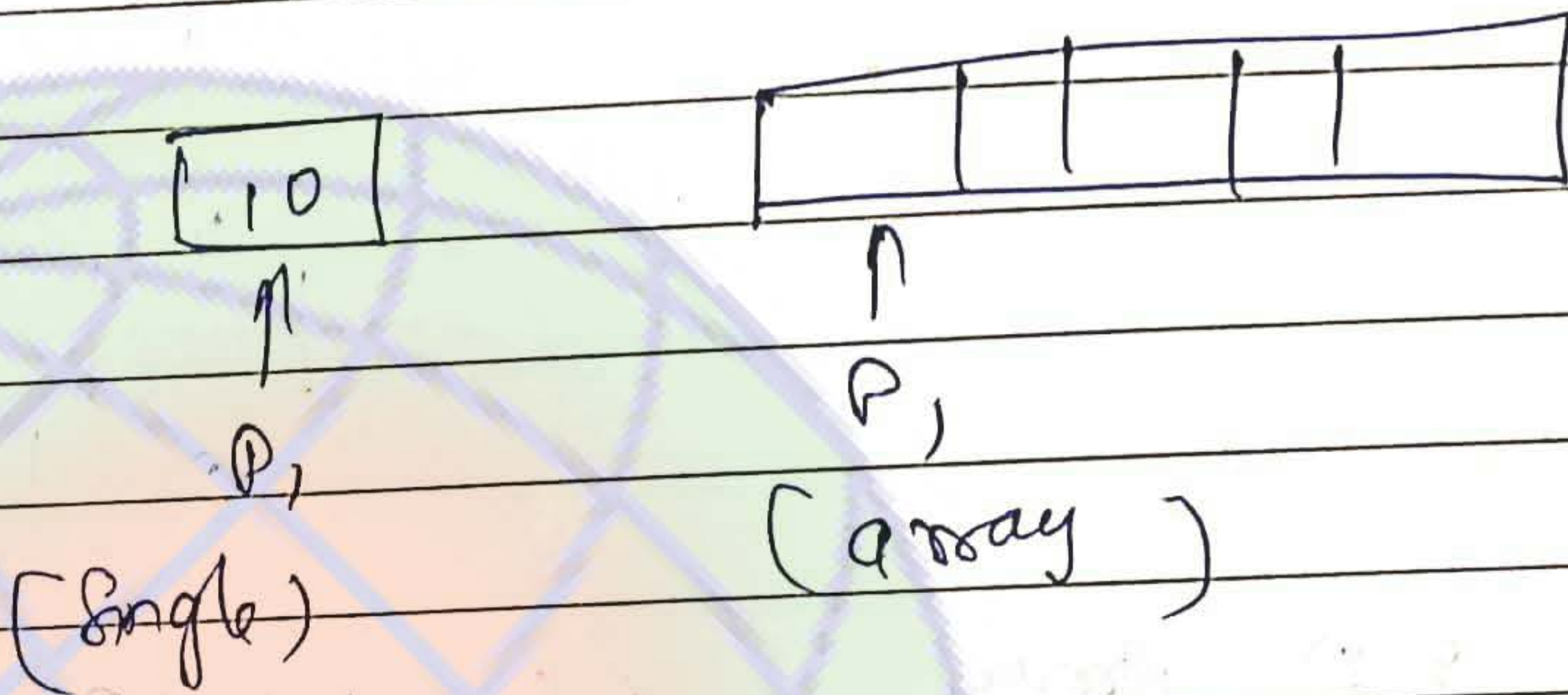
Ans Reasons so pointer have data types:-

(i) dereferencing

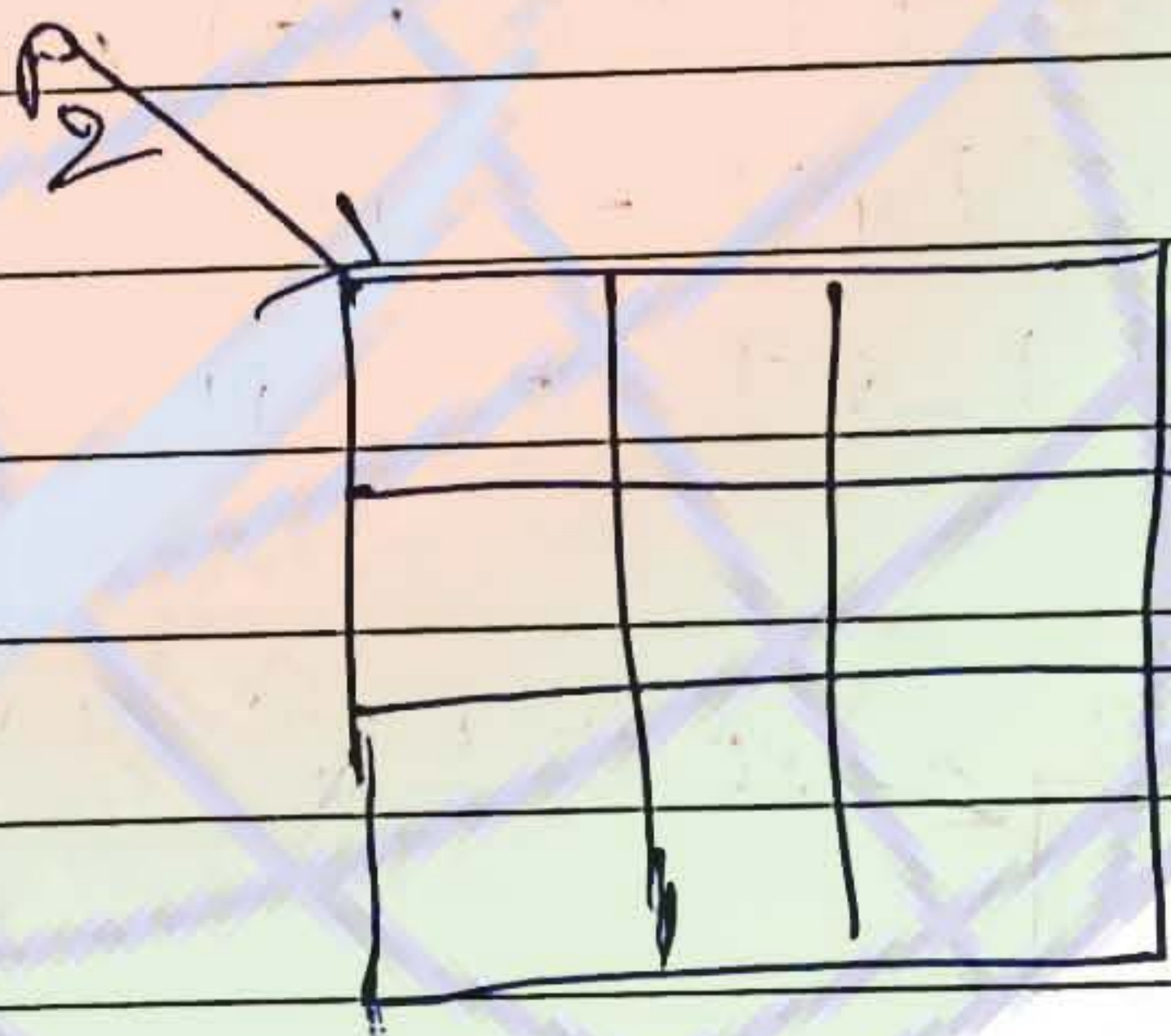
(ii) - pointer arithmetic

Double pointer:-

① `int *P1;` — single pointer



`int **P2;` — double pointer.



2D elements

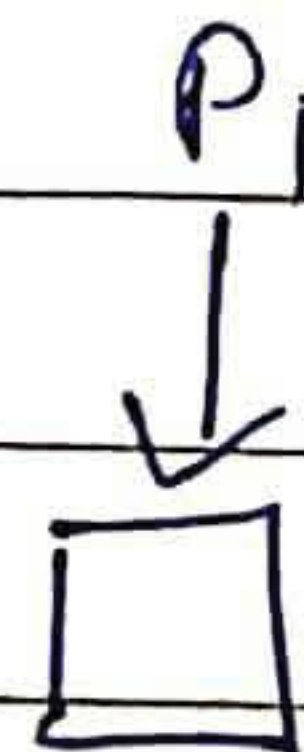
~~single int~~ `int a;` — in stack ✓

`int A[5];` — in stack ✓

`int A[3][4]` — in stack ✓

new
single int

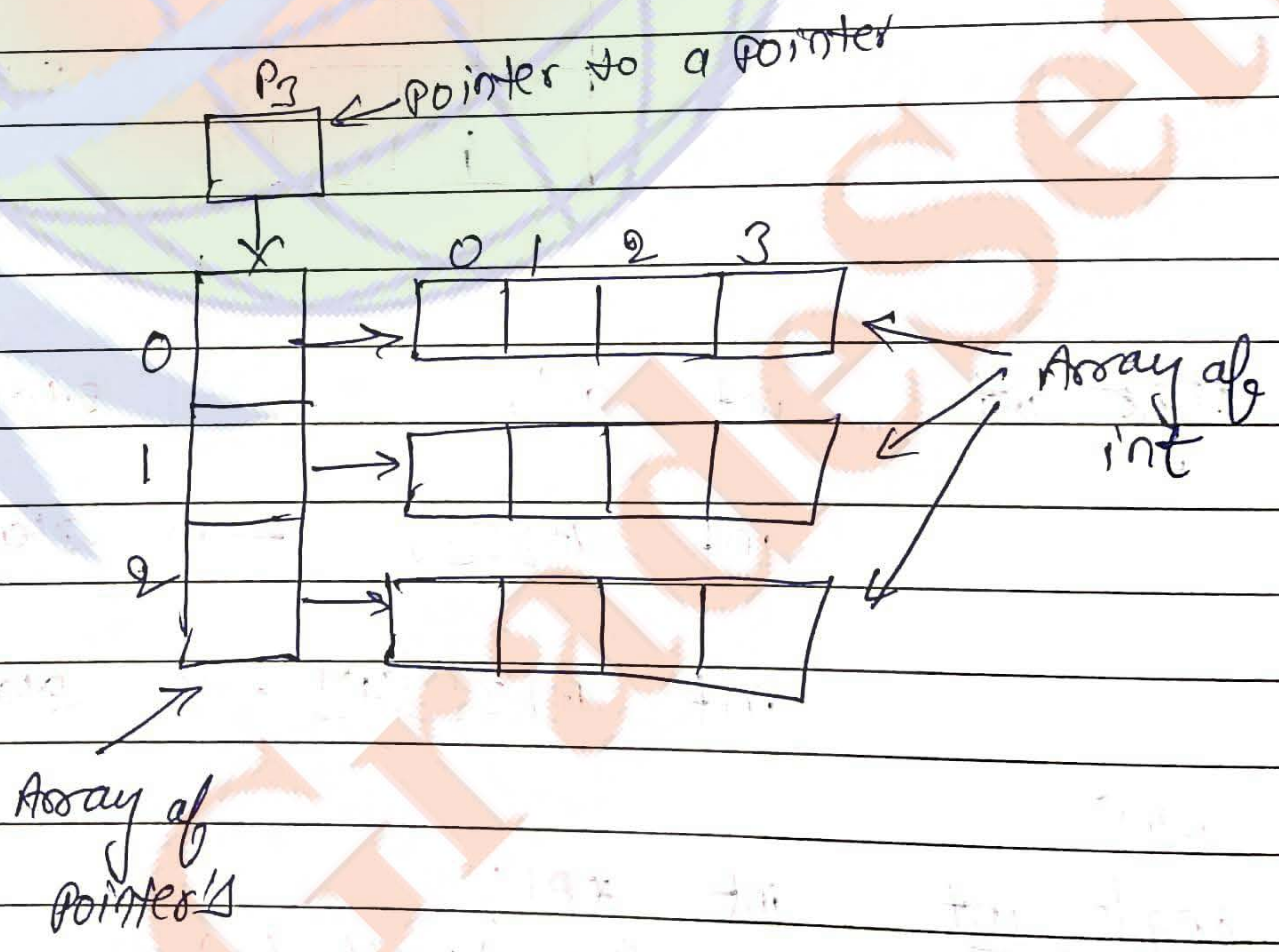
`int *P1;`
`P1 = (int *) malloc(2);`



Array of int int * P2;
P2 = (int *) malloc(10);



2D Array int ** P3;
3x4 P3 = (int **) malloc(3*2);
P3[0] = (int *) malloc(4*2);
P3[1] = //
P3[2] = //



```
main()
{
    int n;
    cout << "what is array size";
    cin >> n;
```

→ stack में array fixed होता है।

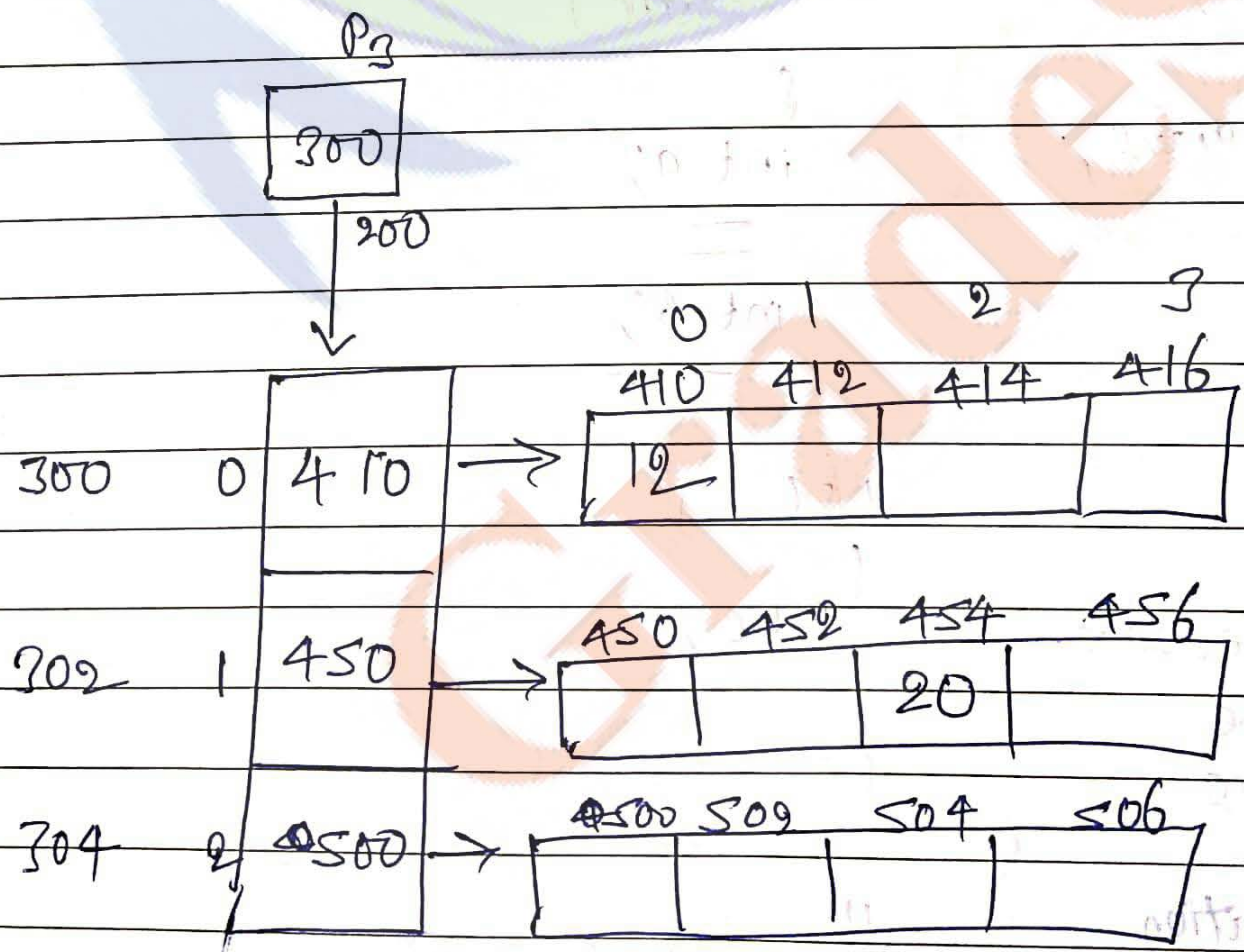
```
X int A[n]; X (not allowed)
```

```
✓ int *B = new int[n]; ← heap में new की जाती है।
```

Note

stack में array का size = static है ✓
heap में " " " " = dynamic है ✓

②



$a = 10$
 $*a = 200$
 $p = 200$
 $*p = 200$
 $**p = 200$

9
 10 classmate
 Date _____
 Page _____
 200
 200

printf ("y.d", p); - 300
 " " *p - 200
 " " **p - 410
 **p - 12

(double pointer)

$\&p[0] \rightarrow p+1 - 302$
 $p[0] \rightarrow *(p+1) - 450$
 $\&p[0][2] \rightarrow *(p+1) + 2 - 454$
 $p[0][2] \rightarrow (*(p+1) + 2) - 20$

Note

C-language

C++ language

```

main()
{
  int a, b, c;
  ==
  ==
}
  
```

```

main()
{
  int a;
  ==
  int b;
  ==
}
  
```

Here, all the variable
 should be
 declared once

so, the activation
 record is static.

```

f()
{
  int c;
}
  
```

you may declare at any time

the activation record

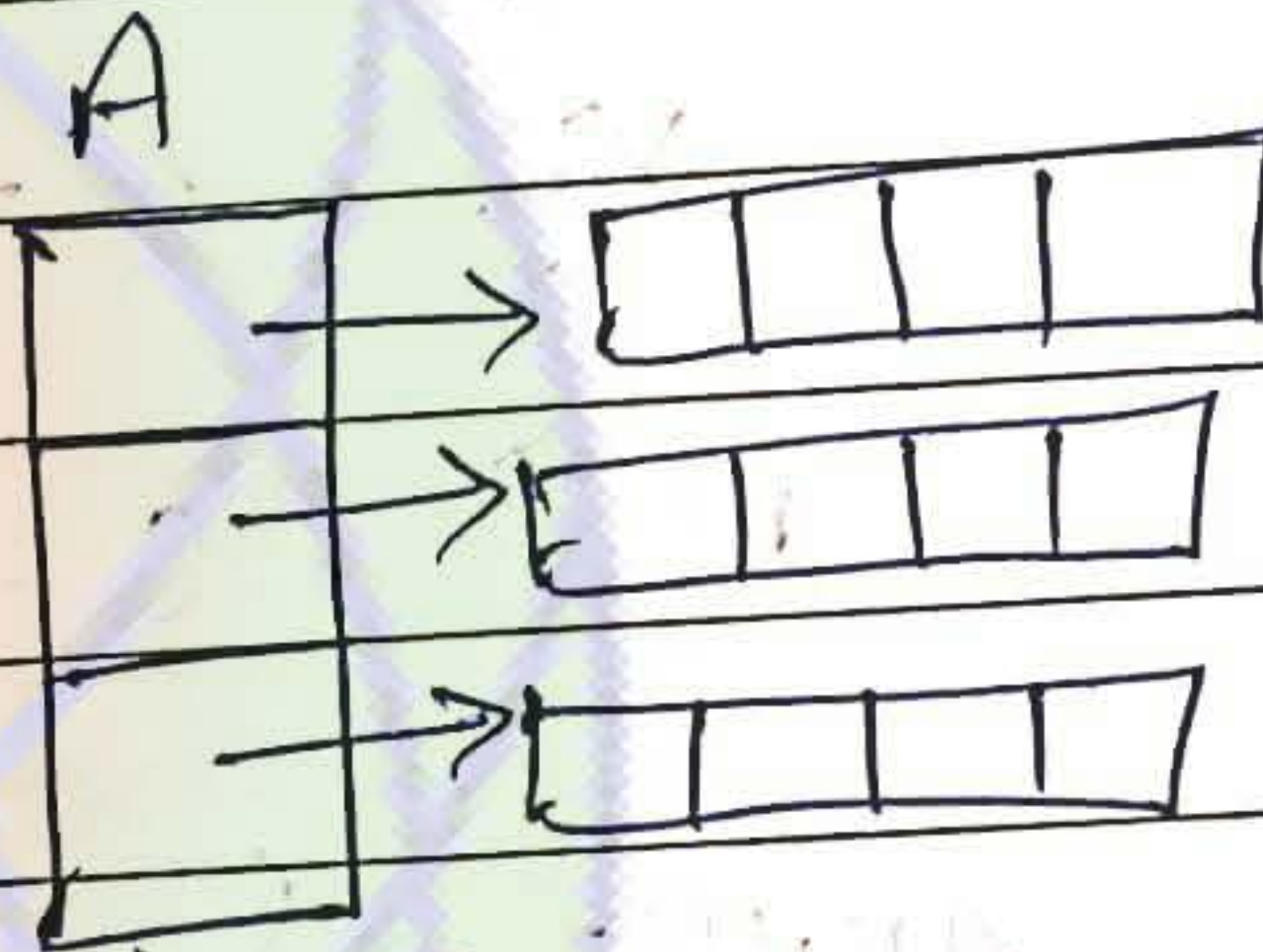
③ methods of declaring 2D array

1. > int A[3][4];



both row & column are static
A[i][j] = r;
(left side)

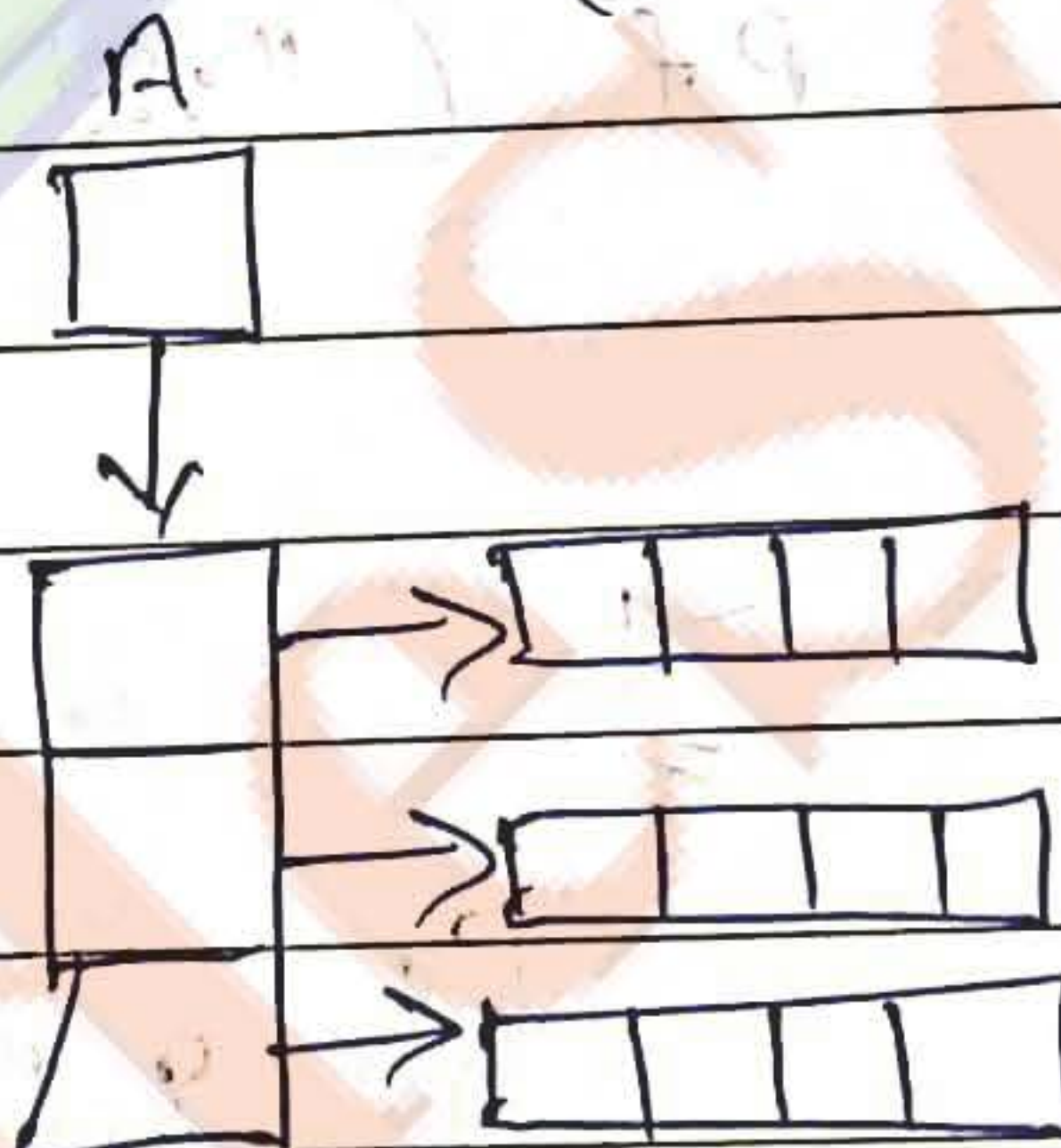
2. > int *A[3];
A[0] = new int[4];
A[1] = "
A[2] = "



rows are static.
size of rows are dynamic.

3. > int **A;
row → A = new int*[3];
A[0] = new int[4];
A[1] = "
A[2] = "

rows & column



both row & column are dynamic.

A[i][j] = r;
A = q;
(left side)

Note:
x = 10 (write)
y = x (read)

A[i][j] = r;
A[i] = k;
A = q;
(left side)

a. > which are allowed or which are not allowed on the left side of assignment

- 1. > int *A[5];
- 2. > int B[2][4];
- 3. > int **C;

- ~~X~~ a. B[C]
- ✓ b. C[C]
- ✓ c. A[C]
- ✓ d. A[C][C]
- ✓ e. C[C][C]

- ~~X~~ f. B
- ✓ g. C
- ~~X~~ h. A
- ✓ i. A = B;
- ~~X~~ j. B = A;
- ✓ k. C = B

only see
left
side

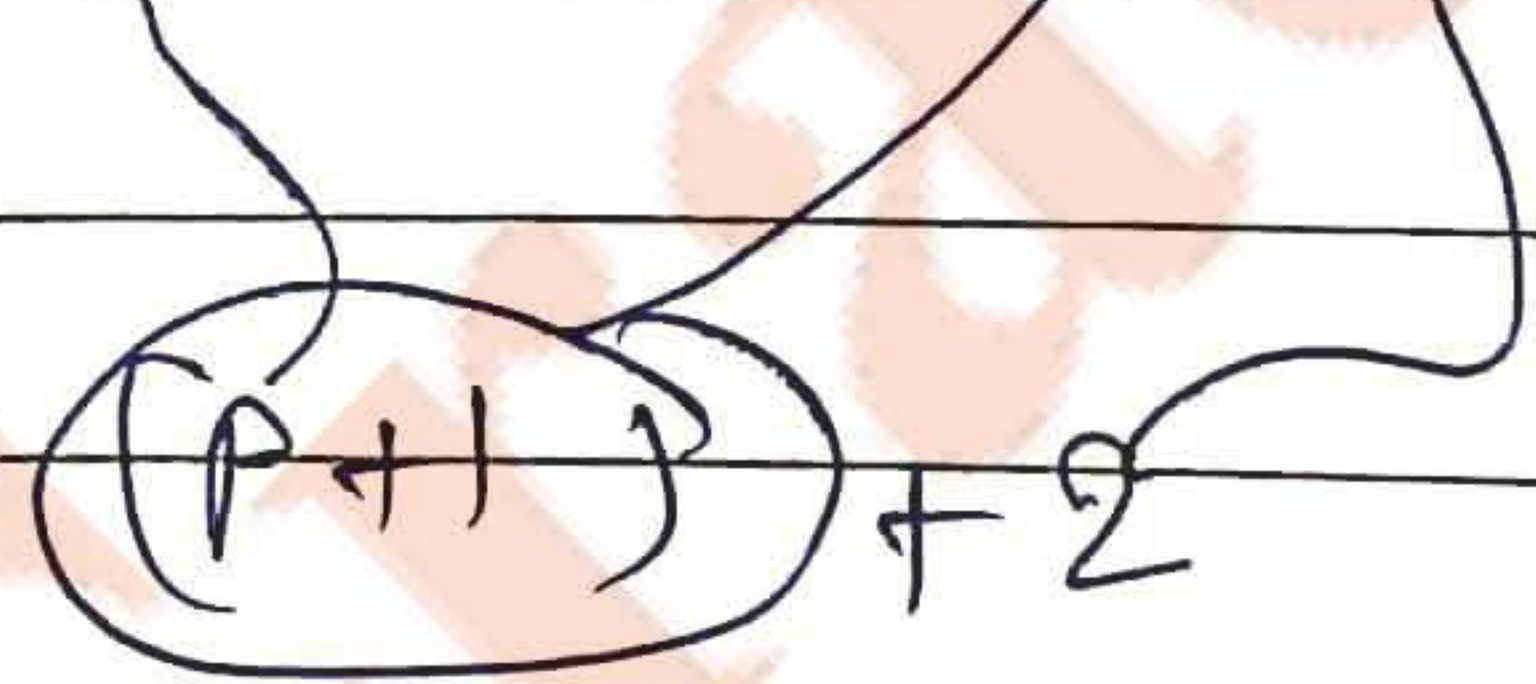
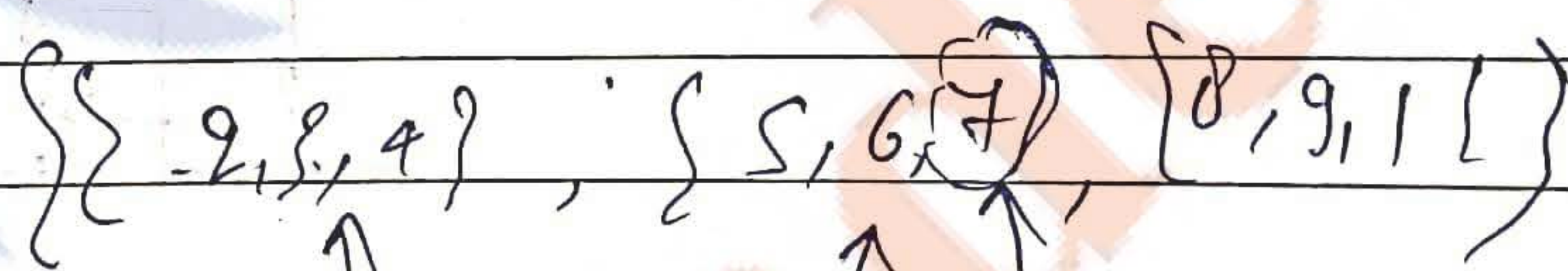
```
eg. int A[C][C] = { {2,3,4}, {5,6,7}, {8,9,1} };
```

```
int *p[S] = A;
```

```
printf ("%d", *( *(p+1)+2));
```

Ans

≠



	0	1	2
0	2	3	4
1	5	6	7
2	8	9	1

∴ $*(*(p+1)+2) = A[1][2]$

1 2

gate
Q. >

```
int a1[] = {6, 7, 8, 10, 34, 67};
```

```
int a2[] = {29, 56, 28, 29};
```

```
int a3[] = {-12, 24, -31};
```

```
int *x[] = {a1, a2, a3};
```

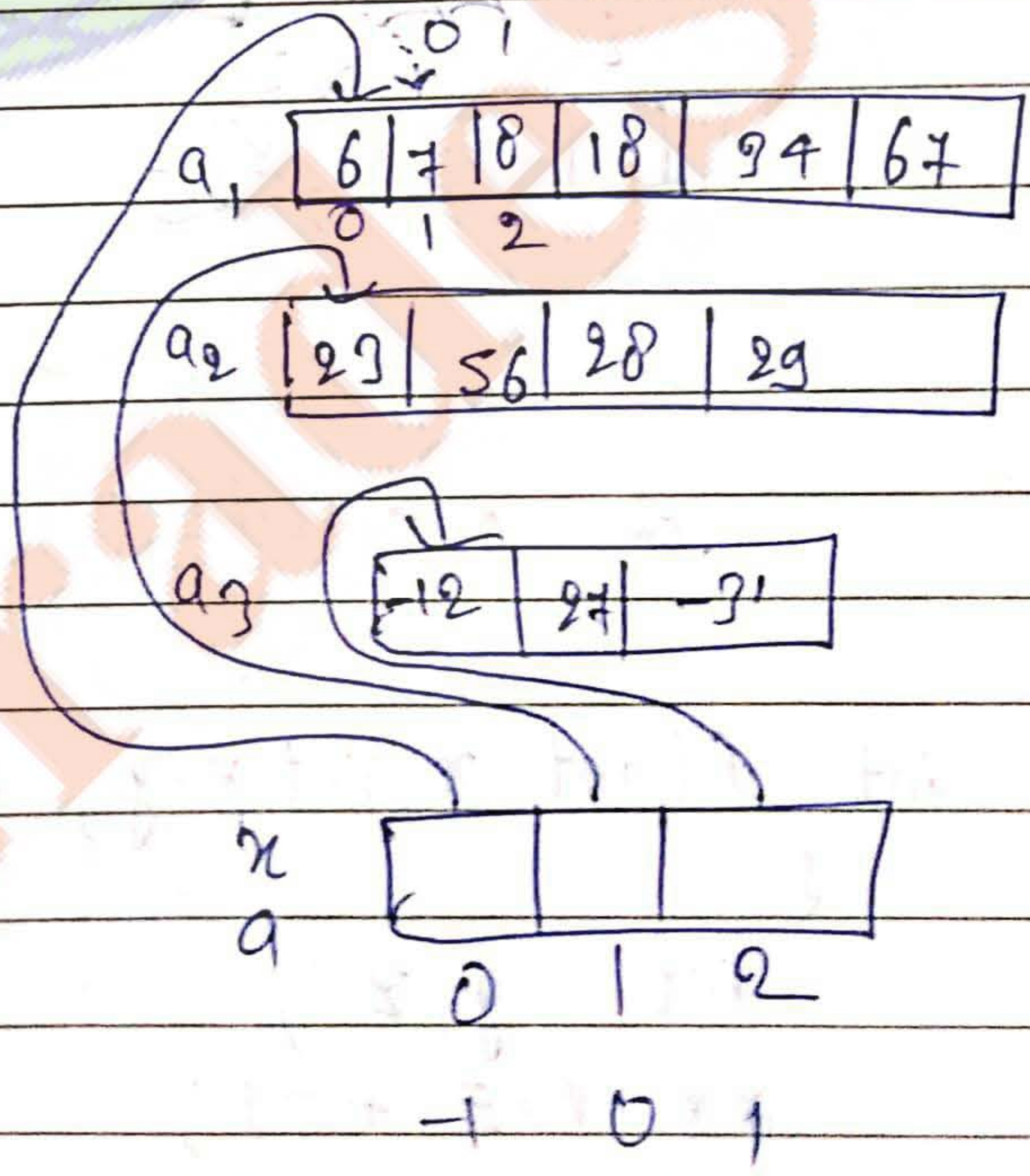
```
void print (int **a[])
{
    printf (a[0][2]);
    printf (*a[2]);
    printf (*++a[0]);
    printf (*(++a)[0]);
    printf (a[-1][+1]);
}

main()
{
    print(x);
}
```

Ans

Q. 8, -12, 7, 29, 8

A.

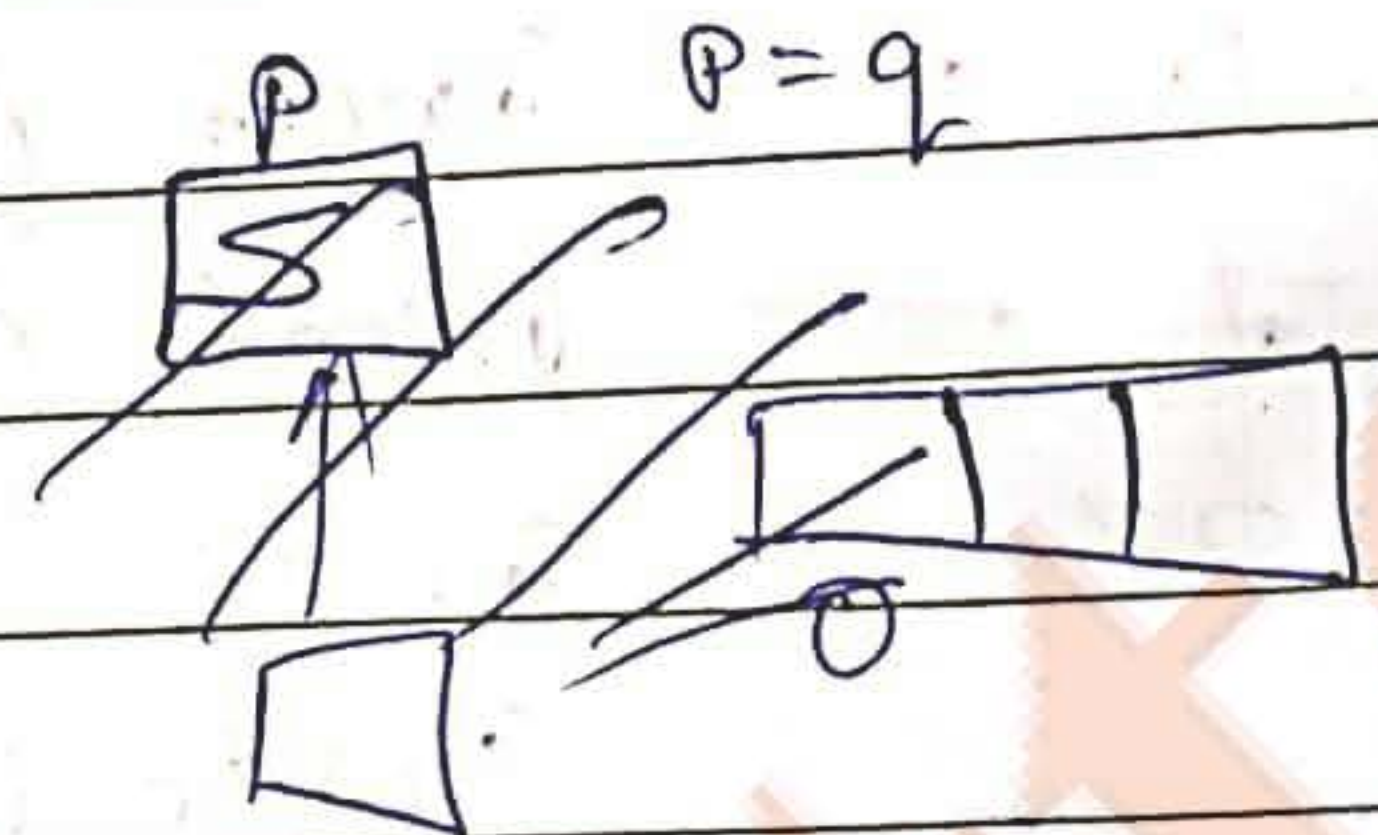
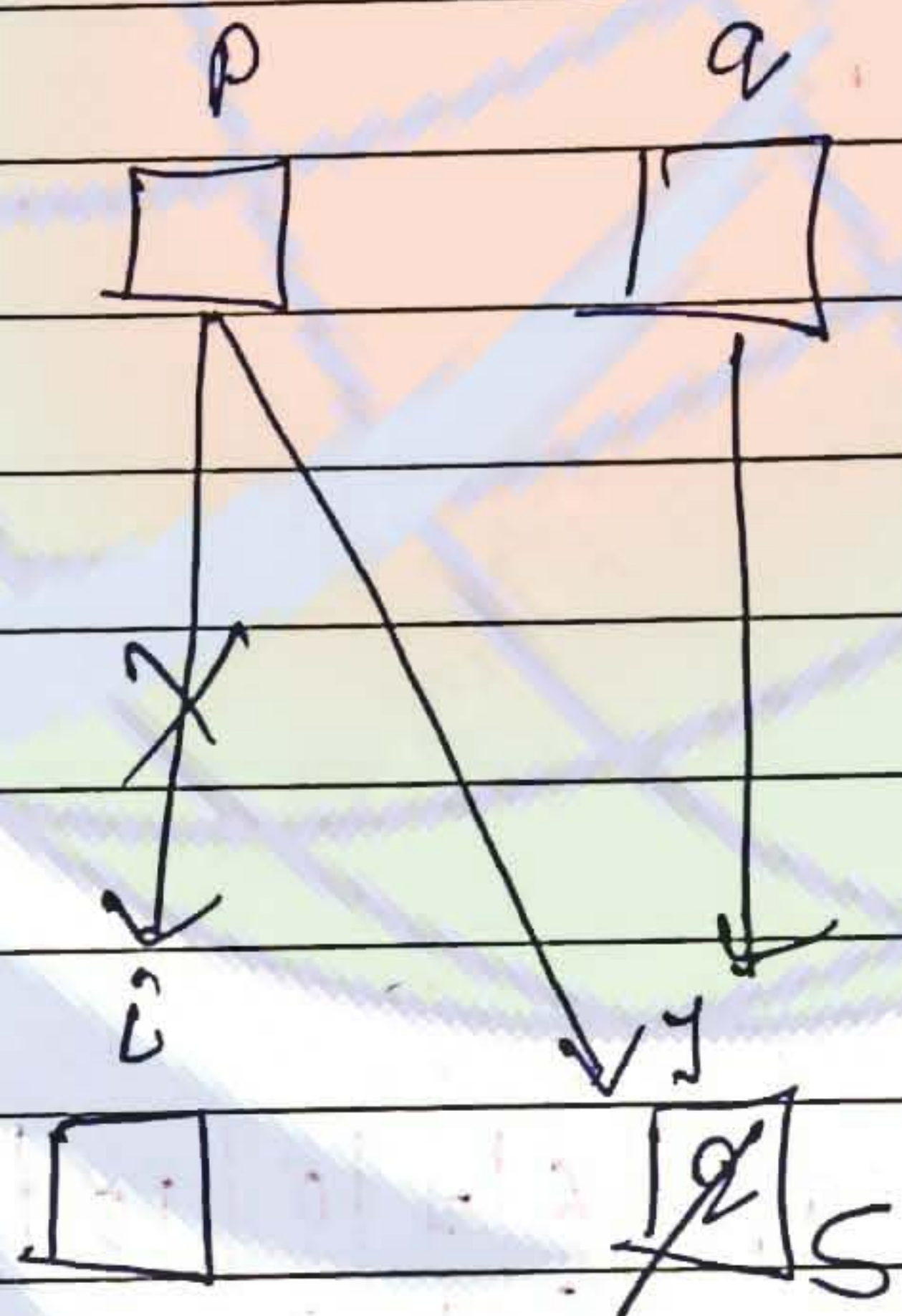


gate
eg 9)

```

main()
int i=0, j=2;
f(&i, &j);
Pf(i, j);
    f(int *p, int *q)
    {
        P=q;
        *P=S;
    }
    main()
    {
        int i=0, j=2;
        f(&i, &j);
        Pf(i, j);
    }
    
```

soln



ans 0, 5, An

gate
eg 10)

```

int f(int x, int *py, int **ppz)
{
    int y, z;
    **ppz += 1;
    z = **ppz;
}
    
```

```

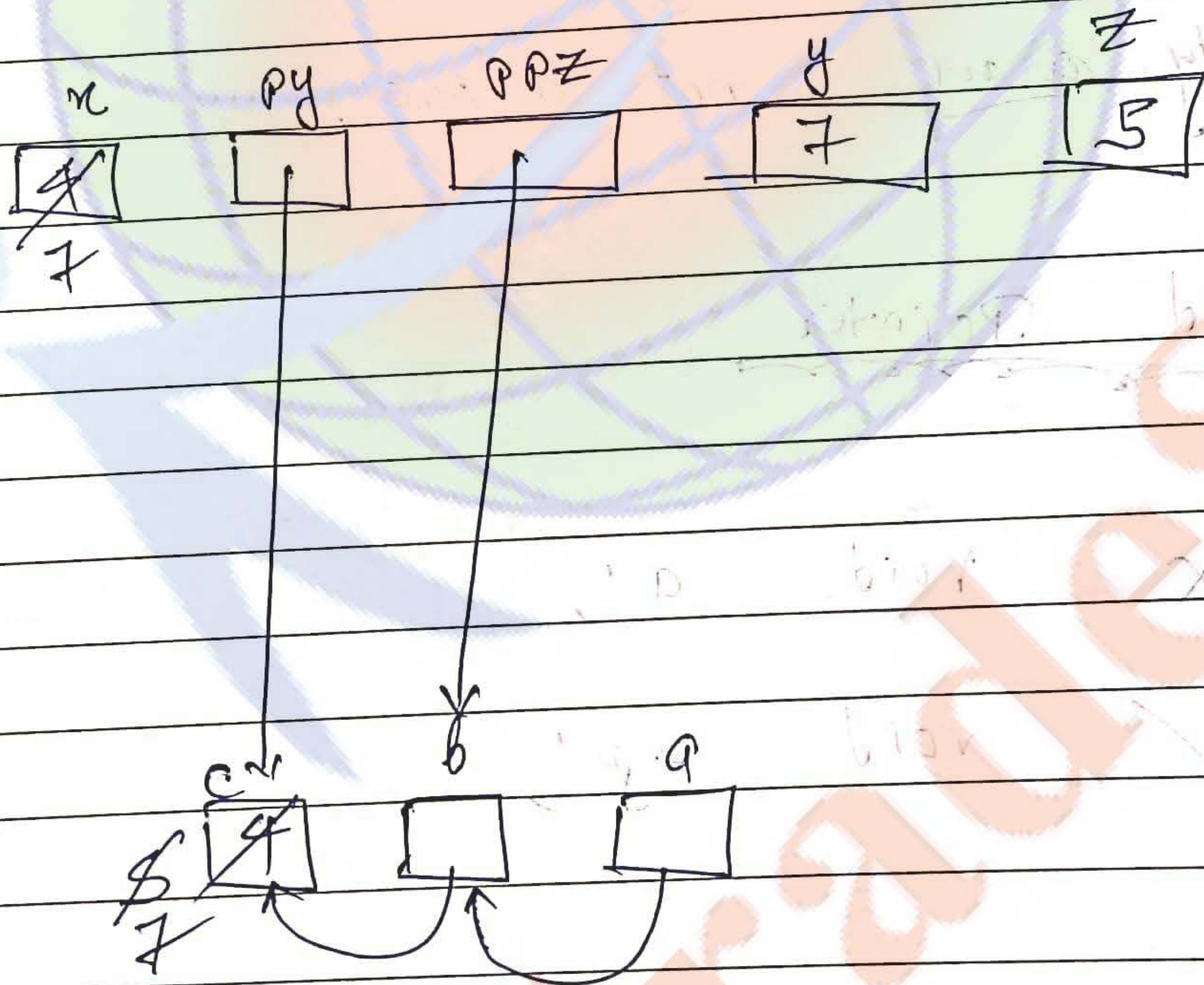
* py += 2;
y = *py;
x += 5;
return x+y+z;
}

```

```

void main()
{
int c, *b, **a;
c=4; b=&c; c=&b;
pf(f(c, b, a));
}

```



Ans $5 + 7 + 7 = 19$

$z + b + x = 5 + 7 + 7 = 19$

$P = \&n;$
 $P = \&y;$
 $P = \&z;$

- void pointer can not be de-references.

~~\times $\&f(\&p);$~~

- pointer arithmetic is not allowed on void pointer.

- void ~~$\&$~~ malloc (int size)
 int ~~$\&$~~ $\&p;$
 $p = (\text{int } \&) \text{ malloc}(10);$

★ Pointer to a function:-

```
void display()
{
    pf("Hi");
}

main()
{
```

decl \rightarrow void ($\&f$)();

init \rightarrow $\&p = \text{display};$

func call \rightarrow ($\&p$)();

}

- Declaration of a function should be same as prototype of a function.

```
# int add (int x, int y)
{
    return x+y;
}

int max (int a, int b)
{
    return a > b ? a : b;
}
```

```
main()
{
    int (*fp) (int, int);
    fp = add;
    (*fp) (10, 5); ✓
    fp = max;
    (*fp) (10, 5);
}
```

→ A function pointer can point on all those function ~~where~~ which has same prototype.

```
# 1.) int f(int)
2.) g(int)
3.) void h( )
4.) void p(void)
```

→ by default 'int' &
→ by default 'void' & on the

```
int (*m) (int);
void (*n) (void);
```

✓ a. m = f;
~~✓ b.~~ m = h;
 ✓ c. m = g;
~~✓ d.~~ n = p;
 ✓ e. n = h;
~~✓ f.~~ n = g;

★ Declarations -

int A[S];
 Array of int *B[S]; → fine pointers

Single pointers { int *c;
 int (*c)[S];

int fun(int, int); — a function which takes two integers and returns integer.

int *fun(int); — fun which takes int as parameter and returns pointer to an integer

int (*fun)(int); — Pointer to a fun
 (Bracket is from left to right)

Note: declaration is from right to left

int **fun(float); - fun which takes float

Common Problems using pointers:-

① memory leak:-

```
#include <stdlib.h>
int *p = (int *) malloc(10);
p = null;
```

↓
memory leak

② uninitialized pointer

```
int *p;
*p = 25;
```

③ dangling pointer

```
int *p = new int[5];
int *q = p;
free(q);
```

gate
eg. →

```
int *p1() { int *p2(); }
int *p3() { }
```

```
int *p;
return p;
}
```

↓
uninitialized pointer

```
int x = 10;
return &x;
}
```

↓
dangling pointer

```
int *p = new int[5];
return p;
}
```

↓
No Problem

Q. Triplet :-

$$A = \begin{bmatrix} 2 & 4 & 6 & 8 \\ 3 & 2 & 4 & 6 \\ 5 & 3 & 2 & 4 \\ 7 & 5 & 3 & 2 \end{bmatrix}$$

4x4

nxn

$$A[i][j] = A[i-1][j-1]$$

No. of elements - n - row

$$n \rightarrow 0 \text{ to } 1$$

$$\frac{2n-1}{2}$$

0	1	2	3	4	5	6
2	4	6	8	3	5	7
row				col		

if (i <= j)

$$\text{Addr}(A[i][j]) = L_0 + \underbrace{[j-i]}_{\text{index}} * W$$

if (i > j)

$$\text{Addr}(A[i][j]) = L_0 + W + [i-j-1] * W$$

Union Test

```
{
char a;
int b;
float c;
}
```

*

discriminant = 2 bytes
takes

Free Union

Union Test t;

```
t.a = 'A';
t.b = 500;
```

// C language supports free union

Discriminant Union

Record : Test (int ch)

{

case ch = 1

char a; — (1)

case ch = 2

int b; — (2)

case ch = 3

float e; — (4)

var test(2) t;

X t.a = 'A'; X

X t.b = 5; ✓

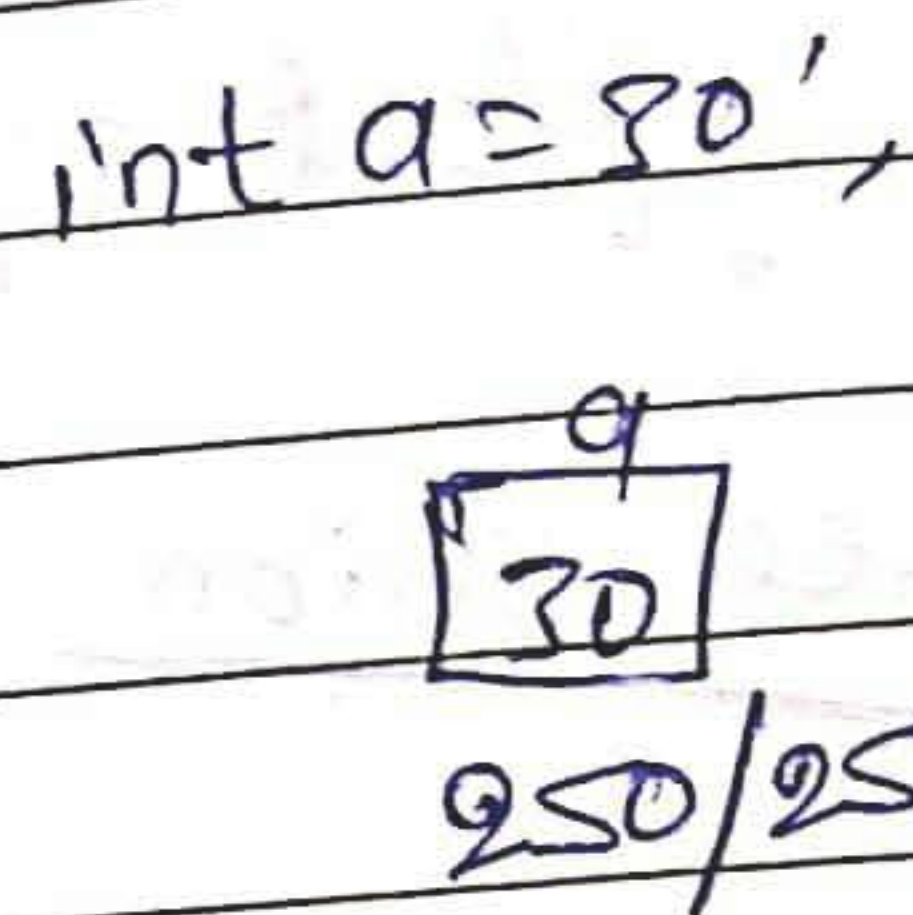
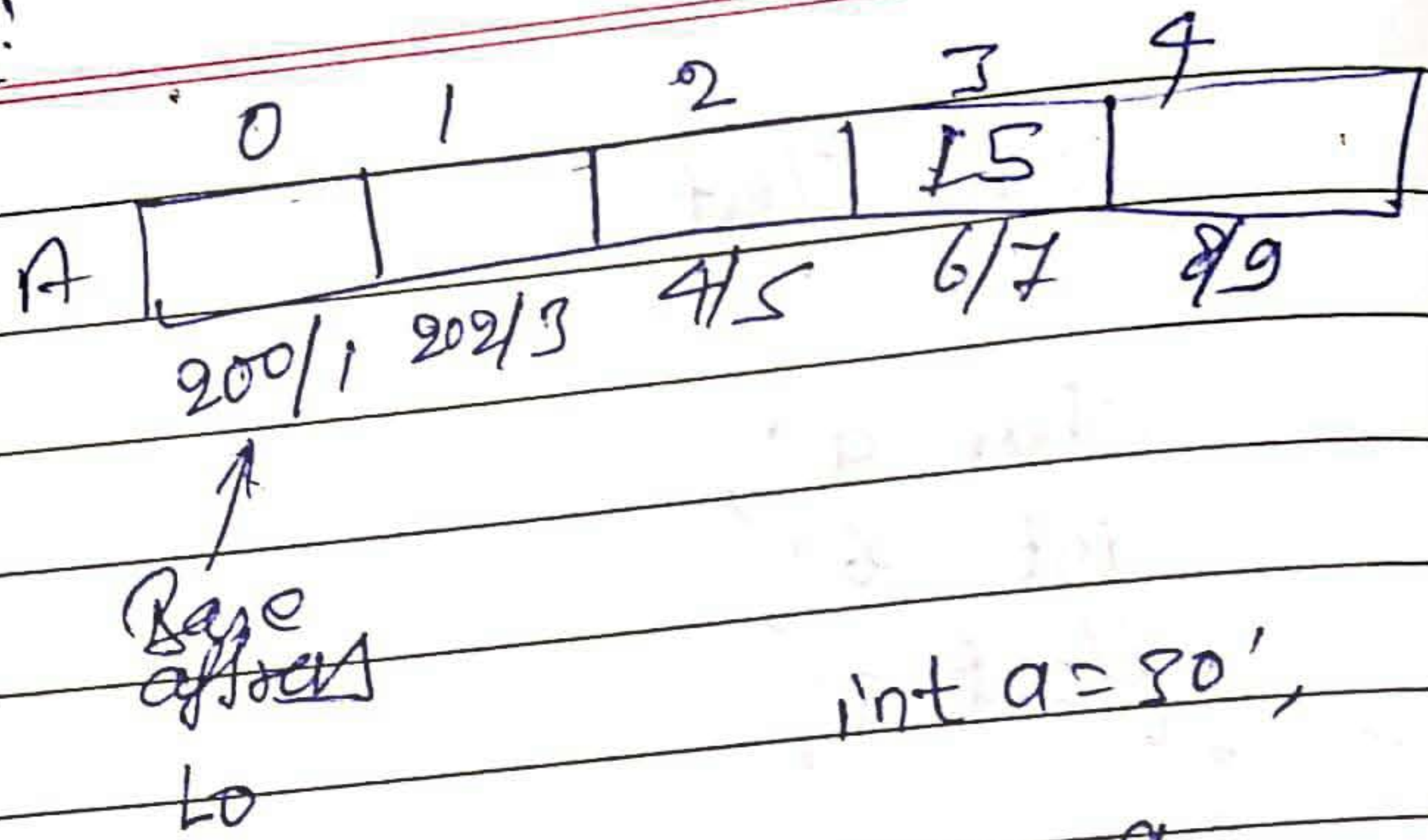
// C language allows discriminant union for using fixed values.

* in discriminant we are allowed only fixed member to use.

Arrays:

①

```
int A[5];
A[3] = 15;
Addr[A[3]] = Lo + 3 * 2
            = 200 + 6
            = 206
```



* How compiler handle array, and generate relative location.

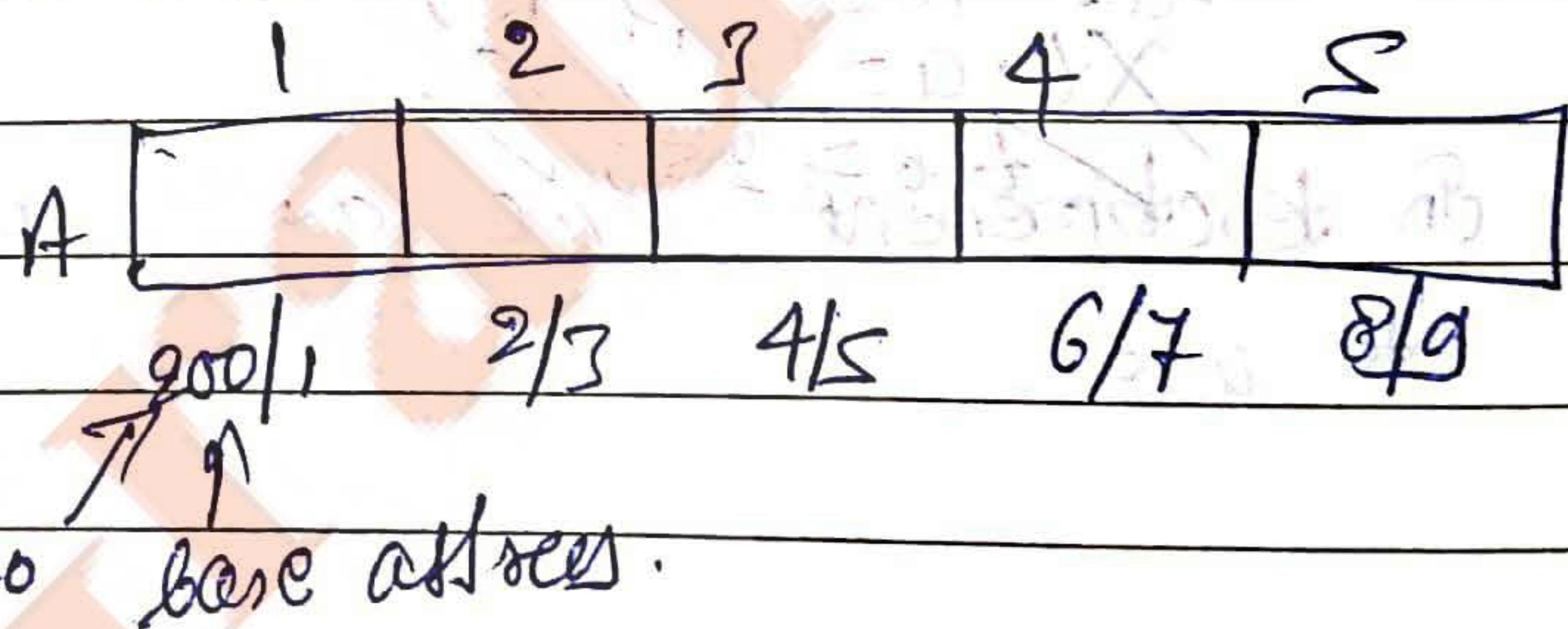
- The addresses are defined based on base address

$$\text{Addr}(A[i]) = \text{Lo} + i * \omega$$

↑
↑
↑

base address
index
size of data type

② Array index starting from '1'.



```
var A[1..5] : Integer
```

$$\text{Addr}(A[i]) = \text{Lo} + (i-1) * \omega$$

$$\text{Addr}(A[1]) = L_0 + 0 \\ = 200$$

$$\text{Addr}(A[2]) = L_0 + 1 \times 2$$

$$\text{Addr}(A[3]) = L_0 + 2 \times 2$$

$$\text{Addr}(A[i]) = L_0 + (i-1) \times W$$

(3) Declare an array, by any starting bound

var A[lb --- ub] Type

$$\text{Addr}(A[i]) = L_0 + (i - lb) \times W$$

eg. int A[-5, --- 5]

$$\text{addr}(A[i]) =$$

$$L_0 = 100$$

$$W = 2$$

$$\text{Addr}(A[1]) = 100 + (1 + 5) \times 2 \\ = 112$$

eg. $\text{Addr}(A[2]) = 112$

$$\text{Addr}(A[3]) = 116$$

$$L_0 + 2 \quad L_0 + 2 \quad \text{etc}$$

(4) 2D array, -

~~int~~ int A[3][4];

	0	1	2	3	4	5	6	7	8	9	10	11
A	a ₀₀	a ₀₁	a ₀₂	a ₀₃	a ₁₀	a ₁₁	a ₁₂	a ₁₃	a ₂₀	a ₂₁	a ₂₂	a ₂₃
	200/1	2/3	4/5	6/7	8/9	10/11	12/13	14	16	18	20	22/23
L ₀												

A	0	1	2	3
0	a ₀₀	a ₀₁	a ₀₂	a ₀₃
1	a ₁₀	a ₁₁	a ₁₂	a ₁₃
2	a ₂₀	a ₂₁	a ₂₂	a ₂₃

1. → Row major mapping
 2. → Column major mapping

Row measure:

Addr (A[i][j])

$$\text{Addr}(A[i][j]) = L_0 + [i \times 4 + j] \times 2$$

$$= 200 + [7] \times 2 = 214$$

$$\text{Addr}(A[2][1]) = L_0 + [2 \times 4 + 1] \times 2$$

$$= 200 + [9] \times 2 = 218$$

$$\text{Addr}(A[i][j]) = L_0 + [i \times n + j] \times w$$

column measure:

	0	1	2	3	4	5	6	7	8	9	10	11
A	a ₀₀	a ₁₀	a ₂₀	a ₀₁	a ₁₁	a ₂₁						
	200/1	2/3	4/5	6/7	8/9	10/11	12/13	14/15	16/17	18/19	20/21	22/23
L ₀	col ₁			col ₂			col ₃				col ₄	

$$\text{Addr of } (A[i][j]) = L_0 + (2 \times 3 + 1) \times 2$$

$$= 200 + [7] \times 2 = 214$$

$$\text{Addr } (A[2][3]) = L_0 + [3 \times 3 + 2] \times 2$$

$$= 200 + [11] \times 2 = 222$$

$$\boxed{\text{Addr } (A[i][j]) = L_0 + [j \times m + i] \times w}$$

Note: - Both are equally efficient
 - In C language row measure is used ~
 - Row measure is also known as lexical analysis.

Gate Q1

$$C = A \times B$$

A in Row measure

B in column measure

→ both in row measure

→ both in column measure

Independent of mapping/representation.

Gate Q2

var A[1..10][1..15] Type

$$L_0 = 100, w = 1$$

$$\text{addr } (A[i][j]) =$$

If lexical mapping/row measure is used.

Ans

$$\text{addr } (A[i][j]) = 100 + [10i + j] \times 1$$

$$= 100 + 10i + j$$

$$= 8 + 15i + j$$

5

Row major index starting

```
int A[l - m][1 - n]
```

$$\text{Addr}(A[i][j]) = b + [(i-1) * n - j - 1] * w$$

Row ~~major~~ major for any index

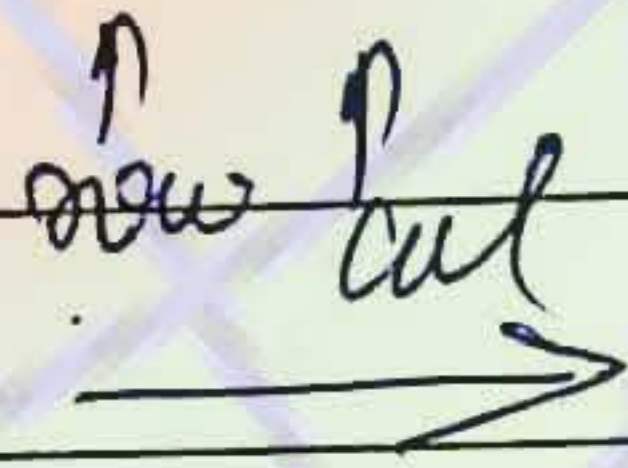
```
Type A[lb1 - ub1][lb2 - ub2]
```

$$\text{Addr}(A[i][j]) = b + [(i - lb_1) * (ub_2 - lb_2 + 1) + (j - lb_2)] * w$$

6) 3D Array.

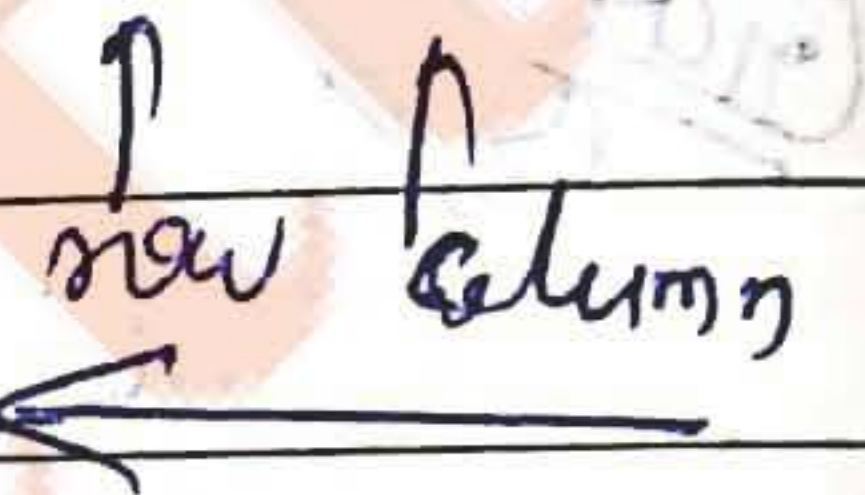
```
int A[m][n]
int A[m][n]
```

```
int A[m][n]
```



b =

```
int A[m][n]
```



Q. compiler has generated ~~these~~ intermediate
 (a) Find datatype and dimensions for
~~int A[10][10]~~

$$t_1 = i \times 1024$$

$$t_2 = j \times 92$$

$$t_3 = k \times 4$$

$$t_4 = t_1 + t_2$$

$$t_5 = t_4 + t_3$$

$$t_6 = x [63]$$

$$[A] = \text{Type} = A [D_1] [D_2] [D_3] [D_4]$$

$$\text{Addr} (A [i_1, i_2])$$

Horner's Rule:

$$P(x) = 4x^3 + 3x^2 + 9x + 7$$

$$- P(x) = 4 \underbrace{x \times x \times x}_3 + \underbrace{3x \times x}_2 + \underbrace{9x}_1 + 7 = 3 + 2 + 1$$

rule:-

$$\begin{aligned} - P(x) &= 7 + 9x + 3x^2 + 4x^3 \\ &= 7 + x(9 + 3x + 4x^2) \\ &= 7 + x(9 + x(3 + 4x)) \end{aligned}$$

$(O(n^2))$

$\rightarrow 3$

$O(n)$

eg: $P(x) = 5x^4 + 3x^2 + 5$

$\Rightarrow 4$

Note The no. of multiplication is equal to atmost degree of polynomial n

eg: $P(x) = x^3 + 2x^2 + 9x + 7$

$$\begin{aligned} P(x) &= 7 + 9x + 2x^2 + x^3 \\ &= 7 + x(9 + 2x + x^2) \\ &= 7 + x(9 + x(2 + x)) \end{aligned}$$

2

Q) $P(n) = 3n^5 + 4n^3 + 8n + 7$

A $P(n) = 7 + 8n + 4n^3 + 3n^5$
 $= 7 + n(8 + 4n^2 + 3n^4)$
 $= 7 + n(8 + n^2(4n + 3n^2))$

~~$= 7 + n(8 + n^2(4n + 3n^2))$~~ \downarrow
 $\textcircled{5}$

Now

$t = n^2$

$= 7 + n(8 + t(4 + 3t))$
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $1 \quad 1 \quad 1 \quad 1 = \textcircled{4}$

Note: If one temporary variable is allowed then no. of multiplication will decrease.

eg $P(n) = n^4 + 3n^2 + 8$

$P(n) = 8 + 3n^2 + n^4$
 $= 8 + n^2(3 + n^2)$

$t = n^2$

$= 8 + t(3 + t)$
 $\downarrow \quad \downarrow$
 $1 \quad 1 = 2$

$1 + 1 = 2$
 $=$

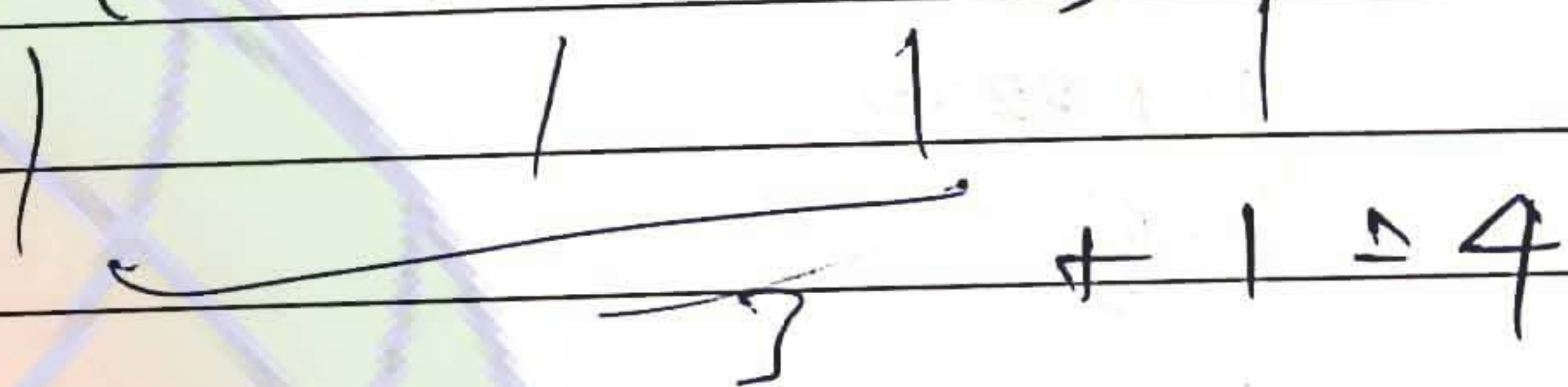
|| " " म को, मानक करण करेगा ||
 सारा त म
 सारा

L1 → learn again

$$\text{Addr}(A[i,j][i_2][i_3][i_4]) = L_0 + (i_1 * D_2 * D_3 * D_4 + i_2 * D_3 * D_4 + i_3 * D_4 + i_4) * W$$

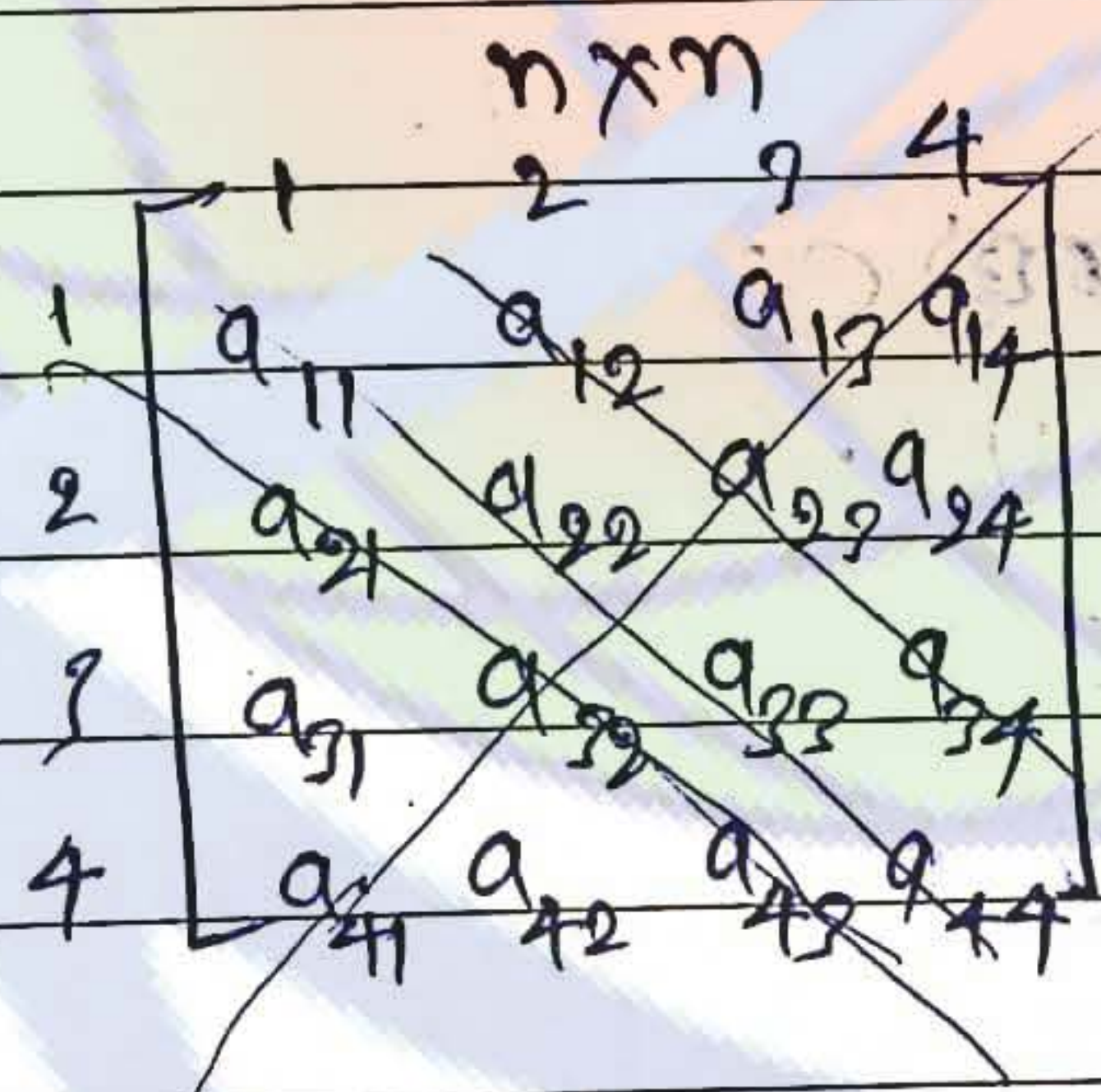
$$= L_0 + [i_4 + i_3 * D_4 + i_2 * D_3 * D_4 + i_1 * D_2 * D_3 * D_4] * W$$

$$= L_0 + [i_4 + D_4 (i_3 + D_3 (i_2 + i_1 * D_2))] * W$$



★ Matrices:

DI



if $(i=j)$ → diagonal

if $(i=1)$ → 1st row

if $(i < j)$ → Upper triangle

if $(i > j)$ → lower triangular

if $(i-j=1)$ → diagonal below main diagonal

if $(i-j=-1)$ → " above " "

if $(i+j=n+1)$ → cross diagonal

if $(i+j > n)$ → right bottom triangle

gate
Q2

V is a matrix $n \times n$

$$\forall V[i][j] = i - j$$

then

sum of all elements = ?

$$11=0 \quad 12=-1$$

$$21=1 \quad 22=0$$

$$= 0$$

Ans = 0

A

Q3

$$C = 100;$$

for (i=1; i<=n; i++)

{
for (j=1; j<=n; j++)

$$t = A[i][j] + C;$$

$$A[i][j] = A[j][i];$$

$$A[j][i] = t - C;$$

}

Ans

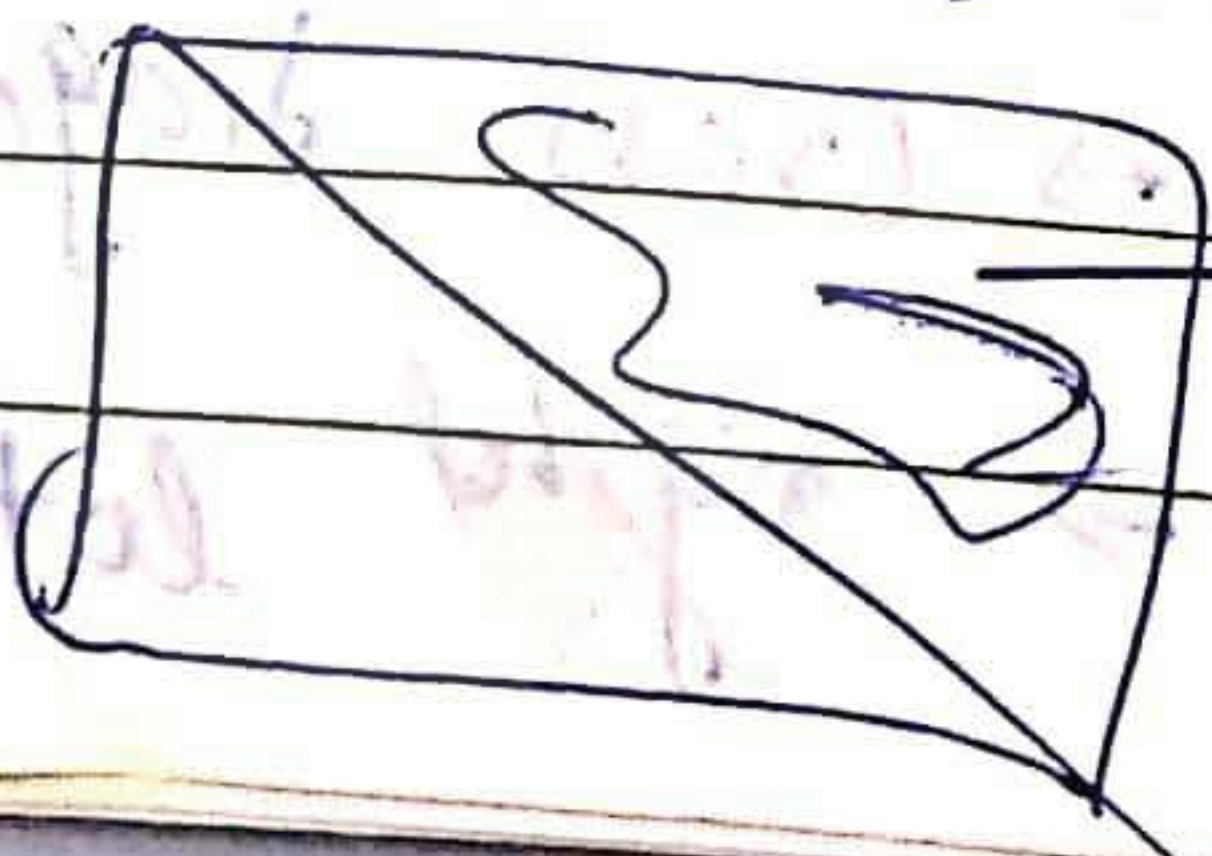
~~A[i][j] != 1~~

try by taking small matrix

$$\begin{matrix}
 & 1 & 2 & 3 & 4 & 5 \\
 1 & 1 & 2 & 3 & 4 & 5 \\
 2 & 2 & 2 & 3 & 4 & 5 \\
 3 & 3 & 3 & 3 & 4 & 5 \\
 4 & 4 & 3 & 3 & 3 & 4 \\
 5 & 5 & 2 & 2 & 2 & 2
 \end{matrix}$$

Same matrix as

Note:



for some matrix from the
take only upper lower

- transpose of a matrix can not be done within a matrix.

★ Special matrix: —

- ★ (i) diagonal
- (2) lower triangular matrix
- (3) upper "
- (4) symmetric
- (5) tridiagonal
- (6) ~~tridiagonal~~ tri-diagonal matrix

① diagonal:-

		1	2	3	4
	1	2	0	0	0
A =	2	0	5	0	0
	3	0	0	8	0
	4	0	0	0	10
		n x n			

if $(i \neq j)$ then $A[i][j] = 0$

No. non-zero element = n

	0	1	2	3
A	2	5	8	10

if $(i = j)$

Addr $(A[i][j]) = \text{Lo} + [i-1] * \omega$

↑
index

if $(i \neq j)$

0

```

class Diagonal
{
    int *A, n;
public
    Diagonal (int d)
    {
        n = d;
        A = new int[n];
    }
    void set (int i, int j, int v)
    {
        if (i == j)
            A[i-1] = v;
    }
    int get (int i, int j)
    {
        if (i == j)
            return A[i-1];
        else
            return 0;
    }
}
    
```

② * lower triangular matrix

1	a_{11}	0	0	0
2	a_{21}	a_{22}	0	0
3	a_{31}	a_{32}	a_{33}	0
4	a_{41}	a_{42}	a_{43}	a_{44}

lower triang

$n \times n$

if $(i < j)$ then $A[i][j] = 0$

then No. of non-zero elements = $1 + 2 + \dots + n = \frac{n(n+1)}{2}$

Row major

	0	1	2	3	4	5	6	7	8	9
A	a ₁₁	a ₁₂	a ₁₃	a ₁₄	a ₁₅	a ₁₆	a ₁₇	a ₁₈	a ₁₉	a ₁₁₀
	col 1		col 2			col 3		col 4		

Row-major

$$\text{Addr}(A[i][j]) = L_0 + \left[\underbrace{1+2+\dots+i}_{i} + \frac{2j}{w} \right] * w$$

$$= L_0 + \underbrace{i}_{\text{index}} * w$$

$$\text{Addr}(A[4][3]) = L_0 + \left[\underbrace{1+2+3}_{i} + \frac{2*3}{w} \right] * w$$

$$= L_0 + 8 * w$$

$$\text{Addr}(A[i][j]) = L_0 + [1+2+\dots+i-1 + j-1] * w$$

$$= L_0 + \left[\frac{i(i-1)}{2} + j-1 \right] * w$$

row major formula for lower triangle

row

Column major

A	a ₁₁	a ₂₁	a ₃₁	a ₄₁	a ₂₂	a ₃₂	a ₄₂	a ₃₃	a ₄₃	a ₄₄
	col 1				col 2		col 3		col 4	

$$\text{Addr}(A[i][j]) = L_0 + [N + N-1 + N-2 + \dots + N - (j-2) + i - j] * w$$

$$\begin{aligned}
 & \left[\begin{array}{c} 10 \times 10 \\ \vdots \\ \vdots \end{array} \right] \quad A [10][4] = 10 + 10 + 9 + 8 + 7 + 6 + 5 \\
 & \quad \quad \quad \quad \quad \quad \quad \quad = 10 + 10 + 10 - 1 + 10 - 2 + 10 - 3 + 10 - 4 + 10 - 5 \\
 & \quad \quad \quad \quad \quad \quad \quad \quad A [10][3] = 10 + 10 + 10 - 1
 \end{aligned}$$

37) Lower Upper triangular matrix

$$\begin{array}{c}
 \begin{matrix} & 1 & 2 & 3 & 4 \\
 1 & a_{11} & a_{12} & a_{13} & a_{14} \\
 2 & 0 & a_{22} & a_{23} & a_{24} \\
 3 & 0 & 0 & a_{33} & a_{34} \\
 4 & 0 & 0 & 0 & a_{44} \end{matrix}
 \end{array}$$

if $(i > j)$ then $A[i][j] = 0$

No. of non-zero elms $\geq \frac{n(n+1)}{2}$

column major

$$\text{Addr } (A [i][j]) = \text{Lo} + \left[\frac{j(j-1)}{2} + (i-1) \right] * w$$

Row major

$$\text{Addr } (A [i][j]) = \text{Lo} + [N + N - 1 + N - 2 + \dots + N - (j - 2) + j - i] * w$$

Note: column major of lower triangle is same as row major of upper triangle.

Row " " " " " "

column " " " "

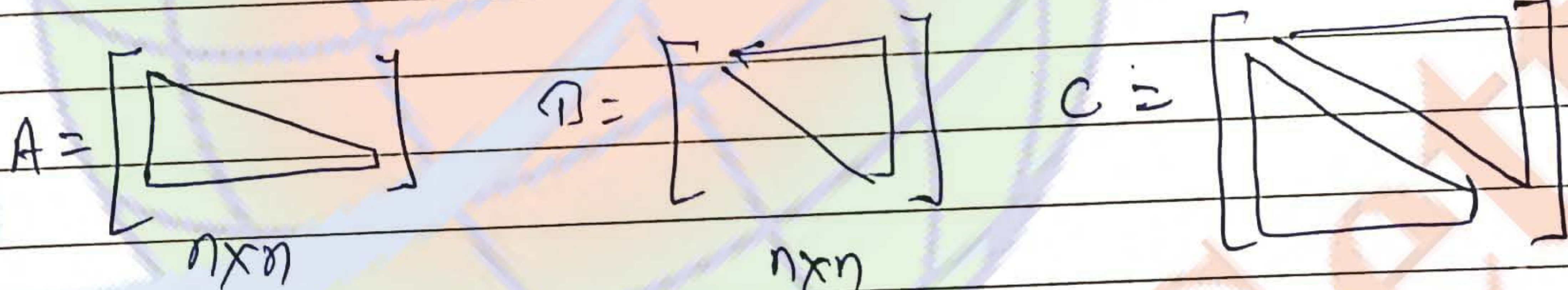
4) Symmetric matrix:-

$$\begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 2 & 4 & 8 & 10 \\ 4 & 8 & 5 & 7 \\ 8 & 5 & 9 & 10 \\ 10 & 7 & 10 & 15 \end{bmatrix} \end{matrix}$$

$$\text{if } (A_{[i][j]}) = A_{[j][i]}$$

$$\frac{n(n+1)}{2}$$

Note



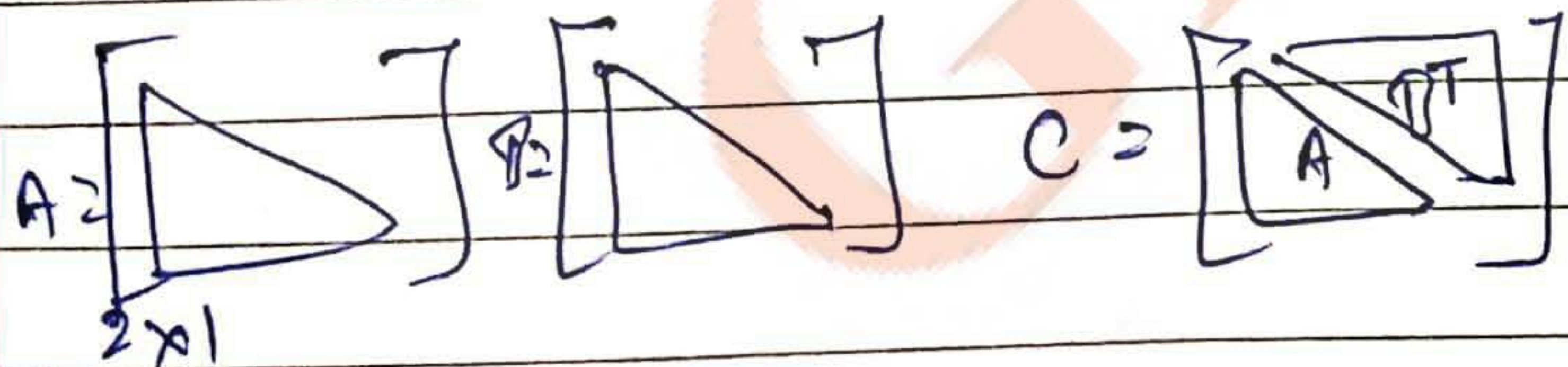
Is x?
↓
dimension of C = ?

$$\begin{bmatrix} 2 & 4 & 8 \\ 4 & 8 & 5 \\ 8 & 5 & 9 \end{bmatrix} \Rightarrow m \times (n+1) A$$

$$A_{[i][j]} = C_{[i][j]}$$

$$B_{[i][j]} = C_{[i][j+1]}$$

Q



$$A_{[i][j]} = C_{[i][j]}$$

$$B_{[i][j]} = C_{[i][j+1]}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & 9 & 0 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 2 & 0 & 0 \\ 7 & 5 & 0 \\ 4 & 6 & 7 \end{bmatrix} = \begin{bmatrix} 2 & 0 & 0 \\ 8 & 5 & 6 \\ 0 & 0 & 7 \end{bmatrix} \quad m \times (n+1)$$

6) Tri-diagonal matrix -

$$A = \begin{bmatrix} a_{11} & a_{12} & 0 & 0 \\ a_{21} & a_{22} & a_{23} & 0 \\ 0 & a_{32} & a_{33} & a_{34} \\ 0 & 0 & a_{43} & a_{44} \end{bmatrix}$$

$$i-j = \{-1, 0, 1\}$$

$$|i-j| \leq 1$$

if $|i-j| > 1$ then $A[i][j] = 0$

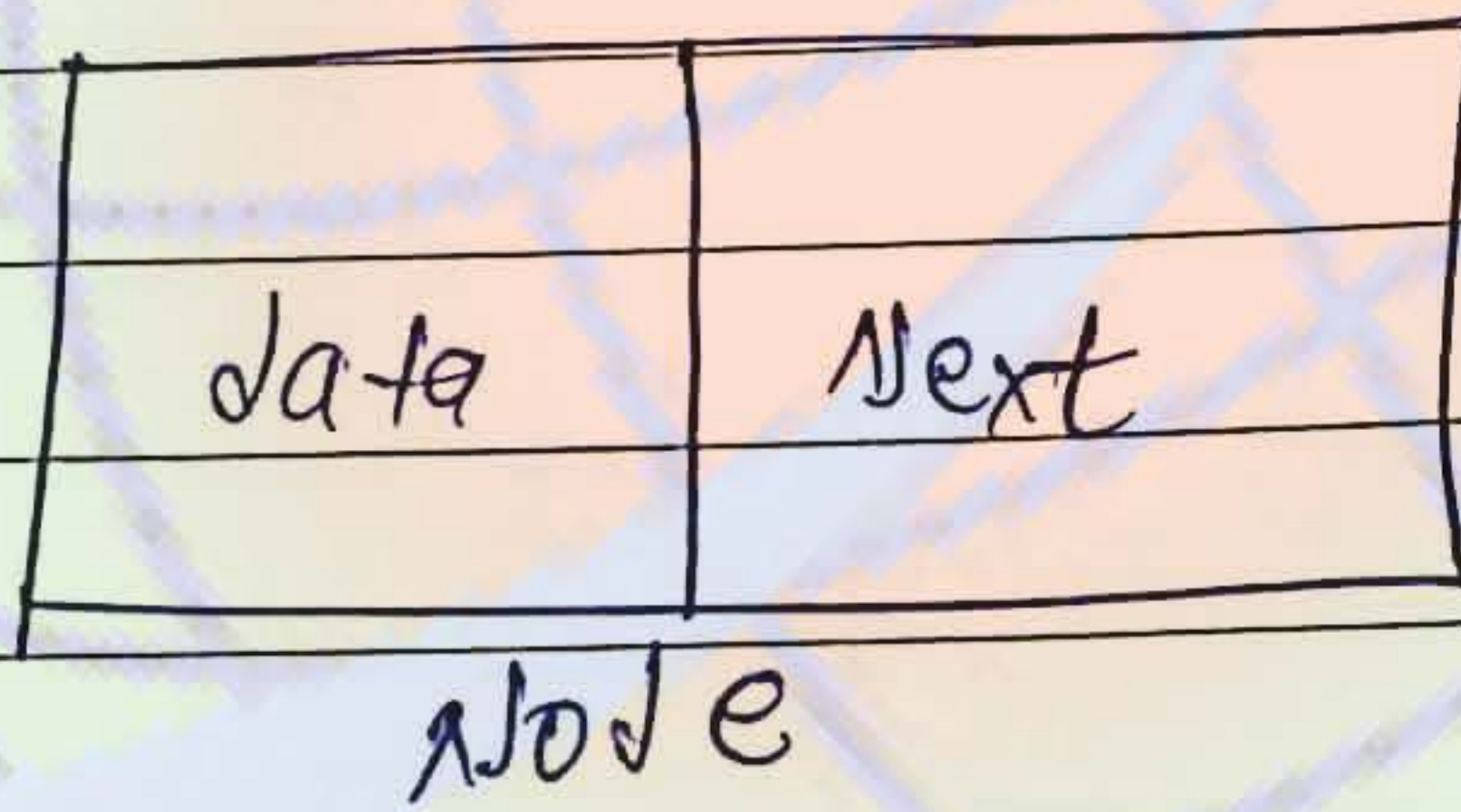
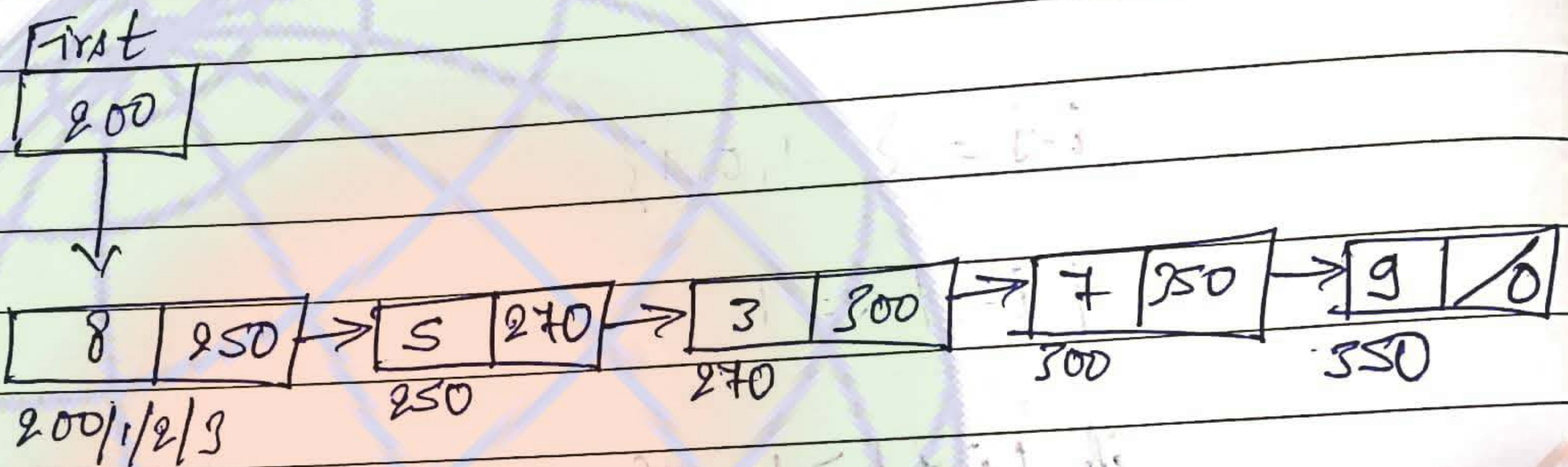
- row major (1 formula)
- col - major (1 formula)

diagonal-by-diagonal
(lower-diag + main diag + upper diag)
(3 formula)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

★ Linked list

- Linked list is a collection of nodes, where each node contain data & pointer to next node.
- First is a pointer, pointing to first node.
- Linked list is stored in heap.



struct Node

int data;

struct Node * next;

};

size = 4 bytes

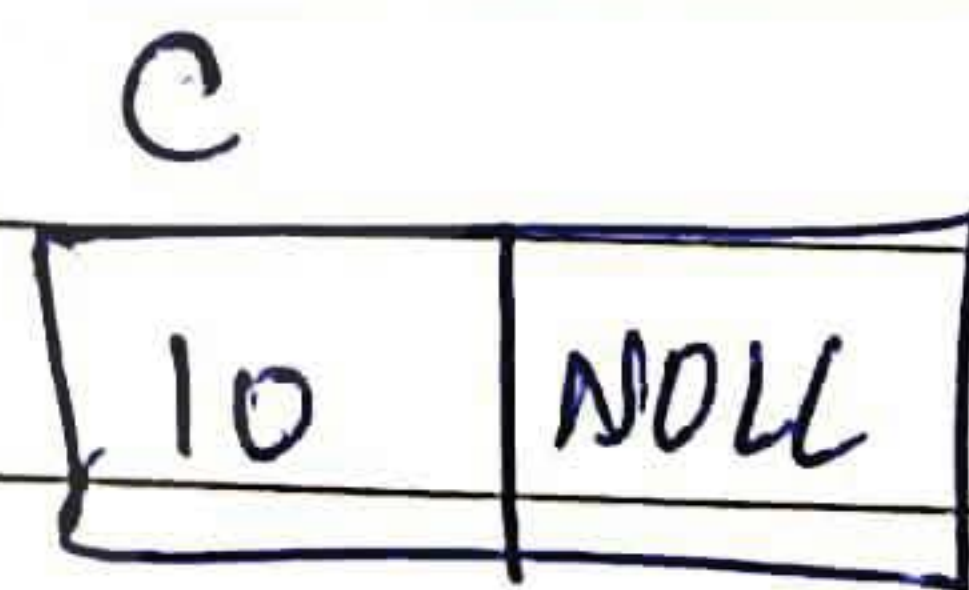
It's a self referential structure.

struct Node * first;

struct Node c;

c.data = 10;

c.next = NULL;

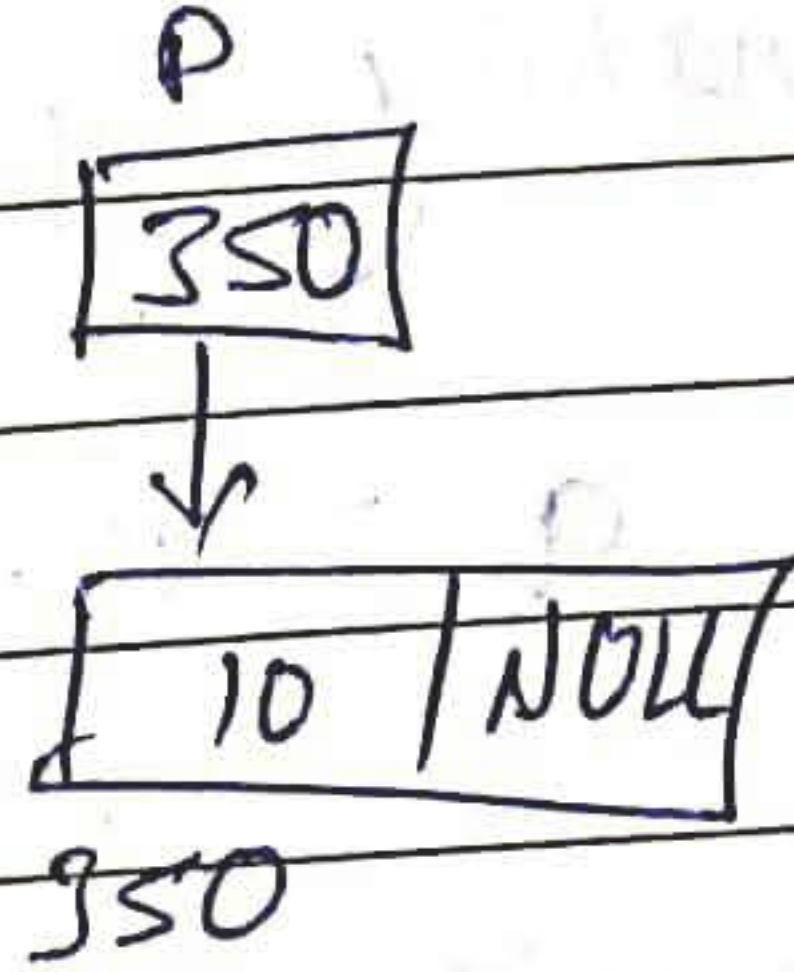


— Creating and accessing a node in stack.

* creating a node in a heap

```

struct Node * p;
p = (struct Node *) malloc (size of (struct Node));
p -> data = 10;
p -> next = NULL;
    
```



Note In C++ we use `new` and `delete`

```

struct Node * p;
p = (struct Node *)
p ->
p ->
p = new Node;
    
```

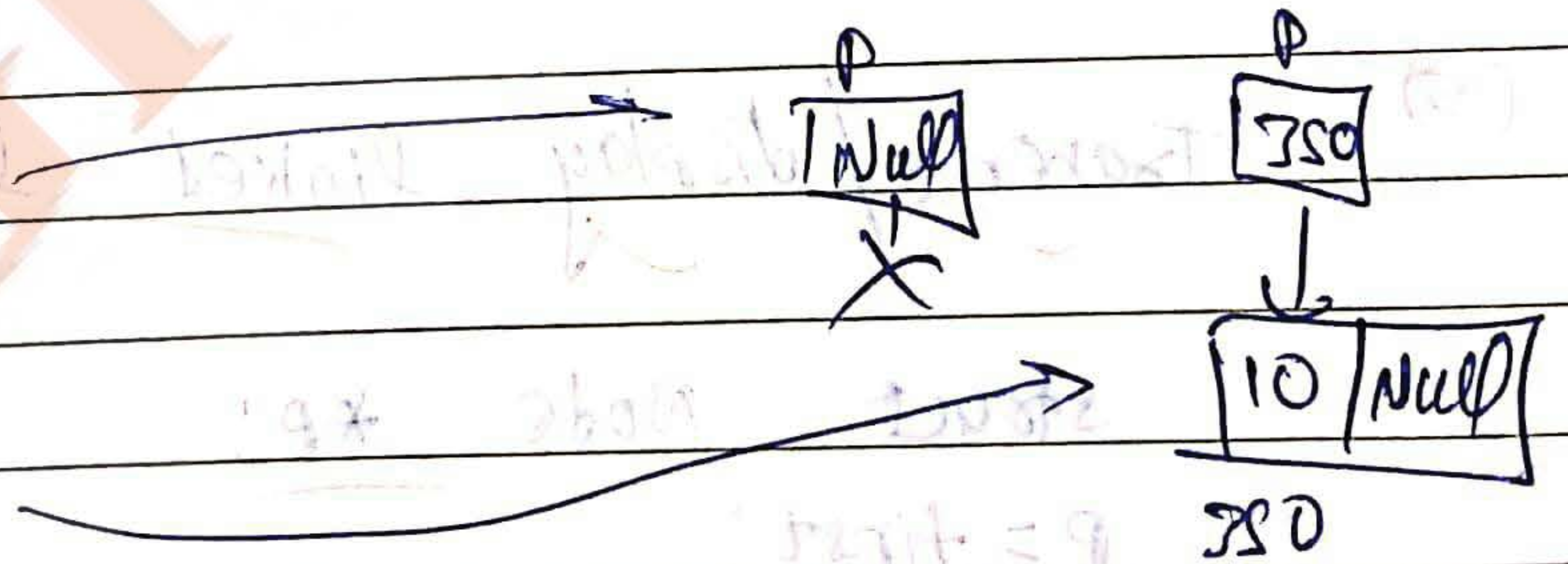
② *

```

struct Node * p;
if (p == NULL)
if (!p)
if (p != NULL)
if (p)
    
```

Not pointing

pointing



3) struct node *P;

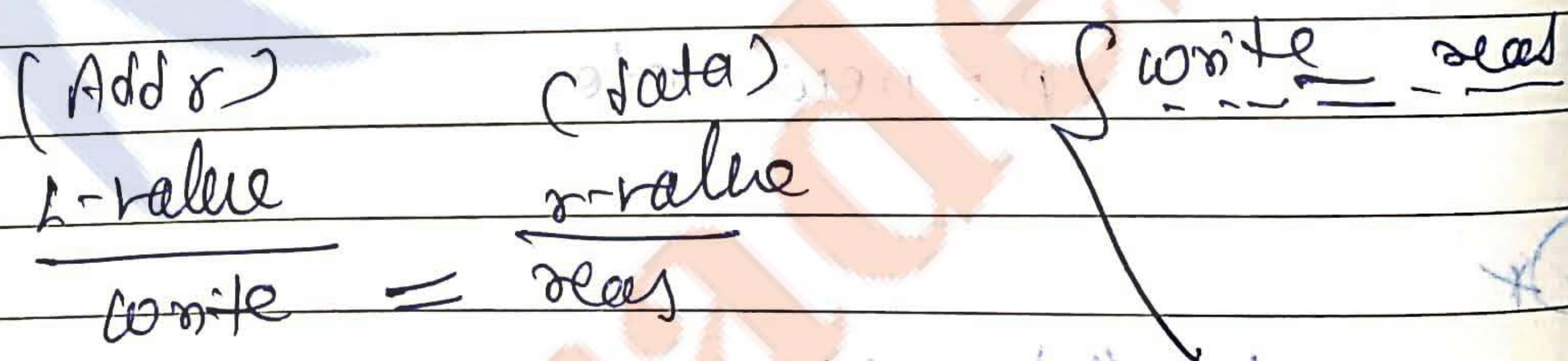
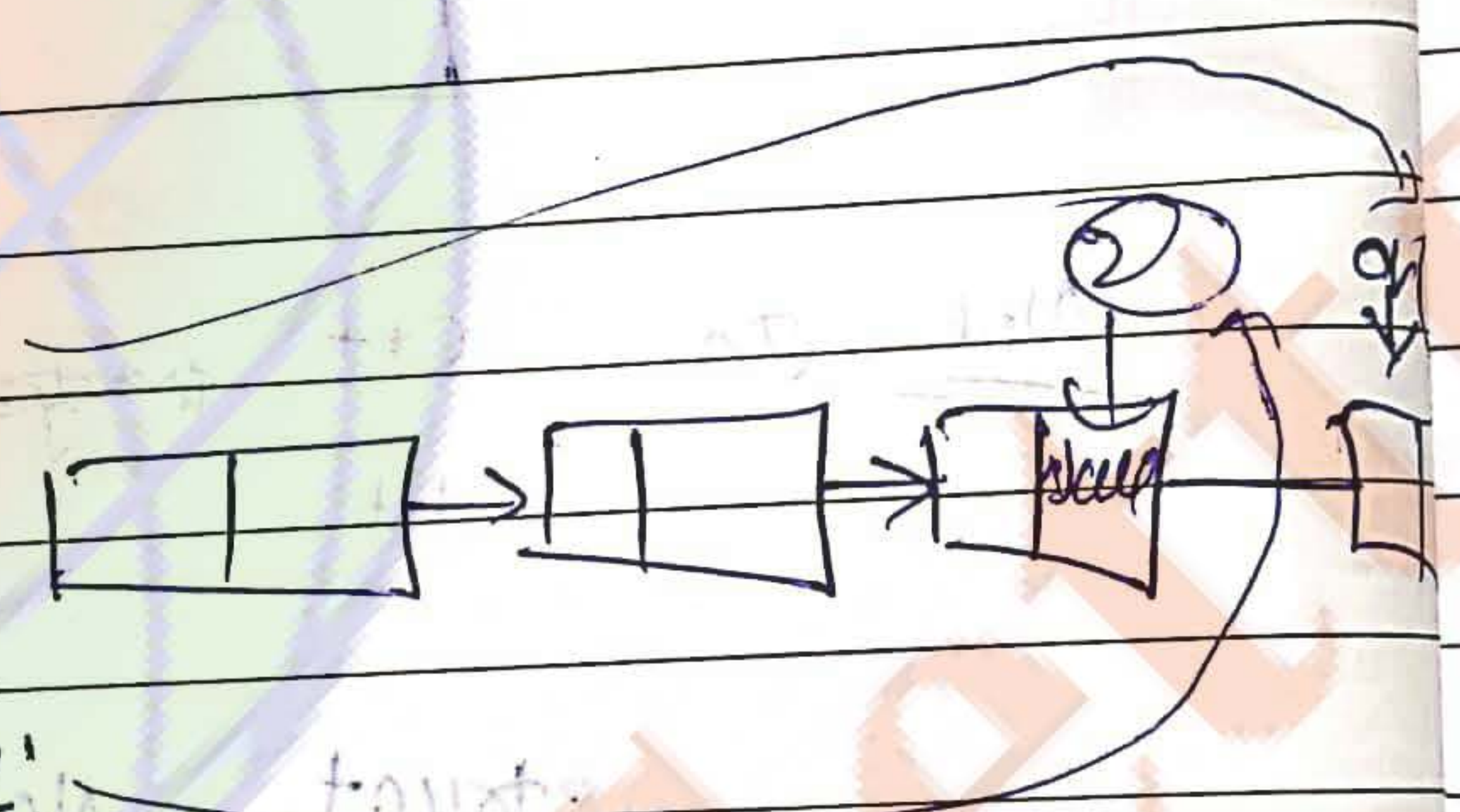
//making q point on next node of P
 $q = P \rightarrow next;$

//moving P to next node
 $P = P \rightarrow next;$

4) struct node *P;

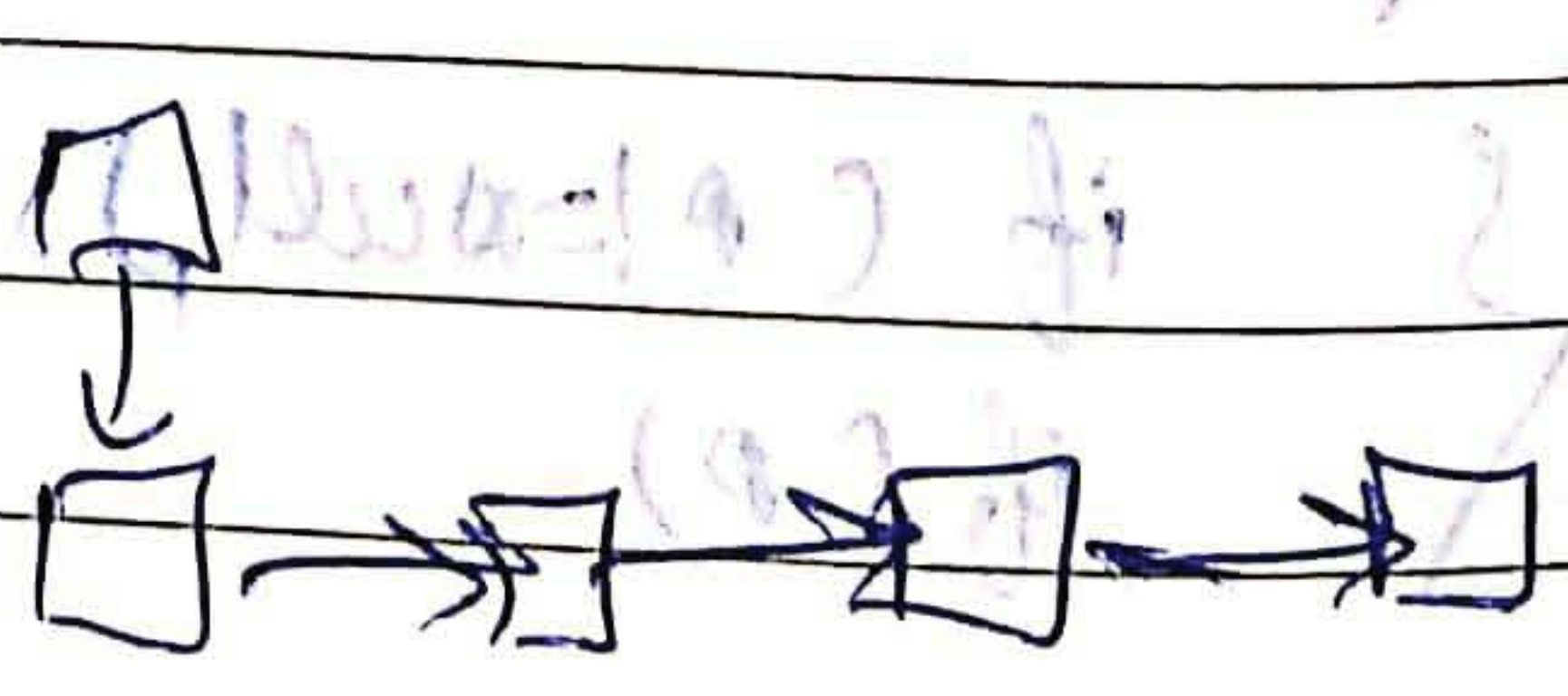
1) $q = P \rightarrow next \rightarrow next \rightarrow next;$
 read

2) $P \rightarrow next \rightarrow next \rightarrow next = NULL;$
 write



5) Traverse/display linked list:-

struct Node *P;
 $P = first;$
 while (P != NULL)



time fe
 $f(n) =$
 $O(n)$

```

printf( "%d", p->data );
p = p->next;
}
    
```

* For n-loop, body of loop will ~~run~~ repeat for n-times.

* And condition will be checked for n+1 times.

```

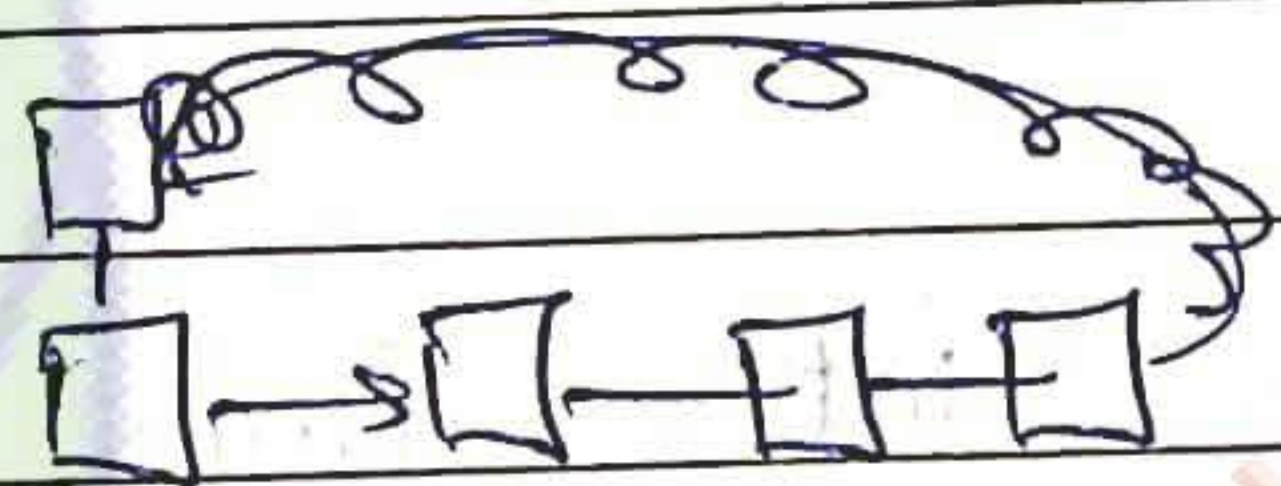
6-> display (struct Node *p)
{
    
```

```

    if (p != NULL)
    {
    
```

```

        printf( "%d", p->data );
        display (p->next);
    }
}
    
```



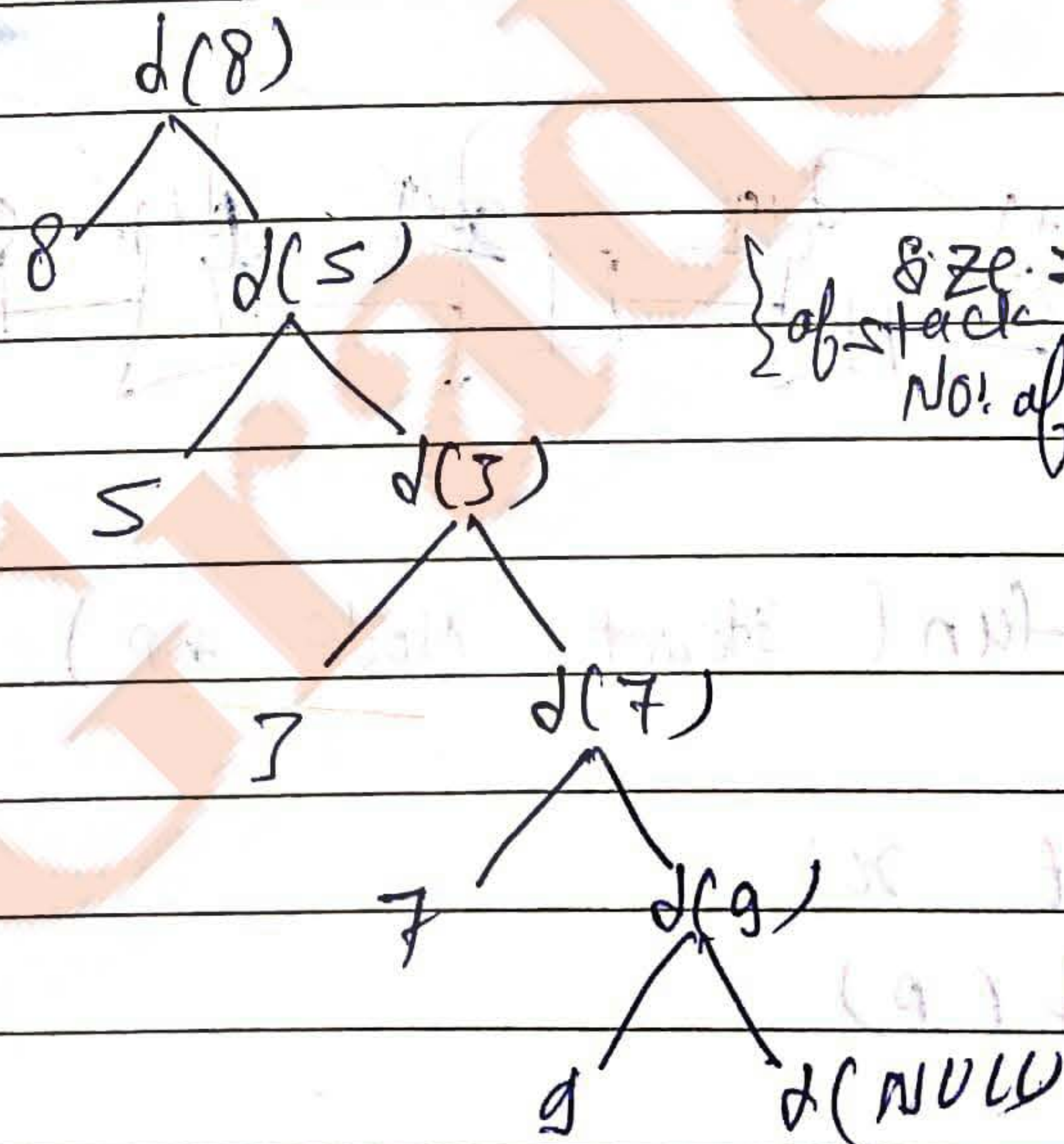
```

display (first);
    
```

time function

$f(n) = n+1$

$O(n)$



Size = n+1
 of stack
 No. of cells = n+1

```

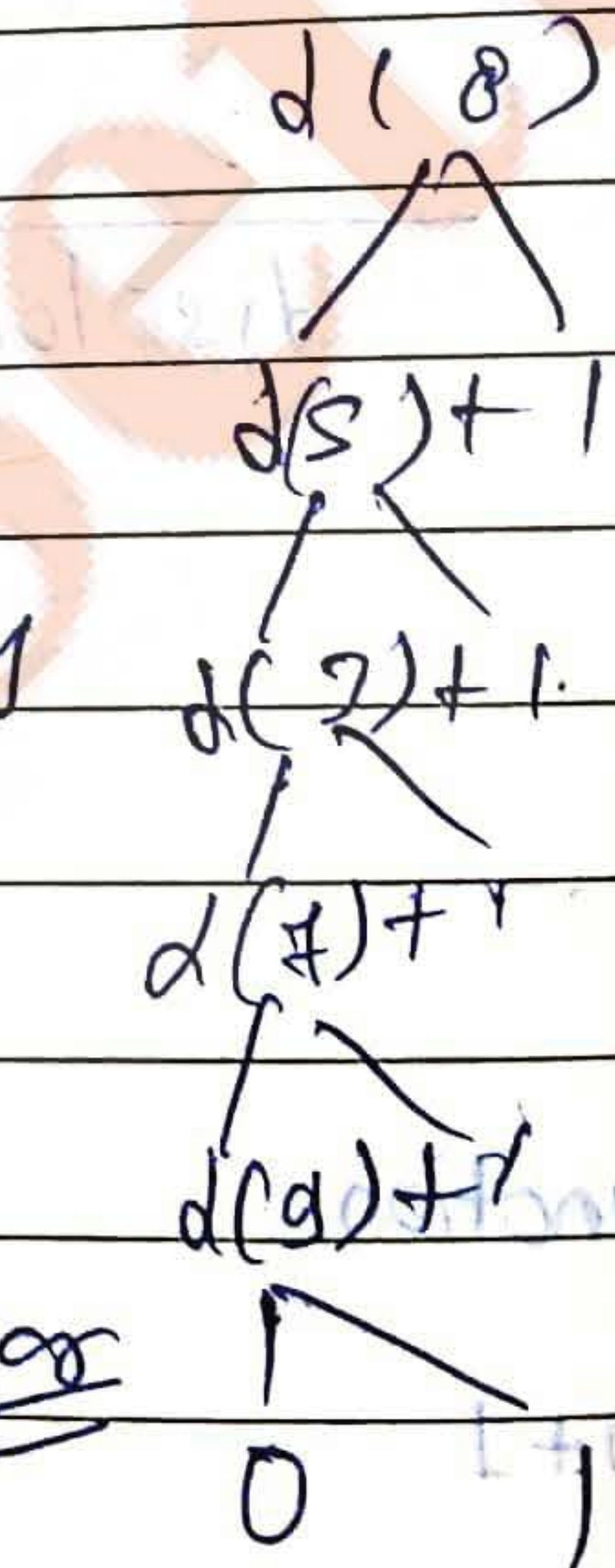
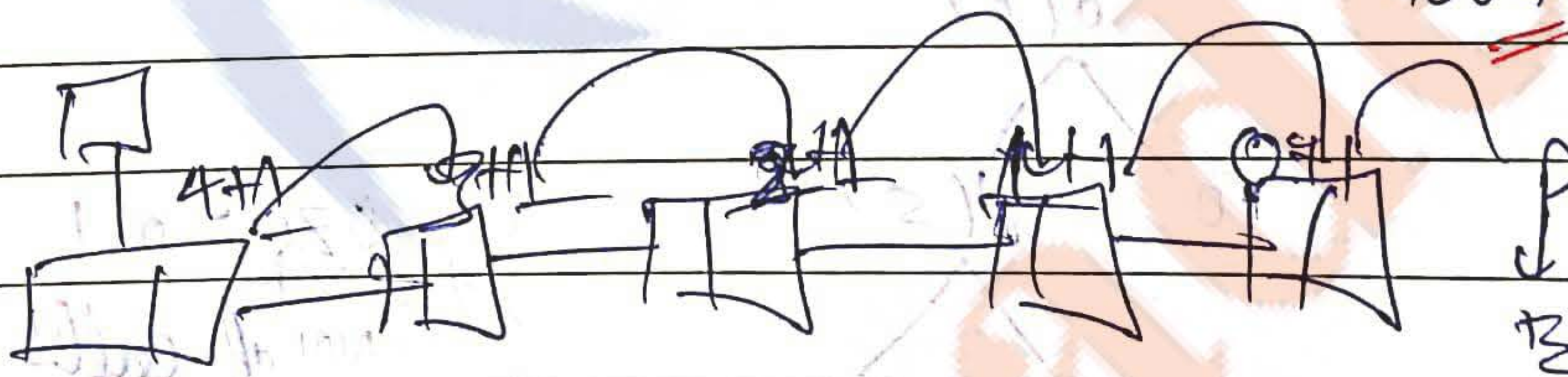
eg> display (struct Node *P)
{
    if (P != NULL)
    {
        display(P->next);
        pf(P->data);
    }
}
    
```

This will display the linked list in reverse

```

eg> int fun (struct Node *P)
{
    if (!P)
        return 0;
    return fun(P->next) + 1;
}
    
```

Ans 5, This is for country node.

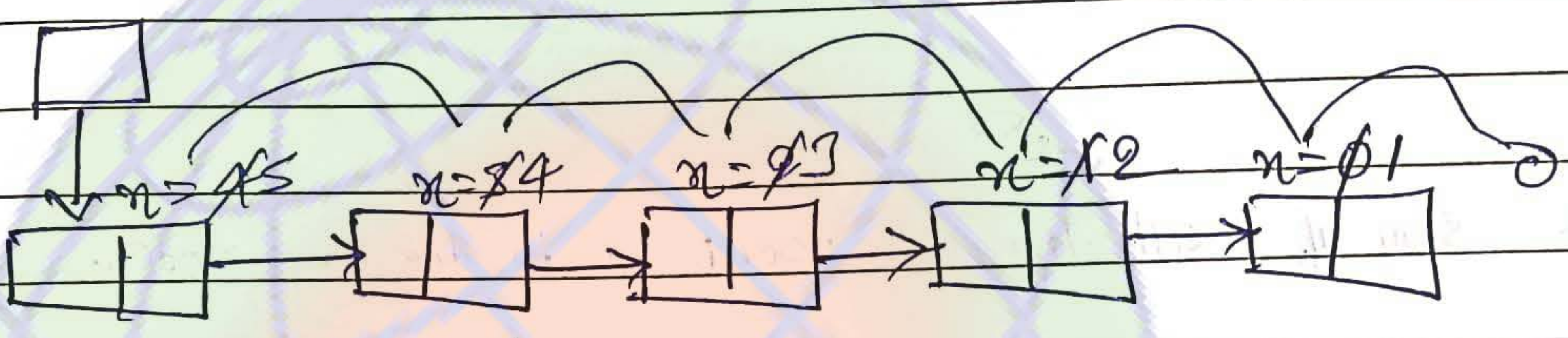


```

eg> int fun (struct Node *P)
{
    int x;
    if (P)
    {
        x = fun(P->next);
    }
}
    
```

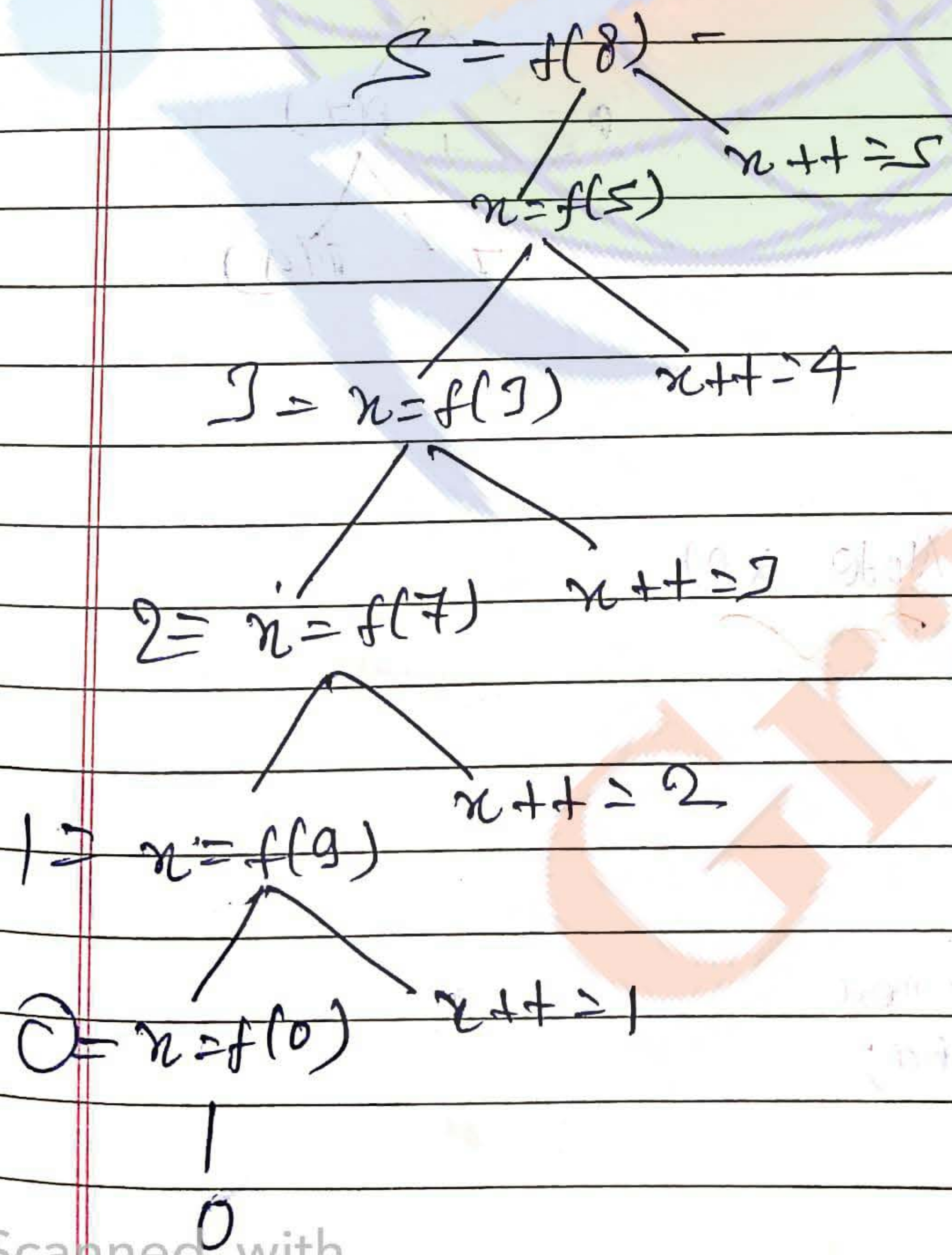
```

    x++;
    return x;
}
return 0;
}
    
```



This is also counting no. of nodes

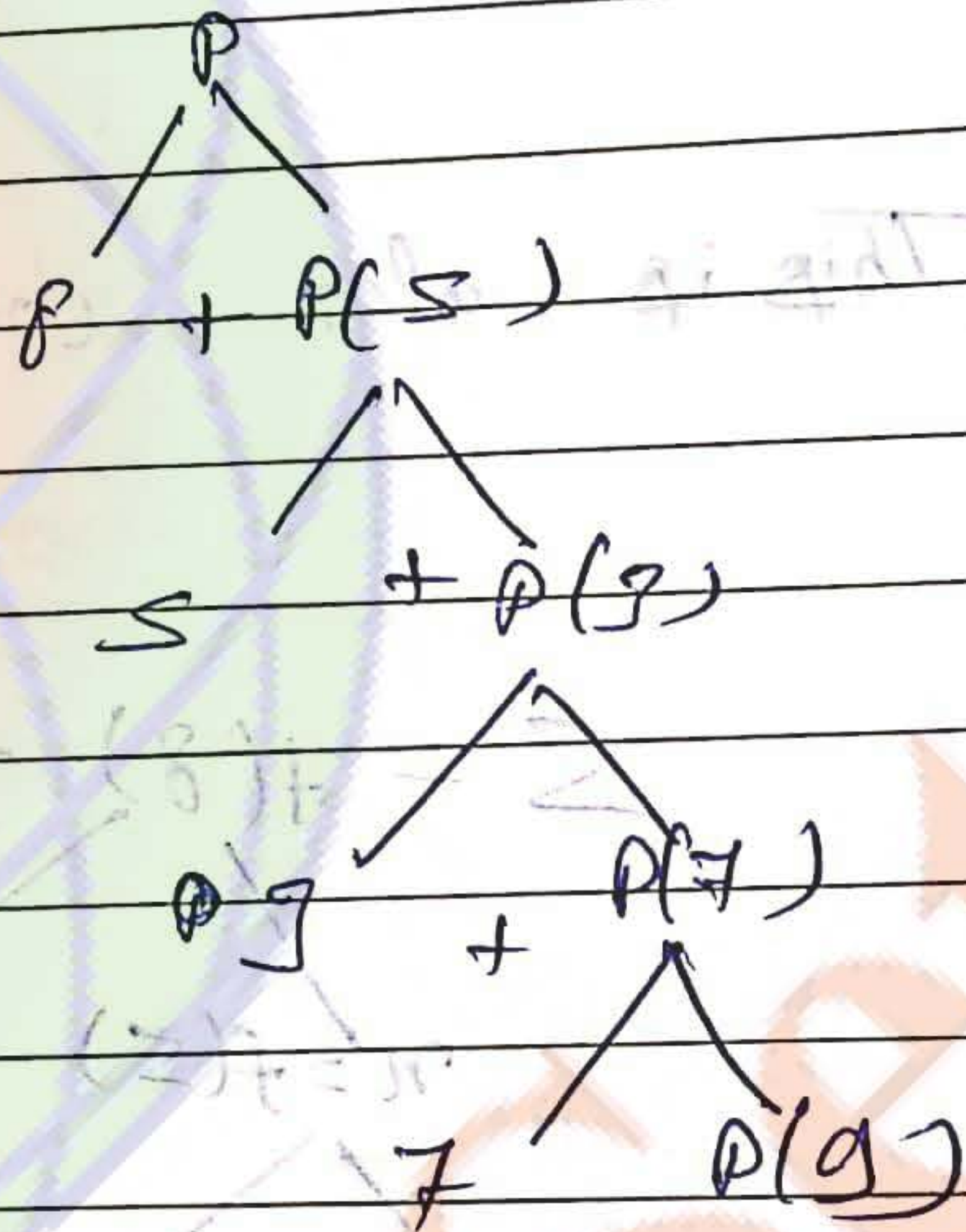
or



```

eg: int fun ( struct Node *P)
{
  if (P)
    return fun ( P->next) + P->data;
  else
    return 0;
}
    
```

An sum of all the present in the nodes.



or

```

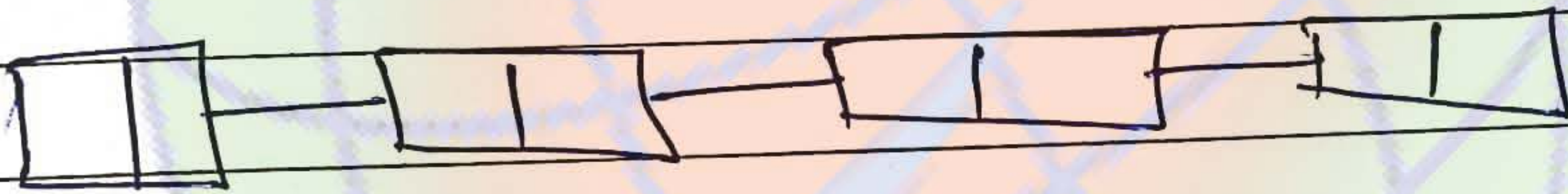
int fun ( struct Node *P)
{
  int x;
  if (P)
  {
    x = fun ( P->next);
    x = x + P->data;
    return x;
  }
  return 0;
}
    
```


~~Q1~~ Linear Search:-

```

int fun (struct Node *P, int x)
{
    if (P)
    {
        if (P->data == x)
            return P;
        return fun(P->next, x);
    }
    return NULL;
}
    
```

A A for searching the data



minimum call = 1 (if in first)
 maximum calls = n+1 (if not in list)
 maximum calls = n (if in the last)

best $O(1)$
 worst $O(n)$

Counting occurrences of x

```

int fun (struct Node *P, int x)
{
    if (P)
    {
        if (P->data == x)
            return fun(P->next, x) + 1;
        return fun(P->next, x);
    }
    return 0;
}
    
```



```

4.) int fun(struct Node *P)
    {
    if (!P)
        return 0;
    x = fun(P->next);
    return x > P->data ? x : P->data;
    }
    
```

A Hint

<pre> c = a > b ? a : b if (a > b) { c = a; } else { c = b; } </pre>	or	<pre> if (x > P->data) return x; else return P->data; </pre>
--	----	---

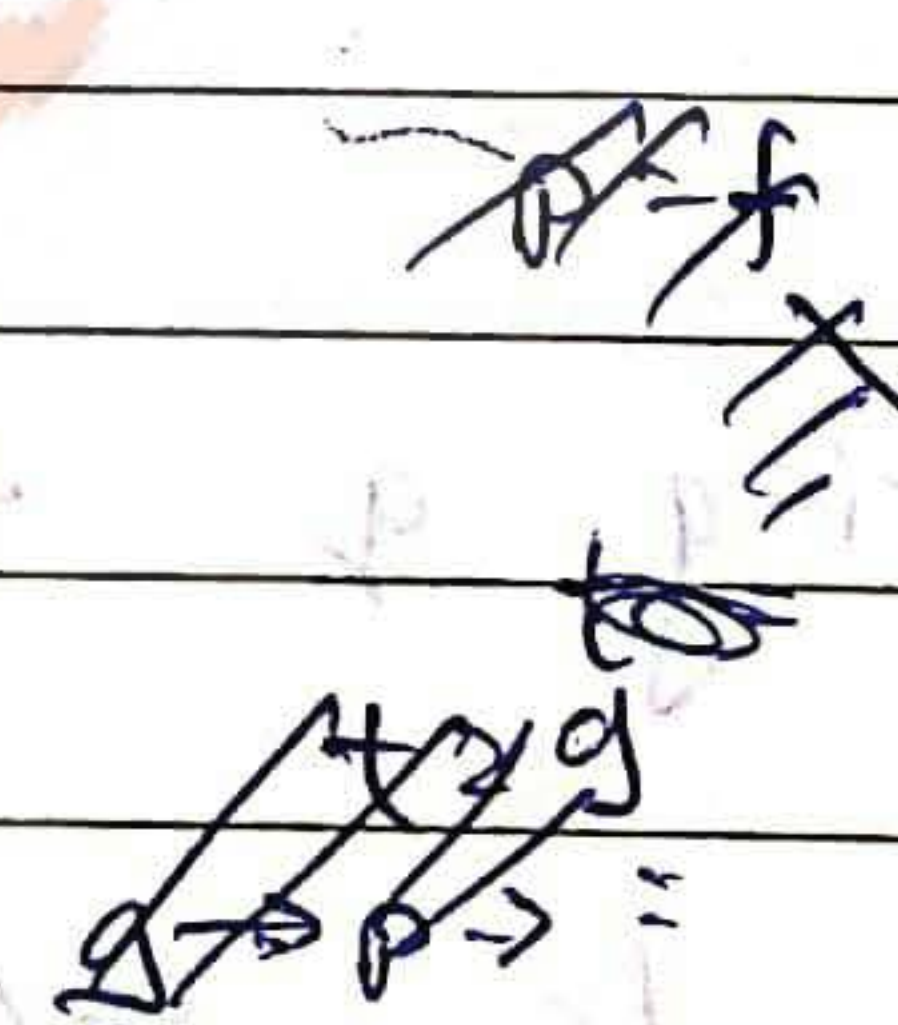
This is for finding greatest number.

- The first value received in x is 0, from the last call.

GATE S.→

```

struct Node *P, *q;
P = first;
q = first->next;
while (P && q)
{
    t = P->data;
    P->data = q->data;
    q->data = t;
    P = P->next;
    q = q->next;
}
P->next = NULL;
    
```



Ans

Hint

```

if ( p != NULL )
    q = p -> next;
else
    q = NULL;
    
```

Ans 5 → 8 → 7 → 3 → 9

```

< >
p = first;
while ( p -> next )
{
    p = p -> next;
}
    
```

// making p move till last node.,

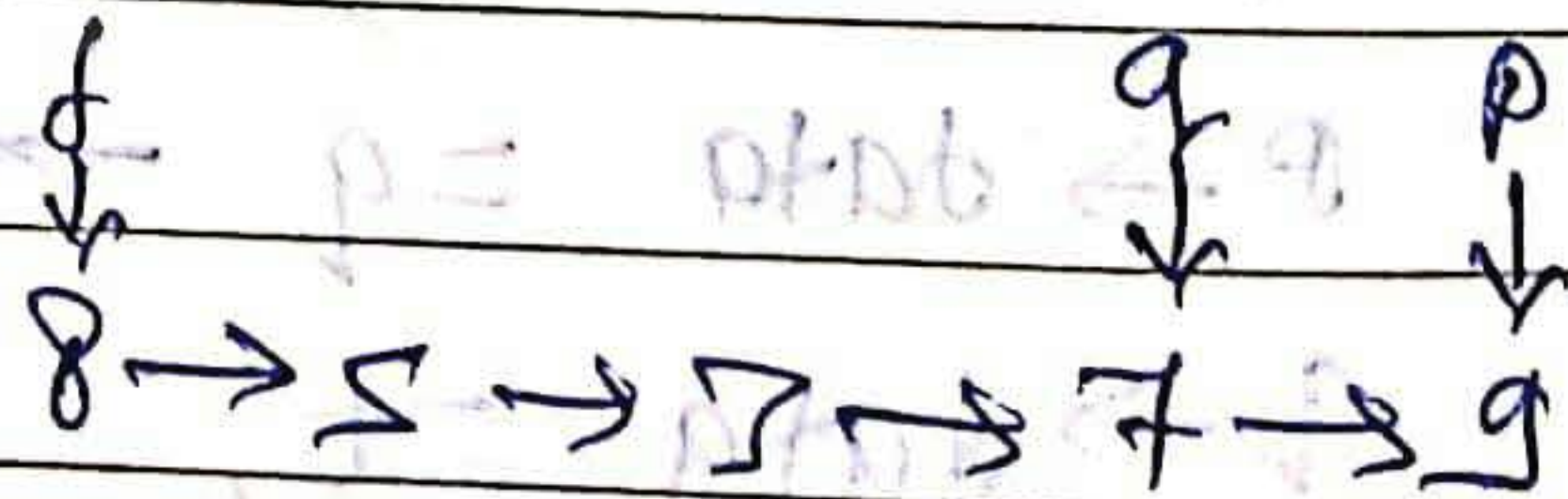
```

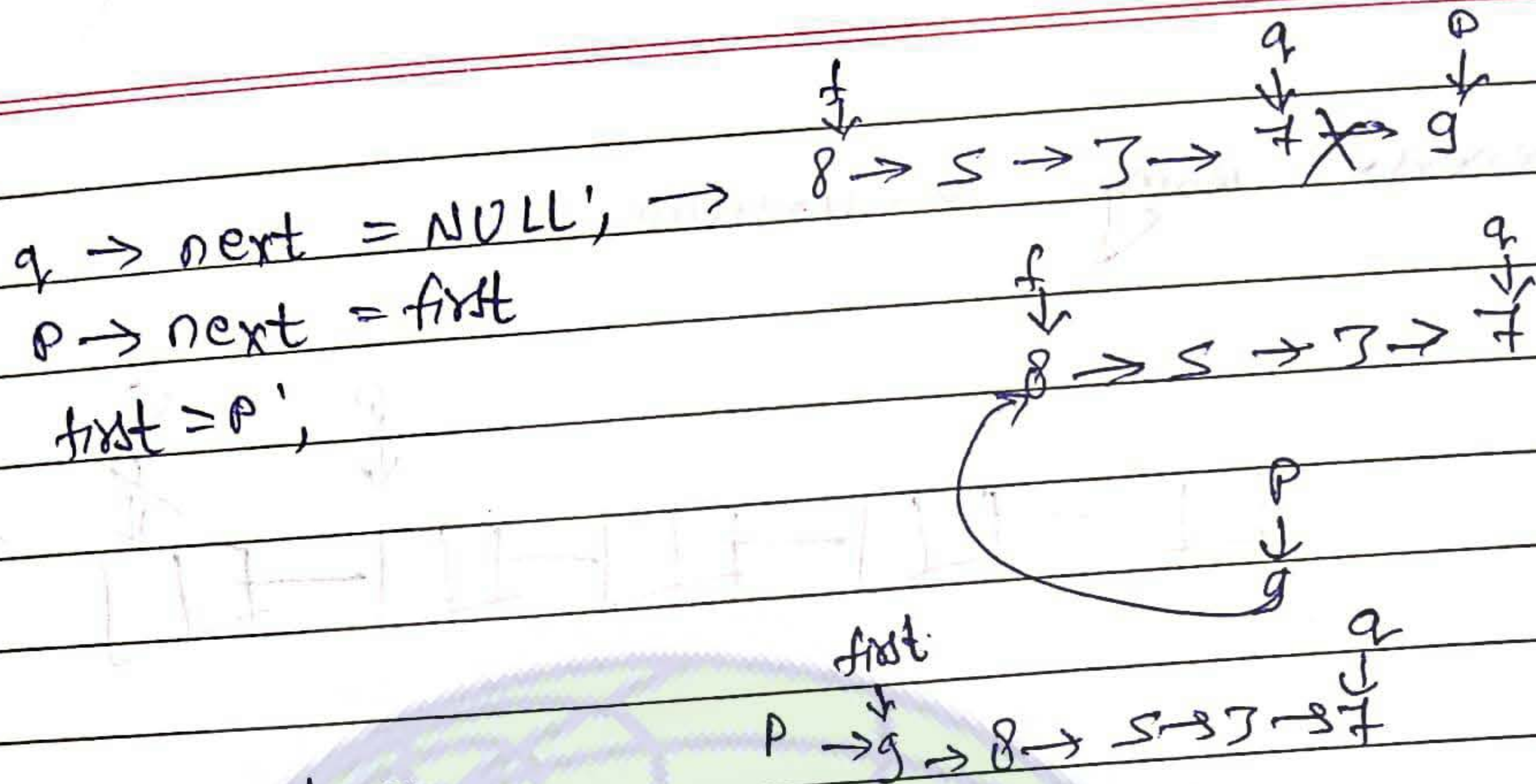
< >
p = first;
while ( p )
{
    q = p;
    p = p -> next;
}
    
```

// taking q till last node

```

< >
move to head
p = first;
while ( p -> next )
{
    q = p;
    p = p -> next;
}
    
```



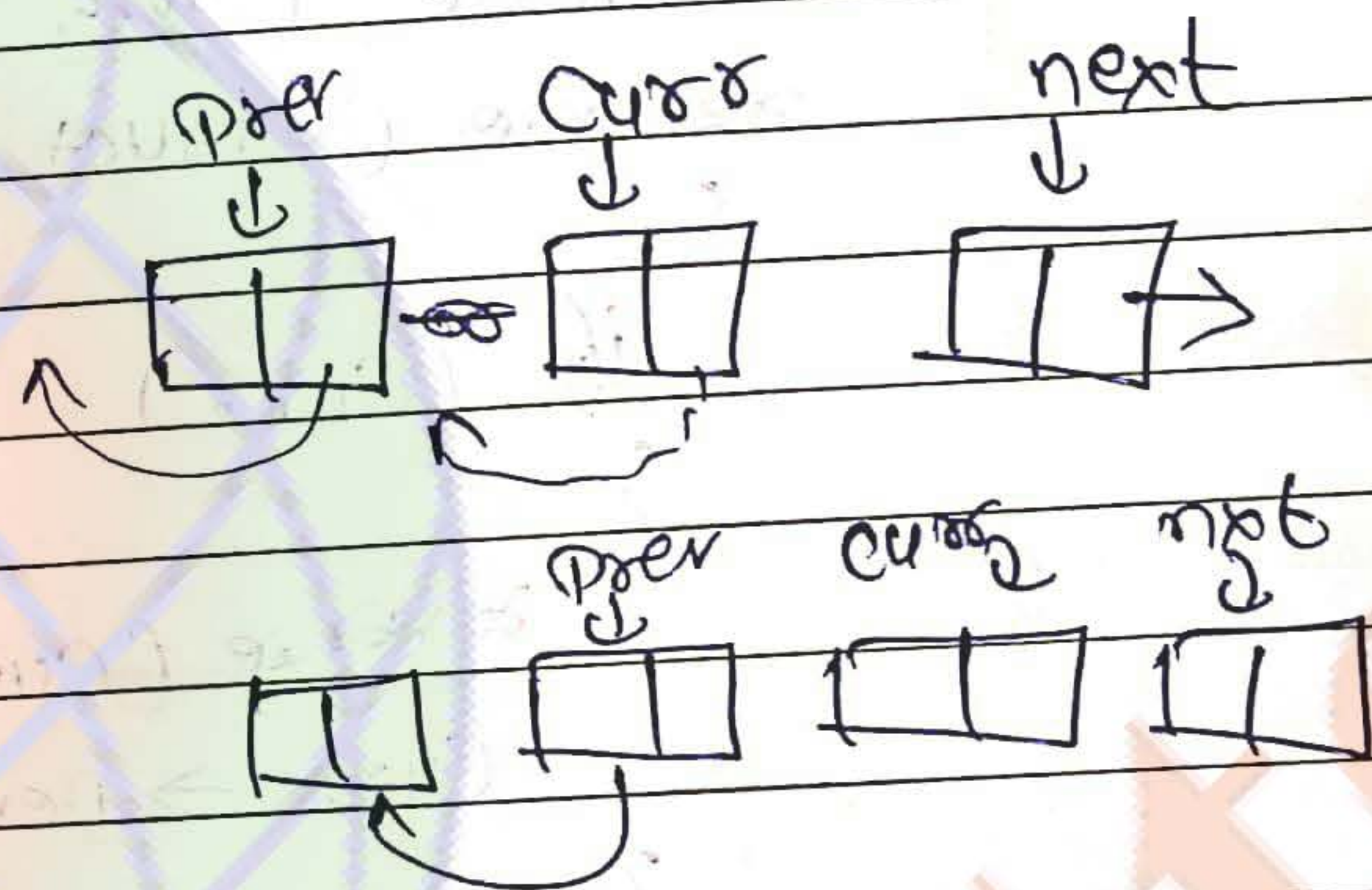


Reversing of link list -
 gate quest

```

prev = NULL;
curr = first;
next = first -> next;
while (curr != NULL)
{

```



```

    } curr -> next = prev;
    } prev = curr;
    } curr = next;
    } next = next -> next -> next = NULL;
}

```

first = prev;

or

```

prev = NULL;
curr = first;
next = first -> next;
while (next != NULL)
{

```

```

    } prev = curr;
    } curr = next;
    } next = next -> next;
}

```

```

    } curr -> next = prev;
    } first = curr;
}

```

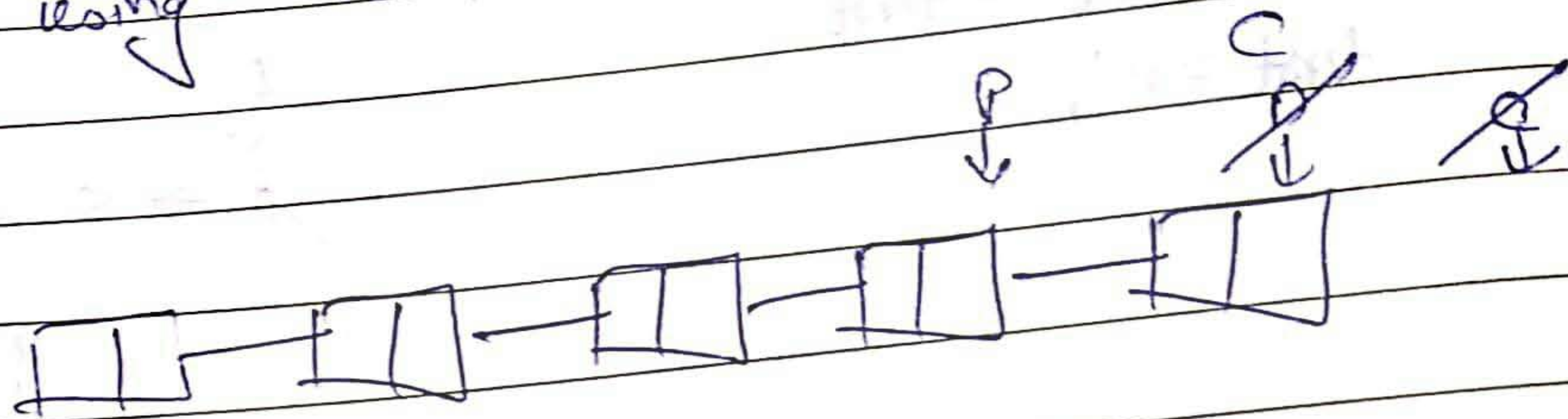
In terms of space,
 // loop is better

// Here firstly the sliding
 then reversing the
 link is taken place

// three pointers are
 required for
 reversal

(best)

* Reverse using recursion:-

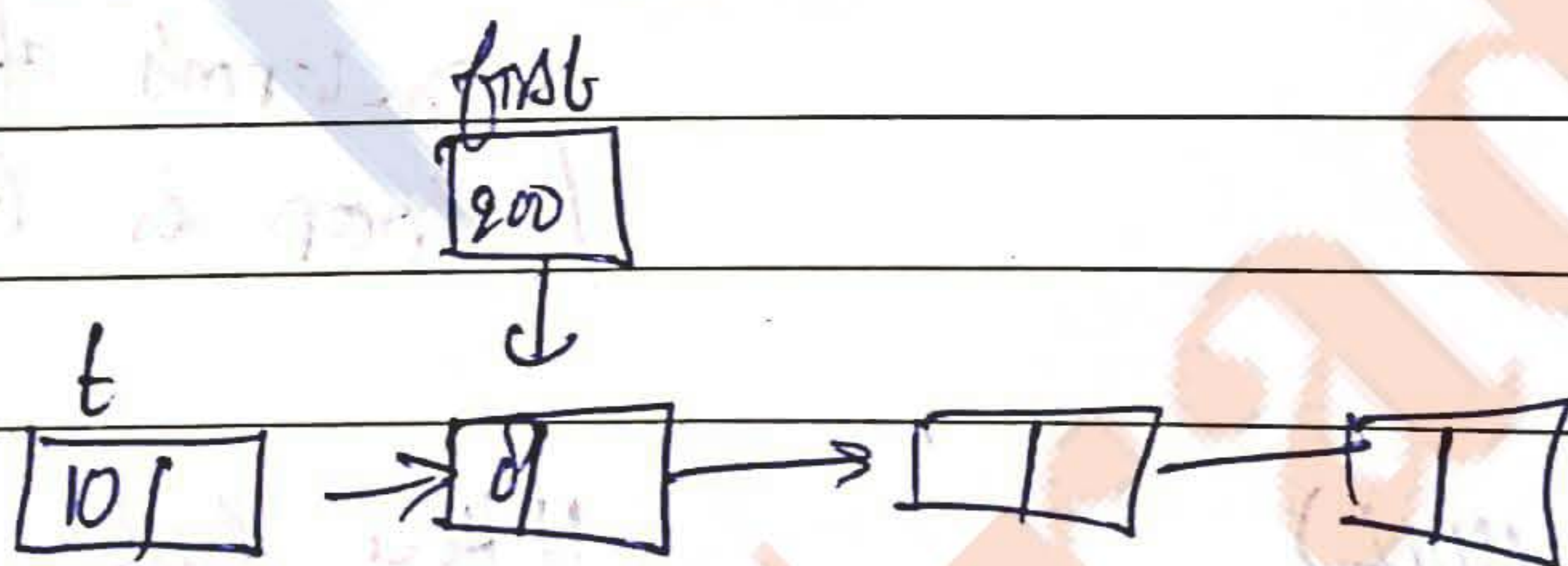


```
reverse (NULL, first);
reverse (struct Node * prev, struct Node * curr)
{
    if (curr)
    {
        reverse (curr, curr->next);
        curr->next = prev;
    }
    first = prev;
}
```

|| Two pointers are required.
Total points = 2x(n+1)

★ Insert operations:-

(1) Inserting before 1st node:-

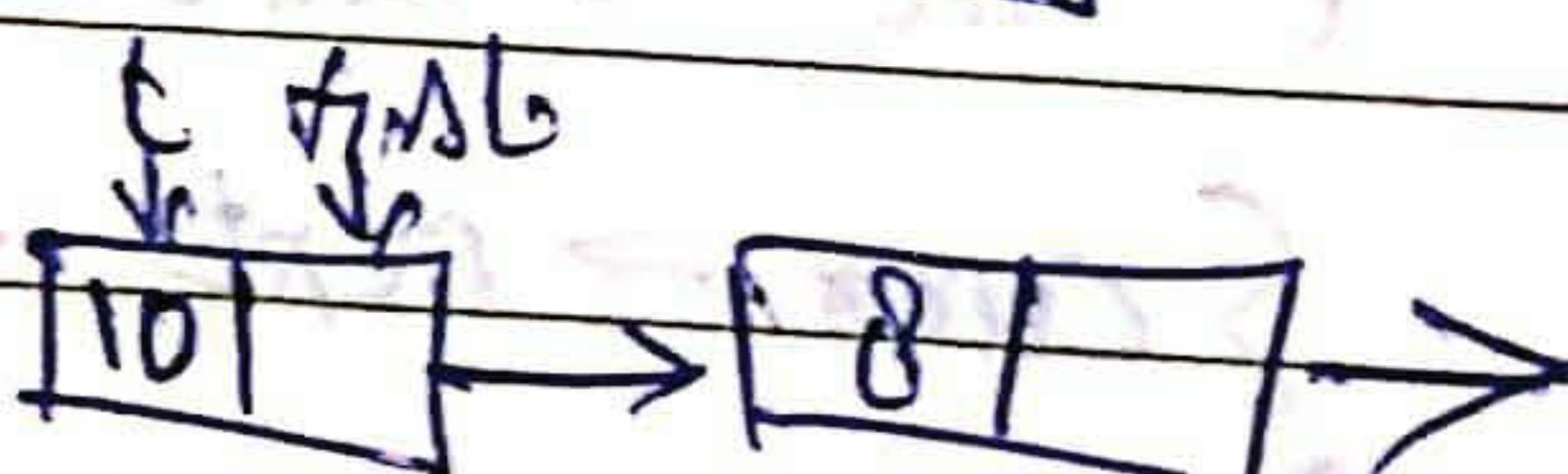
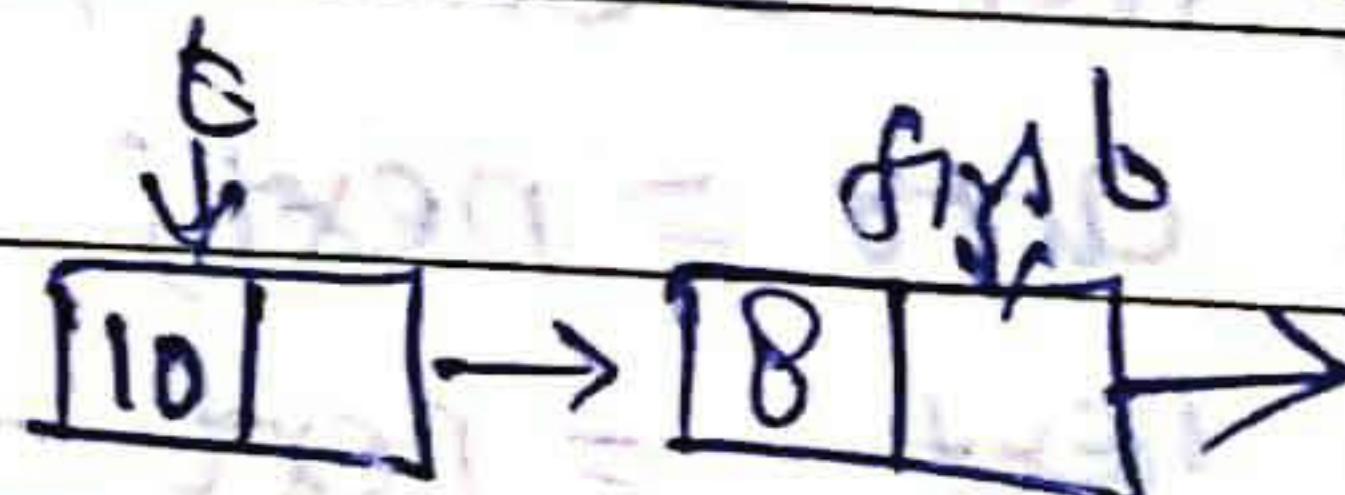


f(n)=4
O(1)
O(n)

t = new node;
t->data = x;

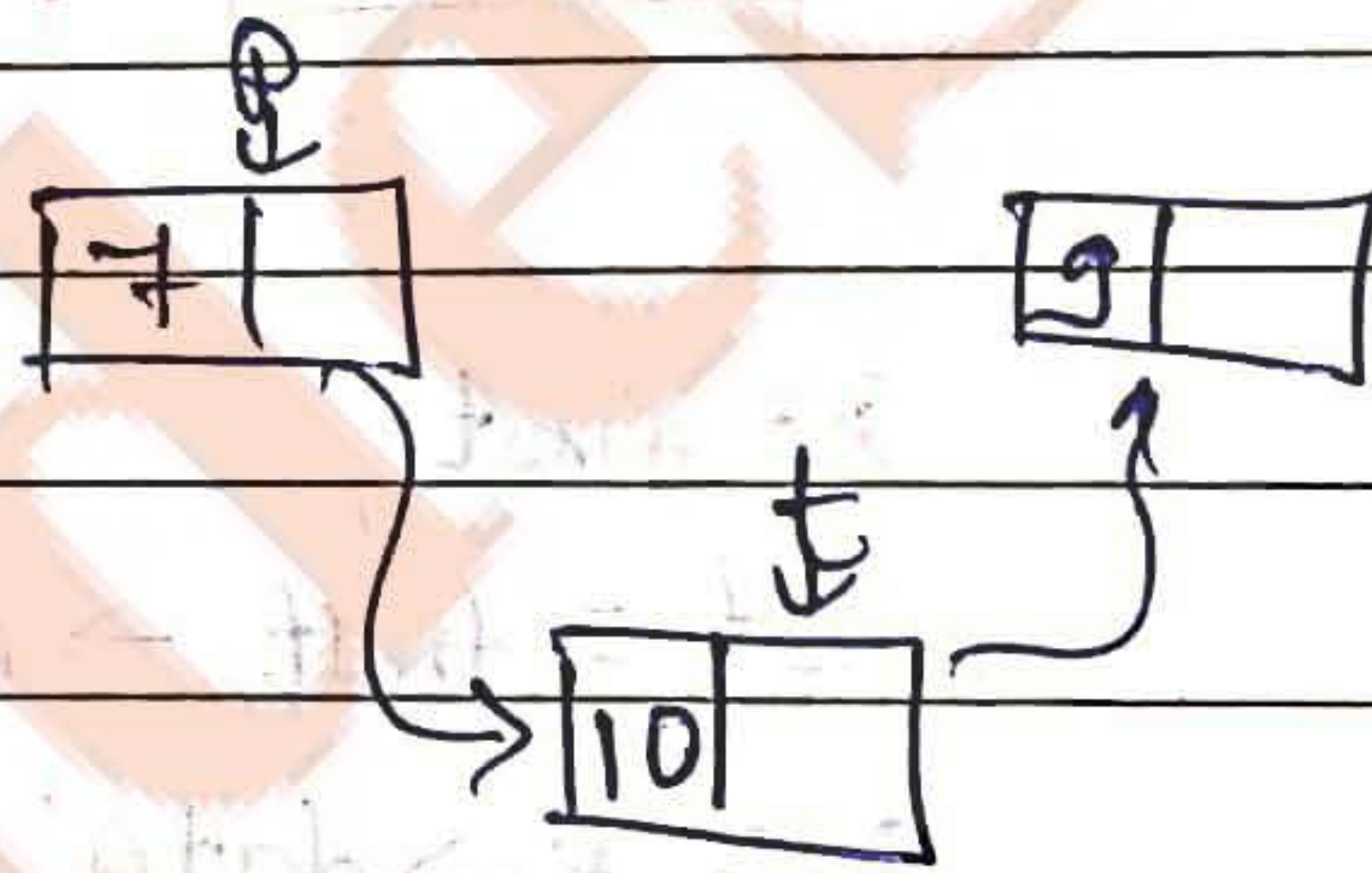
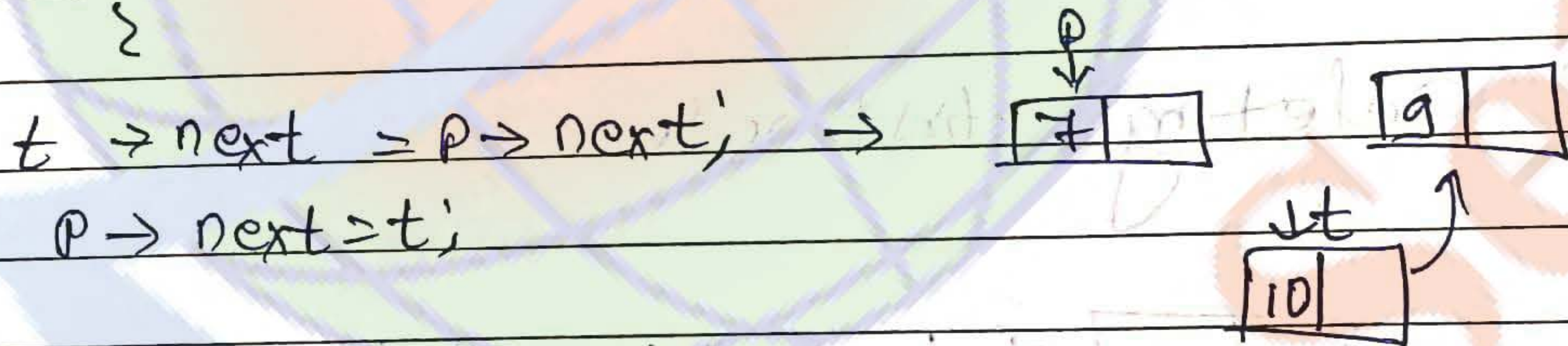
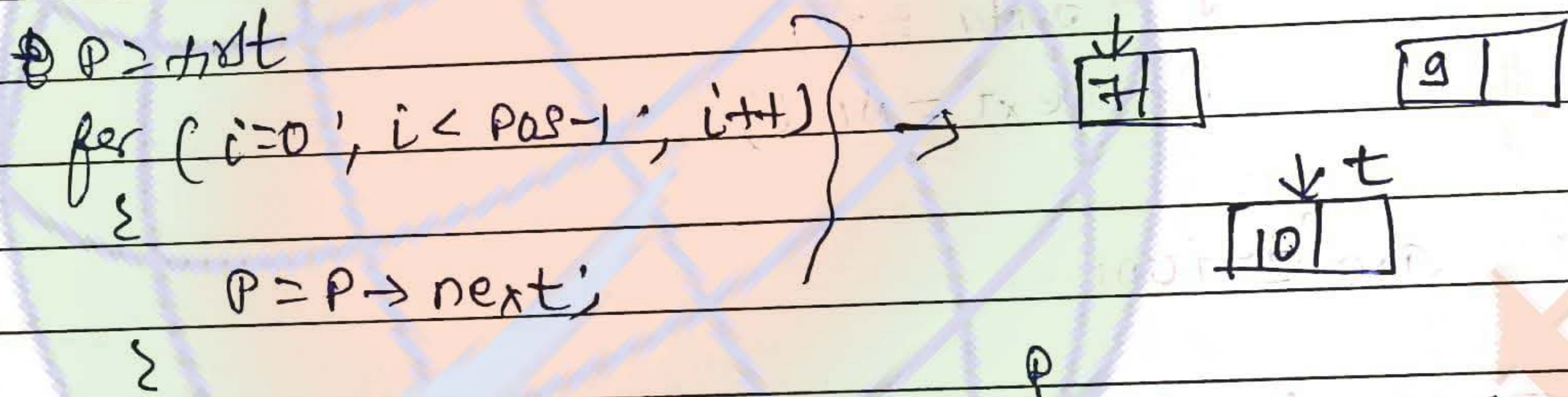
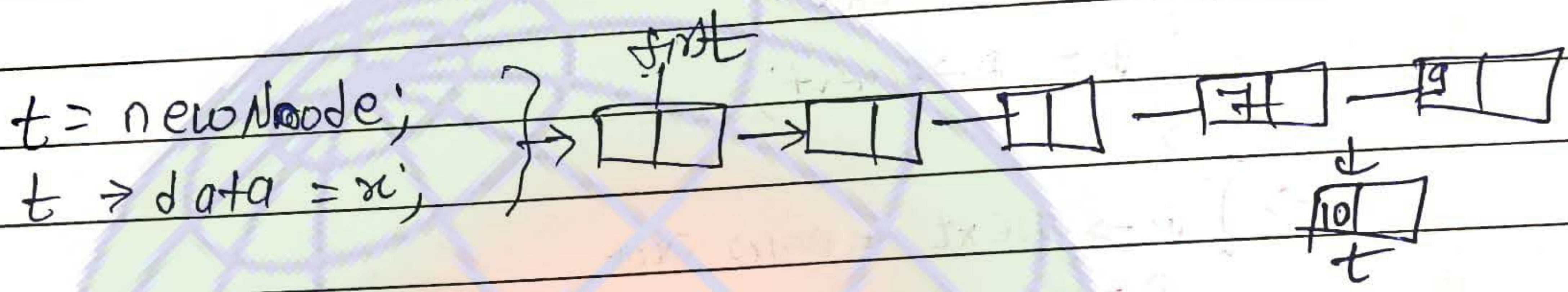
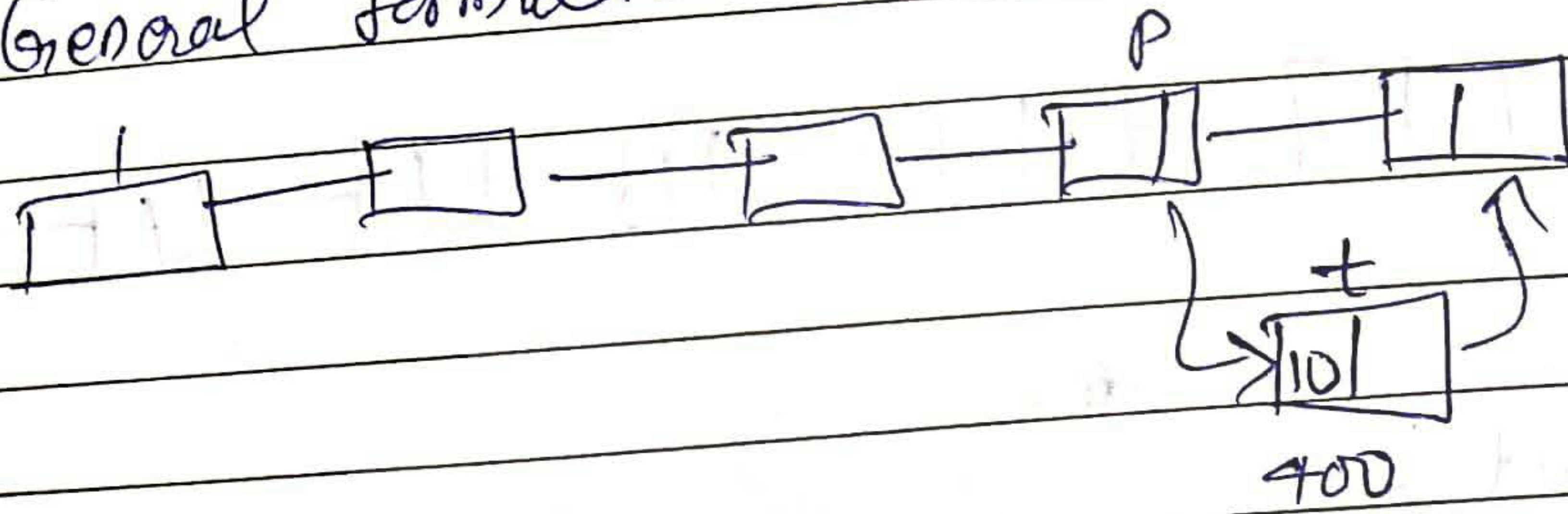
t->next = first;

first = t;



|| one extra pointer is required.

27 General formula:-



// two extra pointer is requires here

P → for links

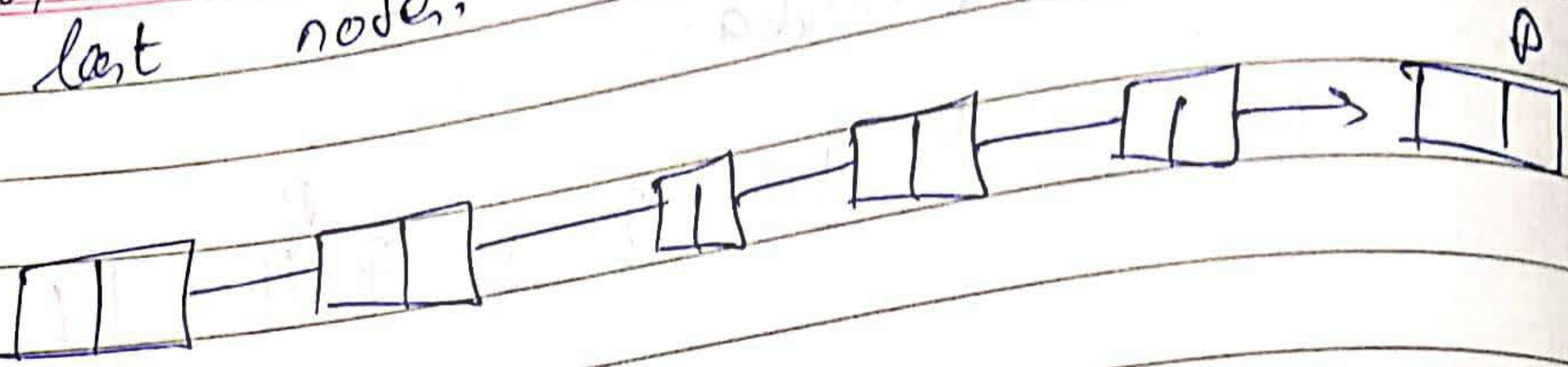
t = for creating new nodes.

//time! O(n)

Notes

This will also work on adding nodes on the last node.

3.7 Insertion
At last node.



(2)

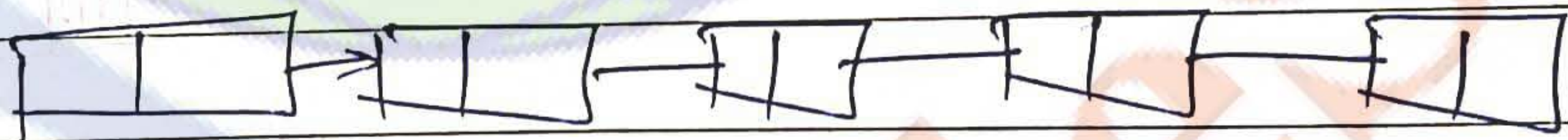
```

first = P
while (P -> next)
{
    P = P -> next;
}
-> [ P -> next = new node;
    P = P -> next;
    P -> data = x;
    P -> next = NULL;

```

★ Deletion: -

① Deleting first node.

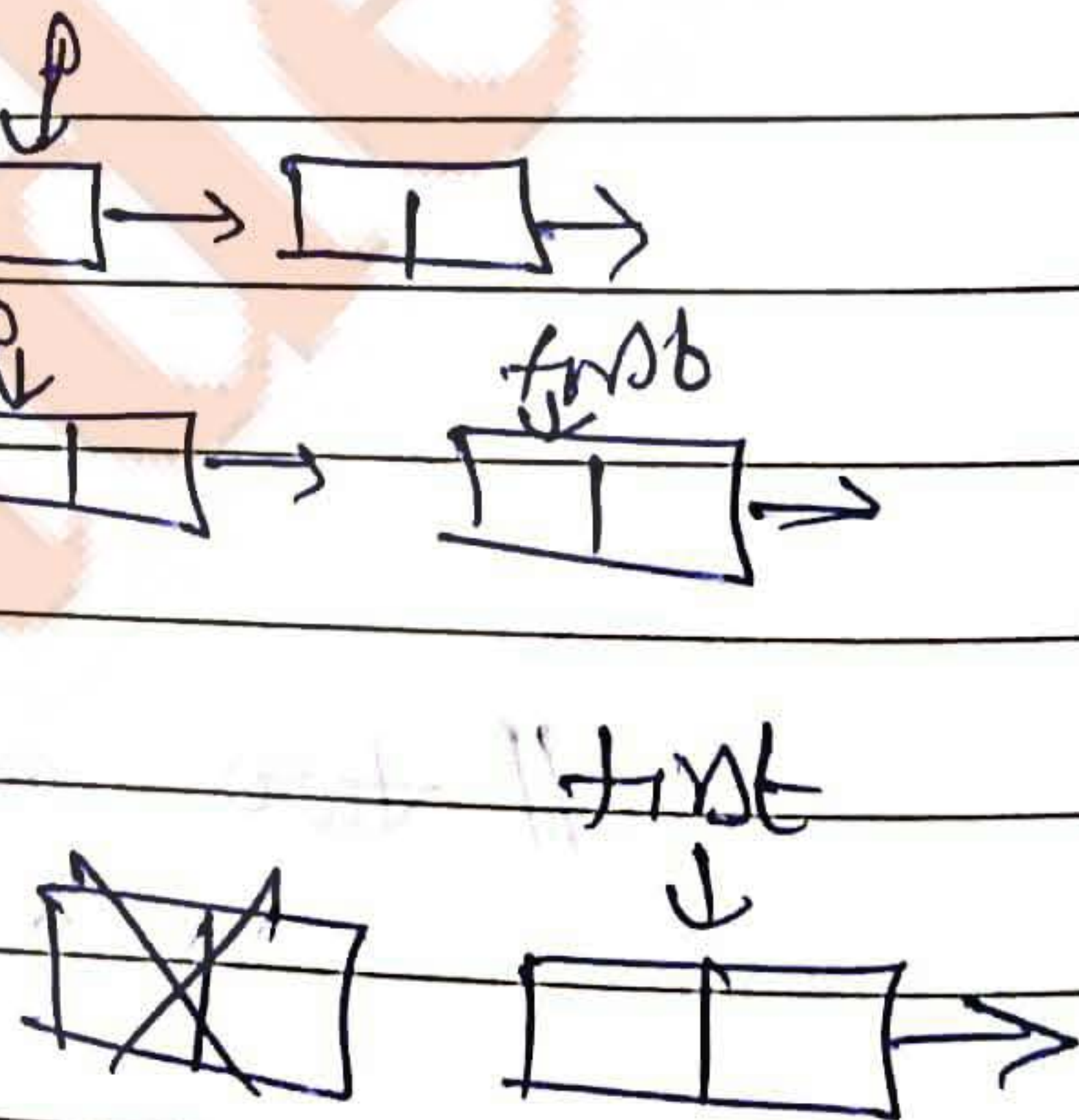


```

P = first;
first = first -> next;
x = P -> data;
free(P);

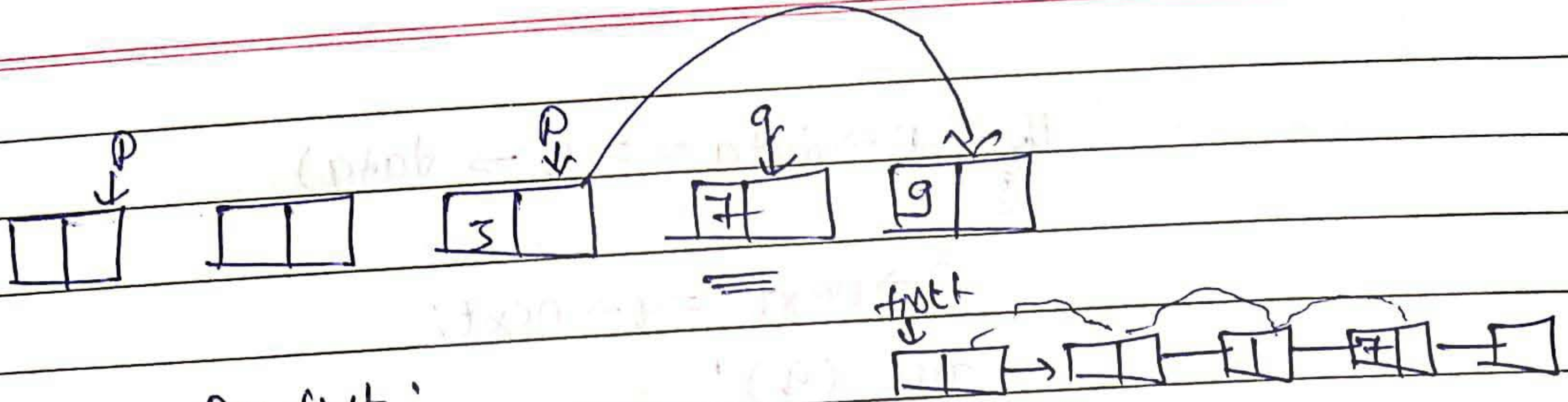
```

delete का मतलब value निकालना है फंक्शन ही!



// one extra pointer is required
// O(1) ← time

(2)



$p = \text{first};$

$\text{for } (i=0, i < \text{pos}-2; i++)$

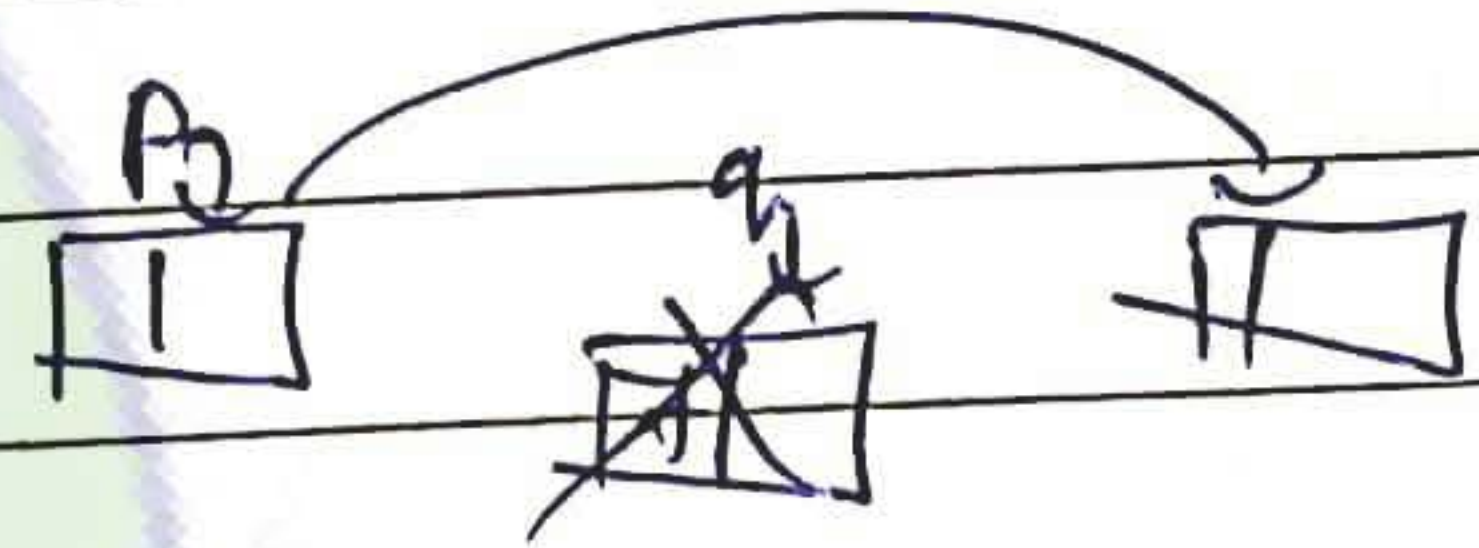
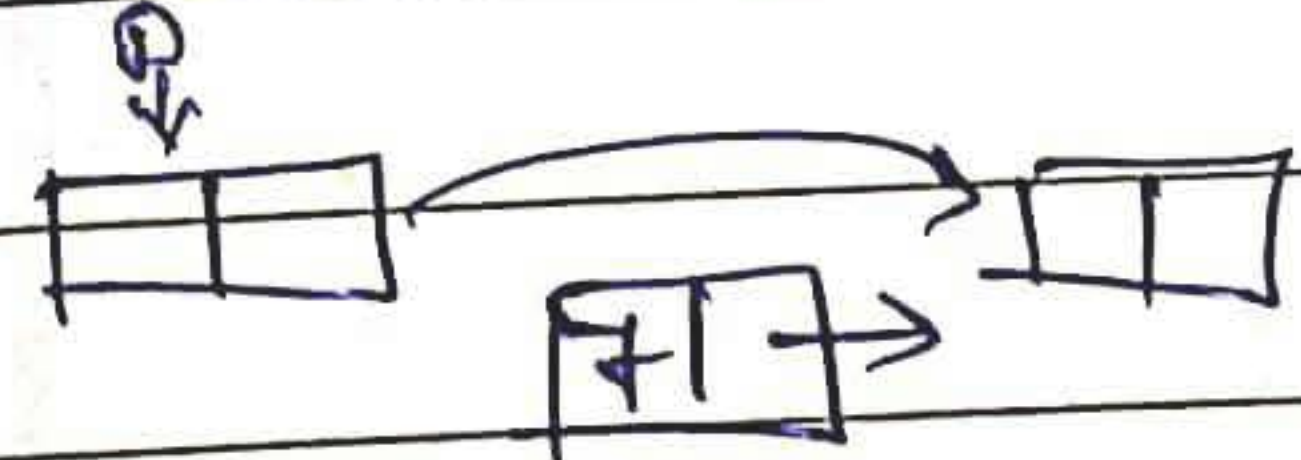
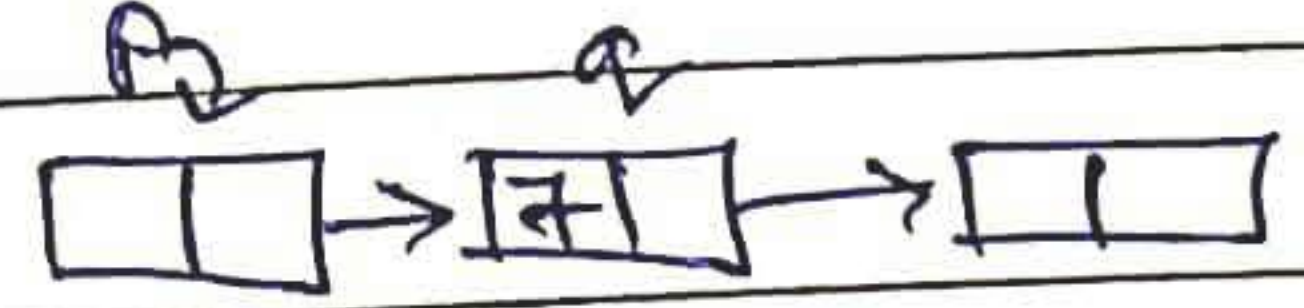
$p = p \rightarrow \text{next};$

$q = p \rightarrow \text{next};$

$p \rightarrow \text{next} = q \rightarrow \text{next};$

$x = q \rightarrow \text{data};$

$\text{free}(q);$



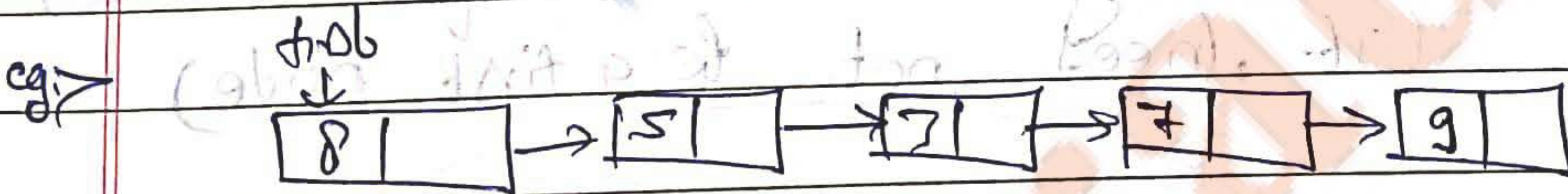
// No. of pointers = 2 ✓

// time : $O(n)$ → Here 'n' is position.
(Linear) ✓

// links modified = 1

3x / last node

Note: First node, second node and last node can be deleted using single pointer.



// This case will delete duplicates from sorted linked list

3 → 5 → 5 → 10 → 12 → 12 → 12 → 16 → 16 → 20

func ()

{

$p = \text{first};$

$q = \text{first} \rightarrow \text{next};$

$\text{while } (p \neq q)$

{

```

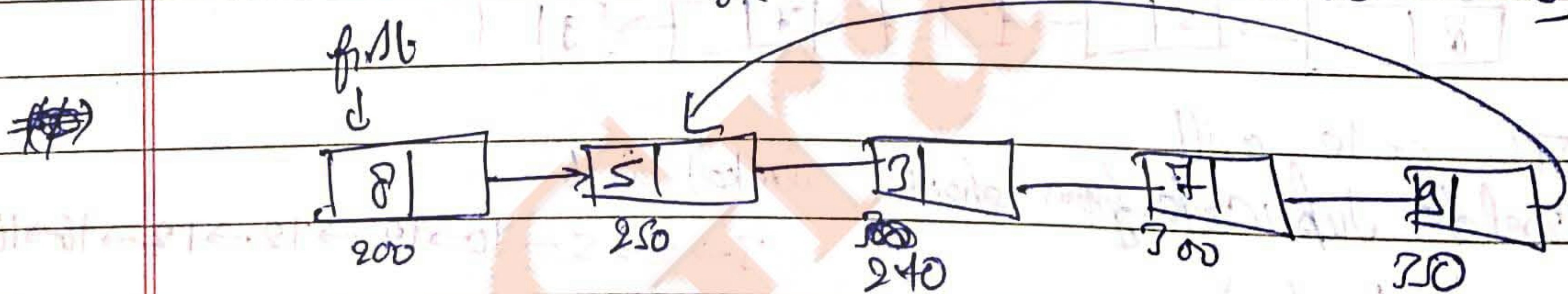
if (P->data == q->data)
{
    P->next = q->next;
    free(q);
    q = P->next;
}
else
{
    P = q;
    q = q->next;
}
}
}
}
    
```

// time: $O(n)$

★ Circular linked list.

① ★ Loop:-

If last node ~~with its pointer~~ is pointing on any other nodes of a linked list, (need not be a first node)



② Algorithm for finding, the given linked list is linear or having the loop.

(a) store the address of newly visited nodes and

if it becomes null

check where the nodes e_i are visited or not
time = $O(n^2)$

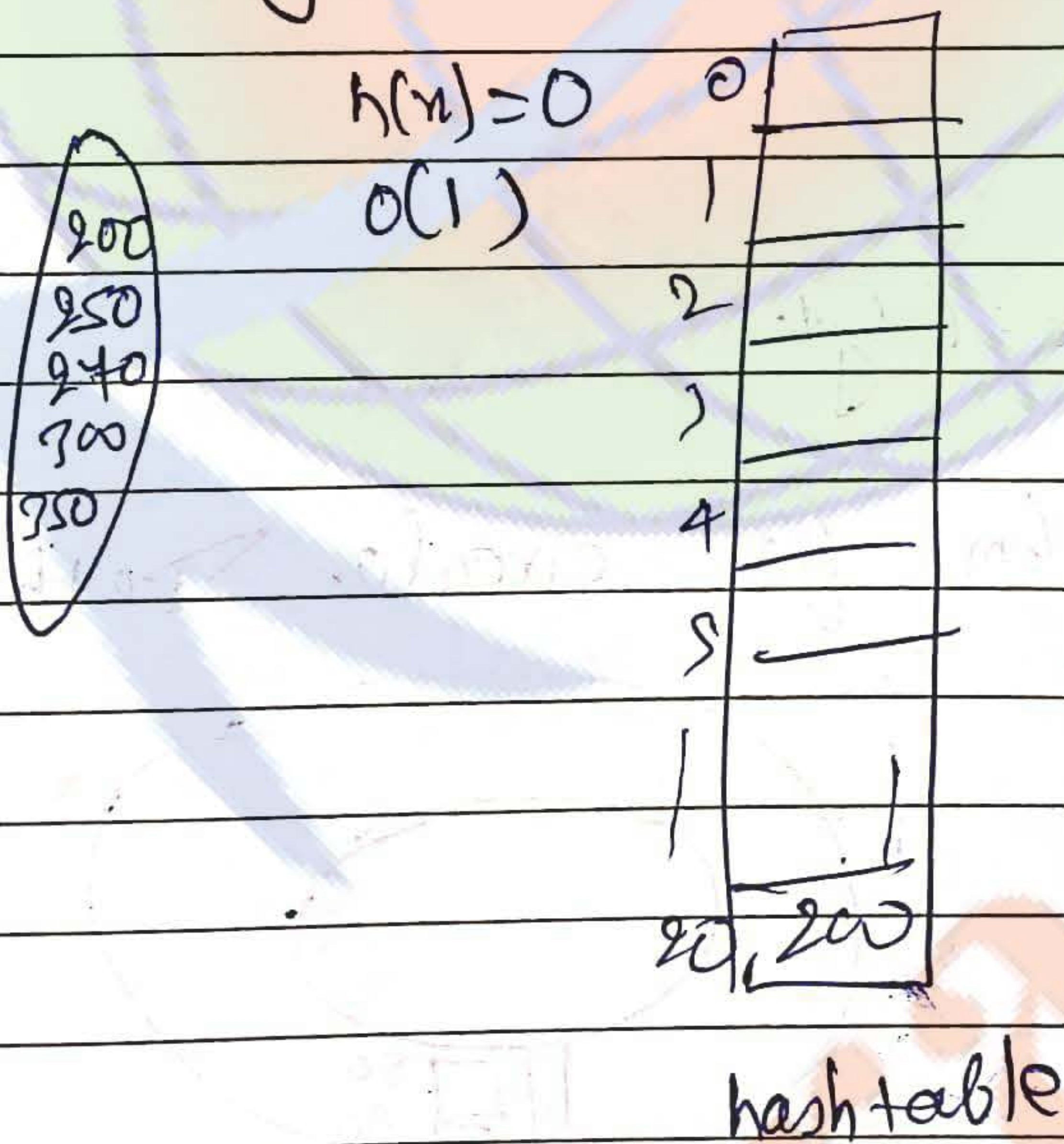
Addr	200	250	240	300	350
------	-----	-----	-----	-----	-----

n nodes
searching for n nodes:
 linear $O(n)$ binary search $O(\log n)$
 (apply on only sorted order)

Note: If we know that the addresses are in sorted order, then we will use binary $O(n \log n)$

~~Hash~~ Hash tables -

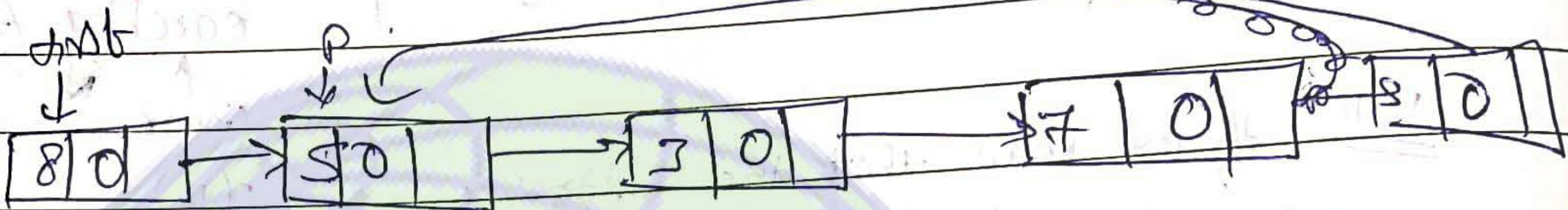
(b) Hashing



// time : $O(n)$

Note:

$n \times n \rightarrow$ linear
 $n \times \log n \rightarrow$ Binary, doesn't mean address should be sorted
 $n \times 1 \rightarrow$ Hash, doesn't mean hashing consumes lot of space

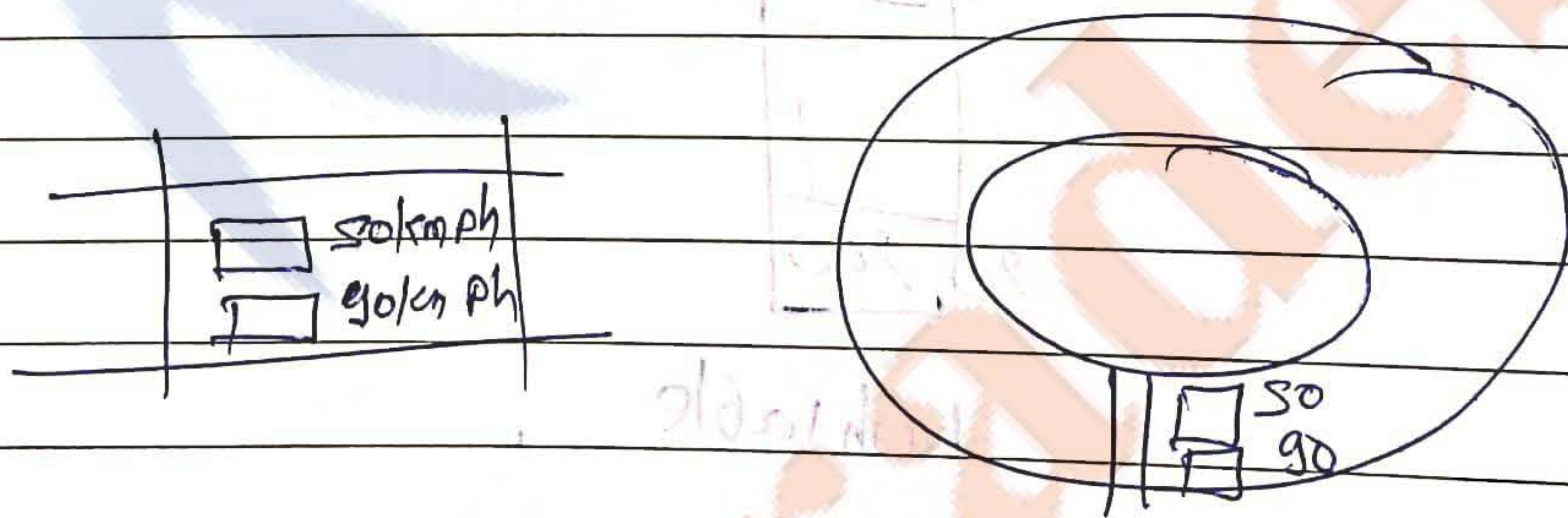


```

struct Node
{
    int data;
    struct Node * next;
    int flag;
};
    
```

size = 6 byte

(d) Floyd's algorithm for circular path:-



// time: $O(n)$

// one pointer is faster and the other is slower, and if circular, they will meet at one time //

If ~~next~~ \rightarrow null, it means linear.

```
p = q = first;
```

```
do
```

```
{
```

```
  p = p -> next;
```

```
  q = q -> next;
```

```
  q = q != q -> next : q;
```

```
} while (p != q && p && q);
```

```
if (p == q)
```

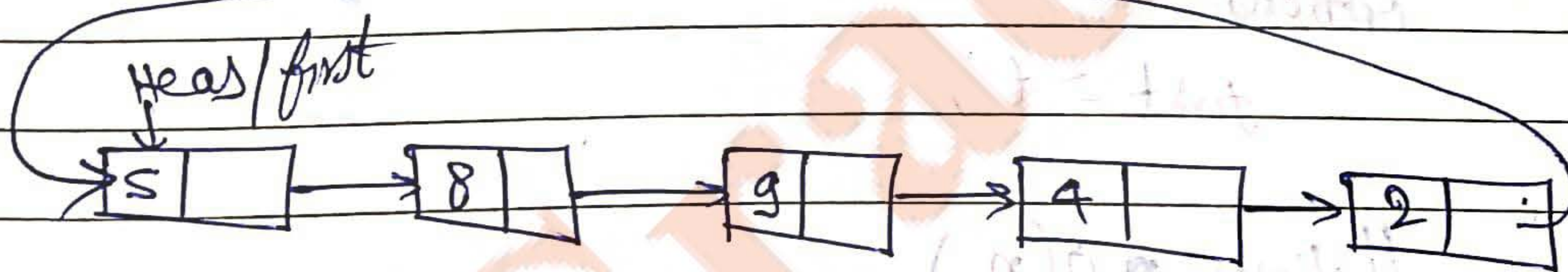
```
  pf ("Loop");
```

```
else
```

```
  pf ("Linear");
```

* Circular linked list:-

- circular linked list is a loop where last node is pointing on first node.



```
p = first
```

```
do
```

```
{ printf ("%d", p -> data);
```

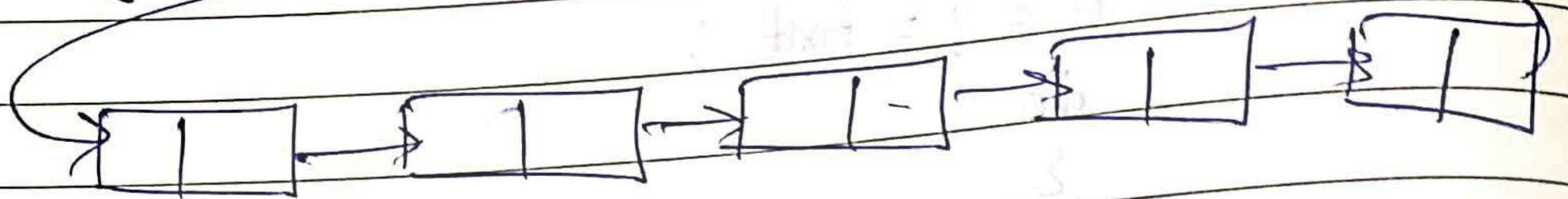
```
  p = p -> next;
```

```
}
```

```
while (p != first);
```

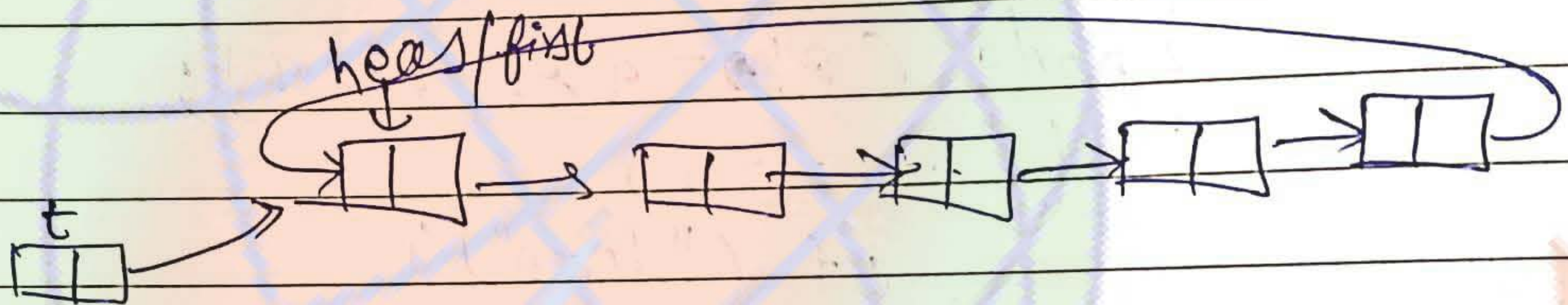
(a) Insertion:

(1) Inserting a node after given position



// procedure is same as inserting in a linear linked list.

(b) Inserting before head node:



```

P = first;
while (P->next != first)
    P = P->next;
t = new node;
t->data = x;
t->next = first;
P->next = t;
    
```

optional
first = t;

// time: $O(n)$

(c) Inserting after first node takes constant time.

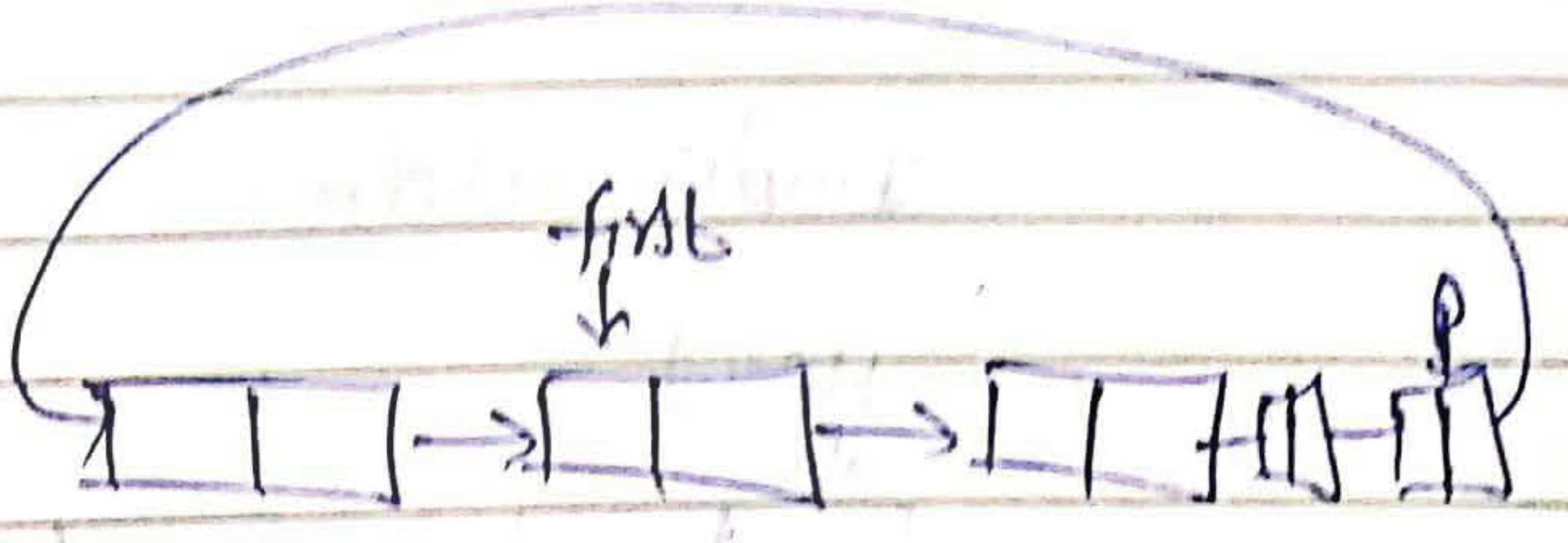
(2) Deletion:

(a) // procedure is same as linear linked list

(b) Deleting first nodes:-

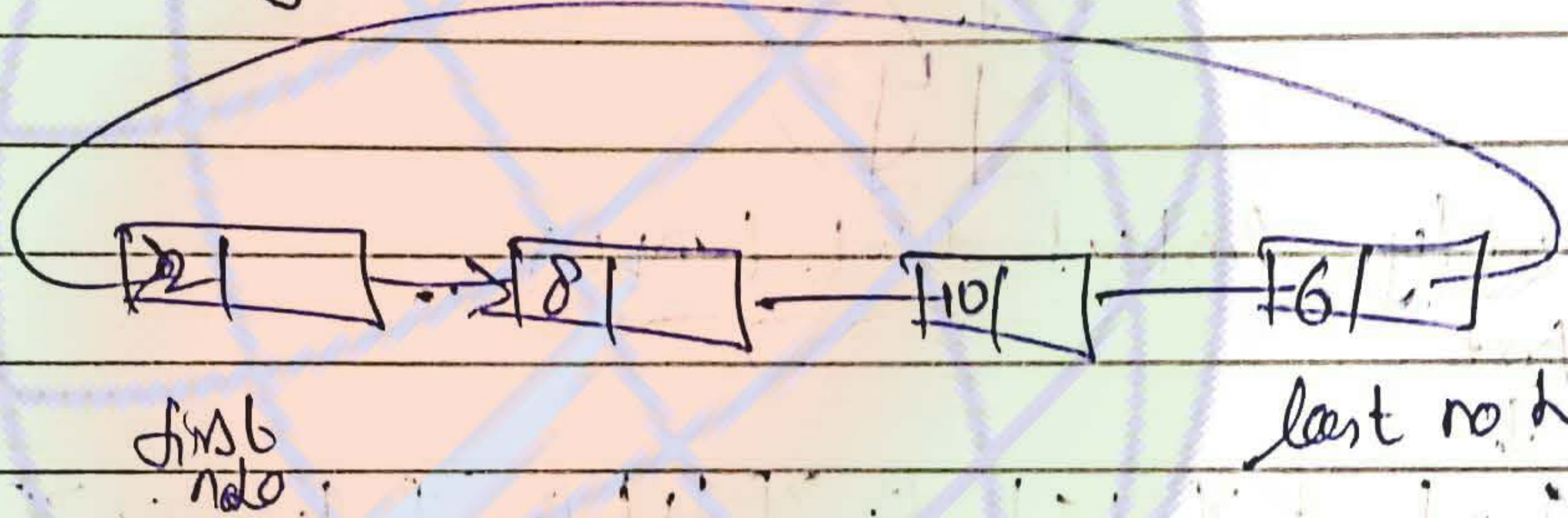
```

P = first;
while (P != first)
{
    P = P->next;
    X = first->data;
    first = first->next;
    free (P->next);
    P->next = first;
}
    
```

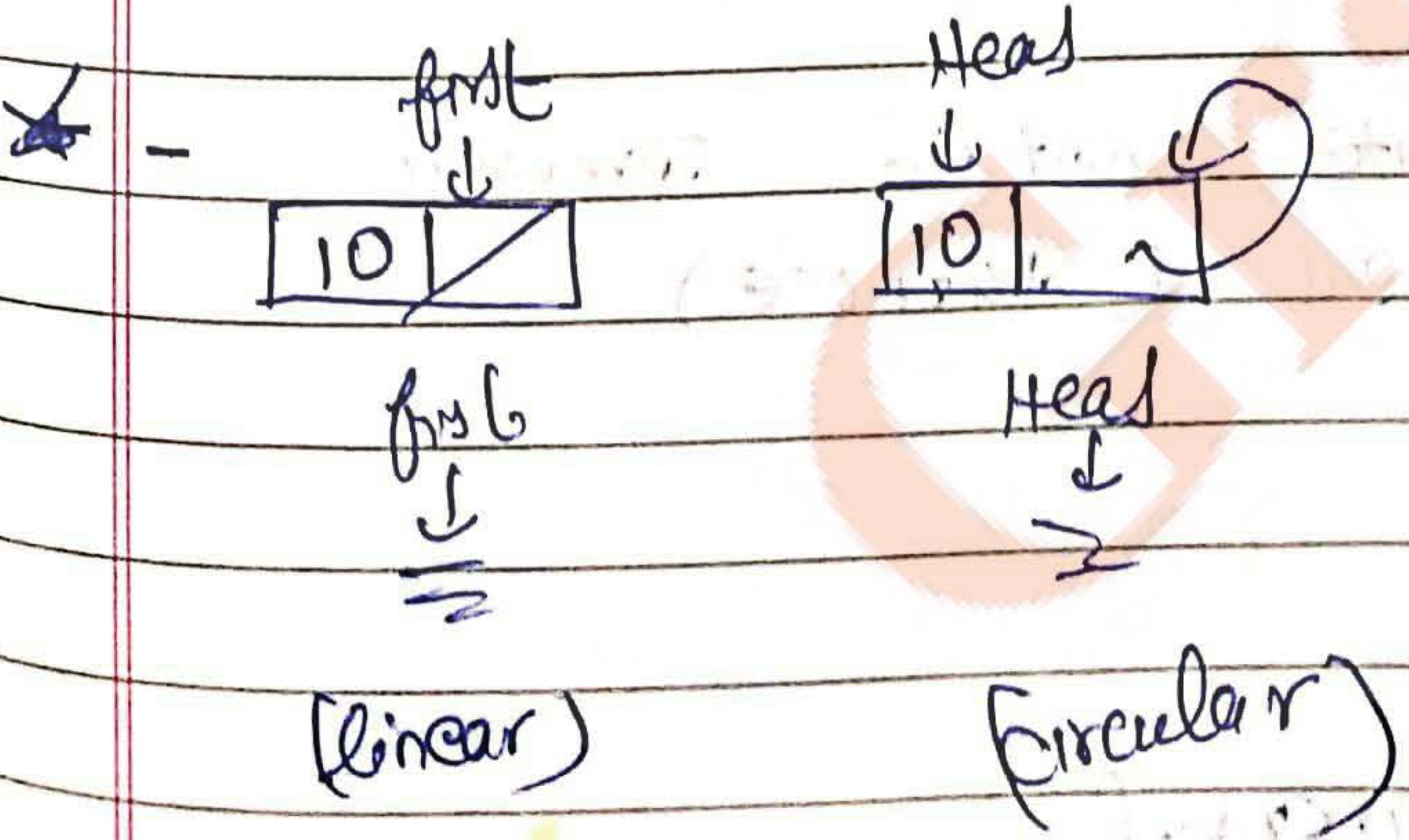


(c) ~~Deleting~~ Deleting after first nodes takes constant time.

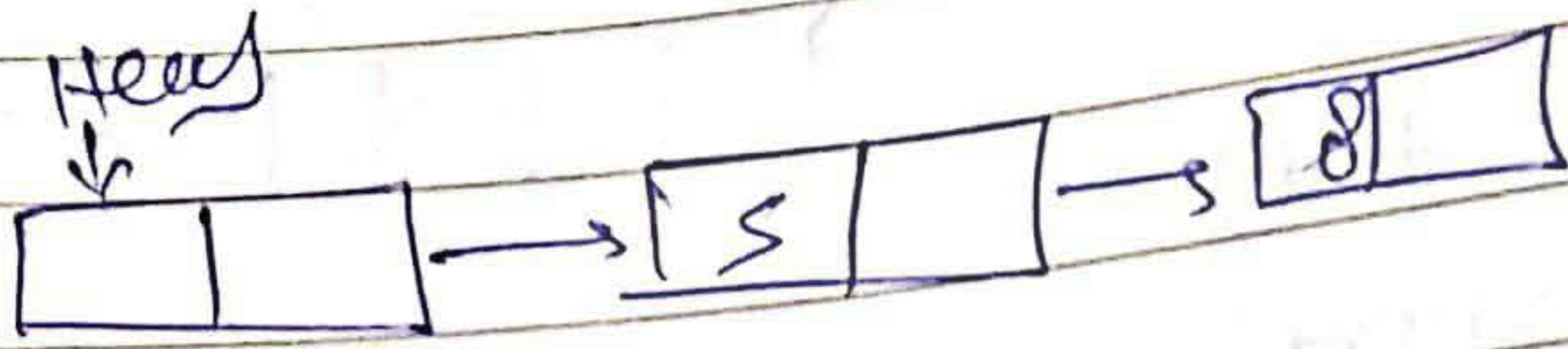
gate



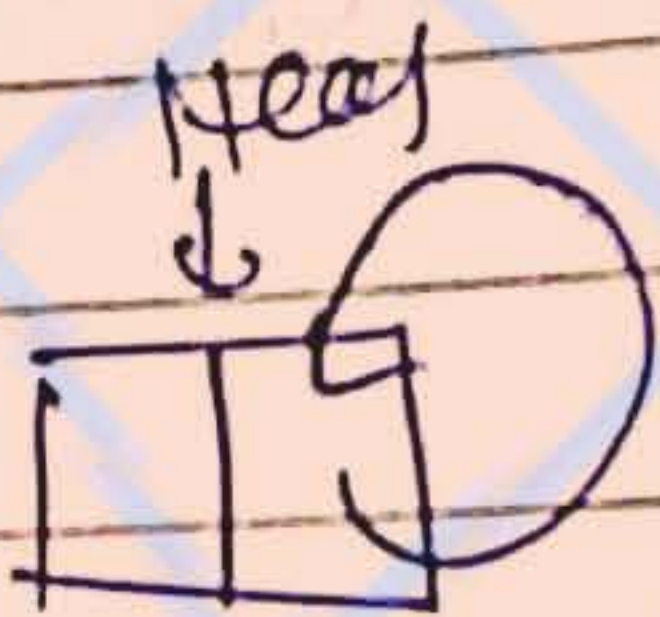
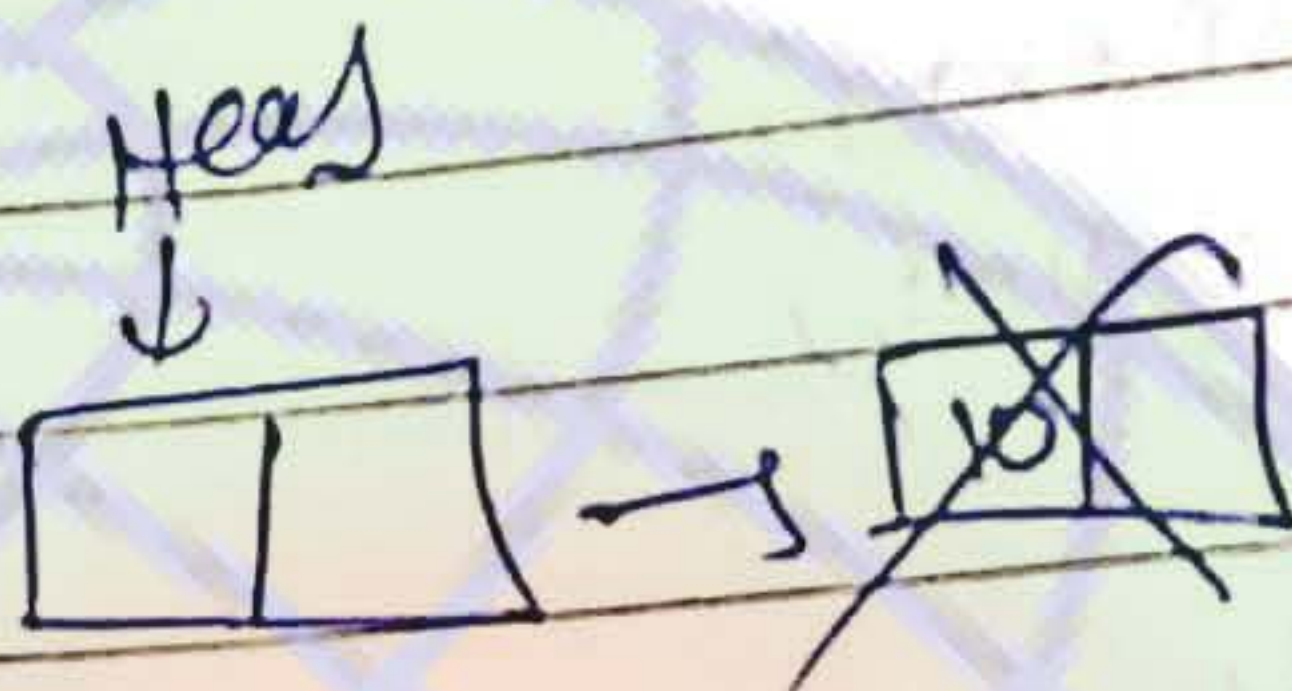
- If a circular linked list is used for implementing
- linked list is already having some elements
- there are no pointers on linked list.
- If a pointer p is given, then where it should point such insertion and deletion in a queue takes constant time



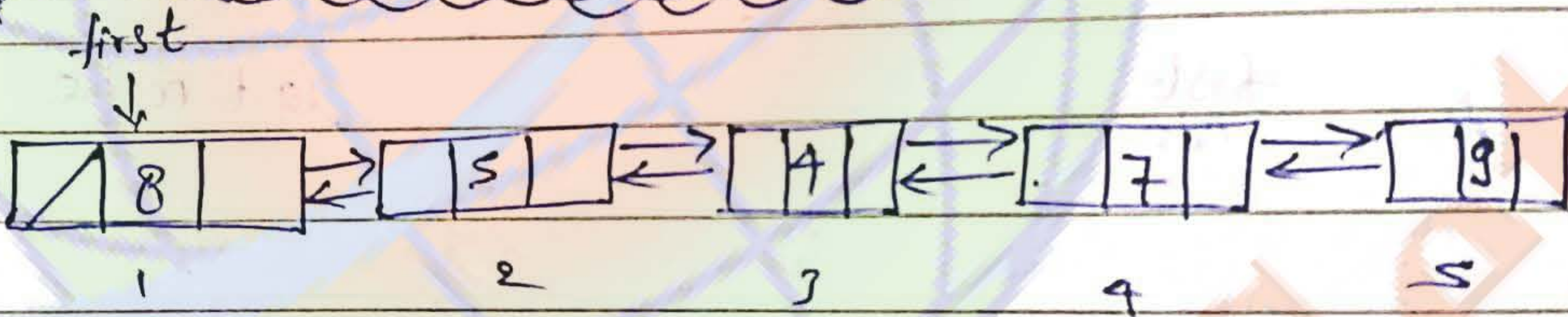
Implementation:



(enter head)



Doubly linked list (DLL)

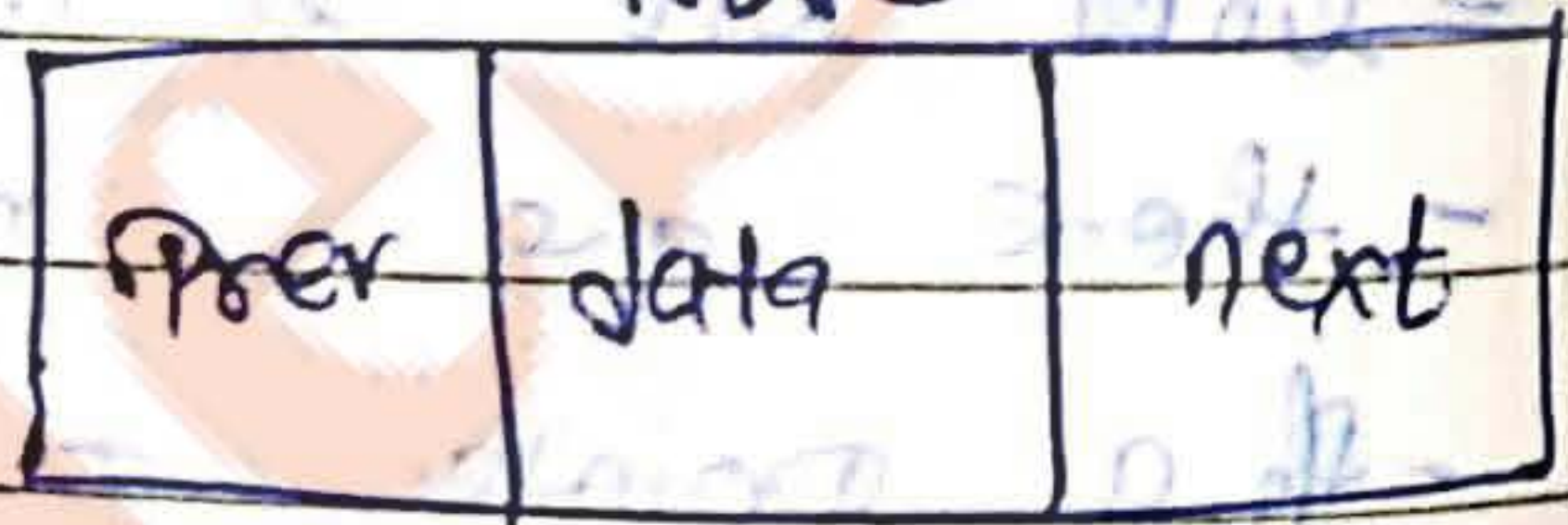


Struct Node

```

    struct Node {
        struct Node *prev;
        int data;
        struct Node *next;
    };
    
```

Node



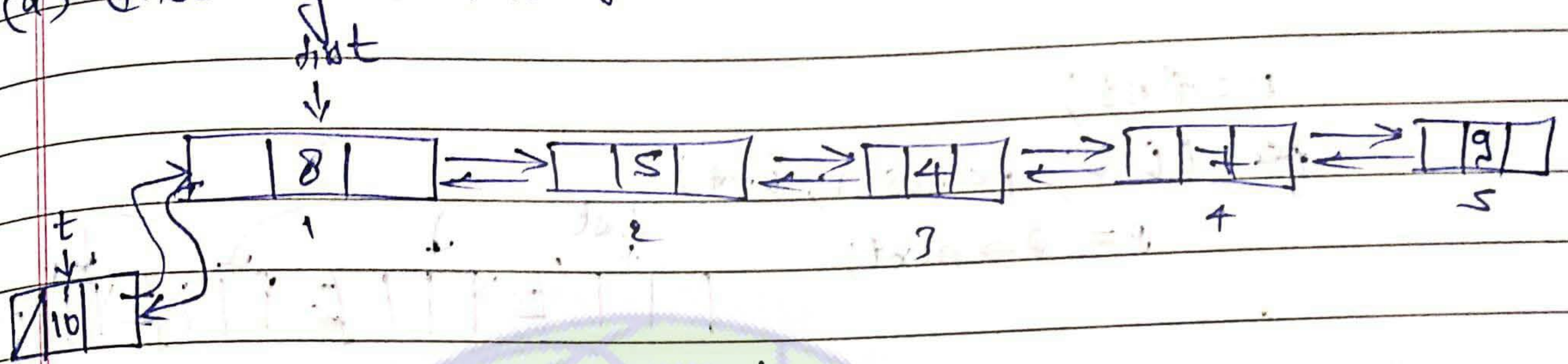
- Every node will ~~code~~ point to previous
- Bidirectional traversal (purpose)

Note:

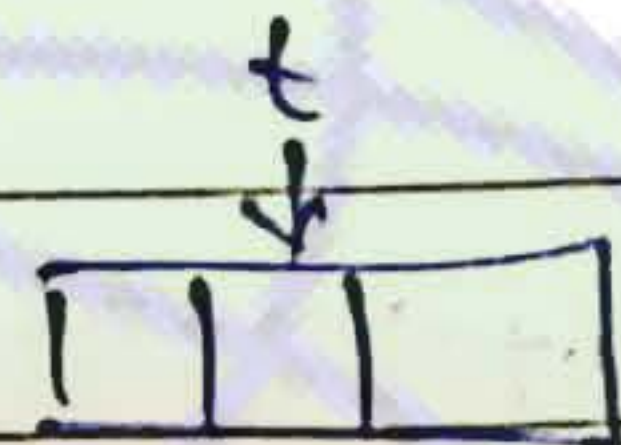
circular link list
 ↓
 purpose
 ↓
 circular traversal

(i) Insertion:-

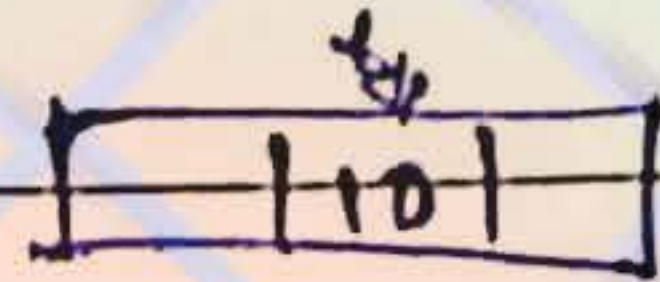
(a) Inserting at first position:-



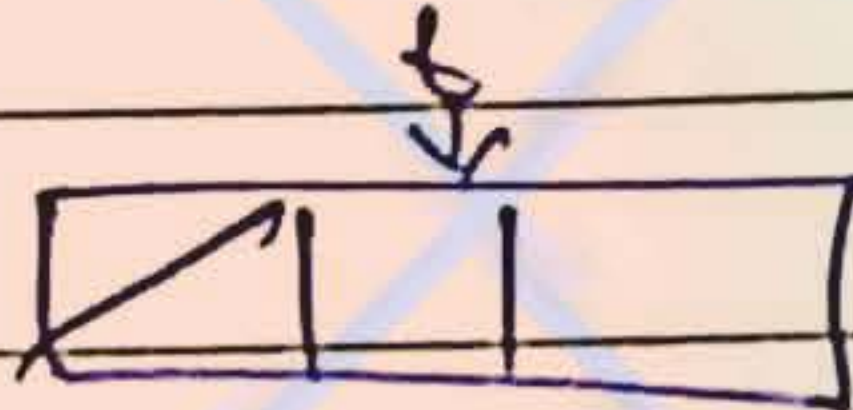
$t = \text{new Node}$;



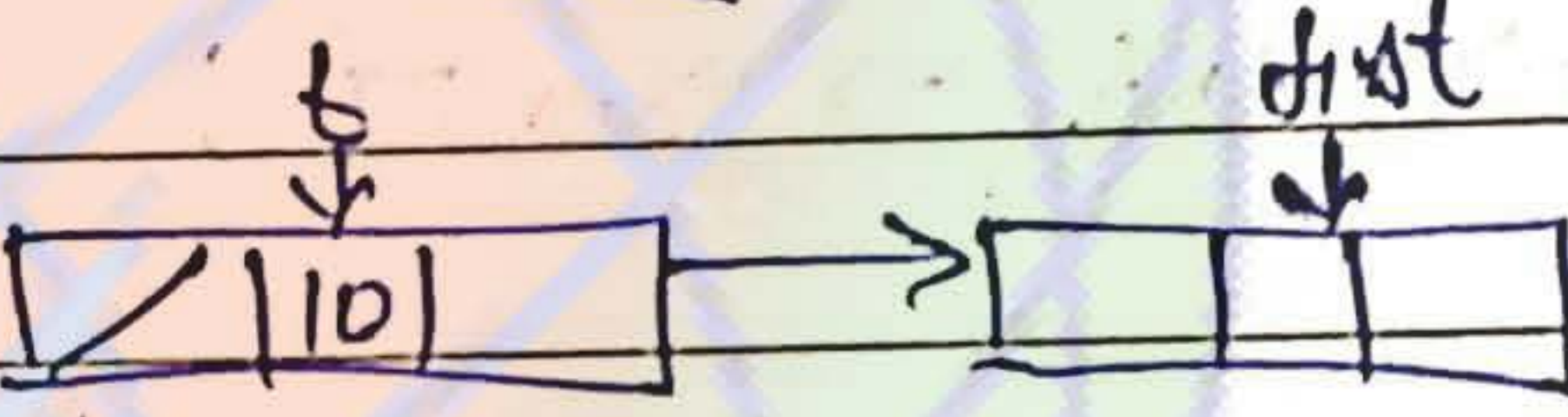
$t \rightarrow \text{data} = n$;



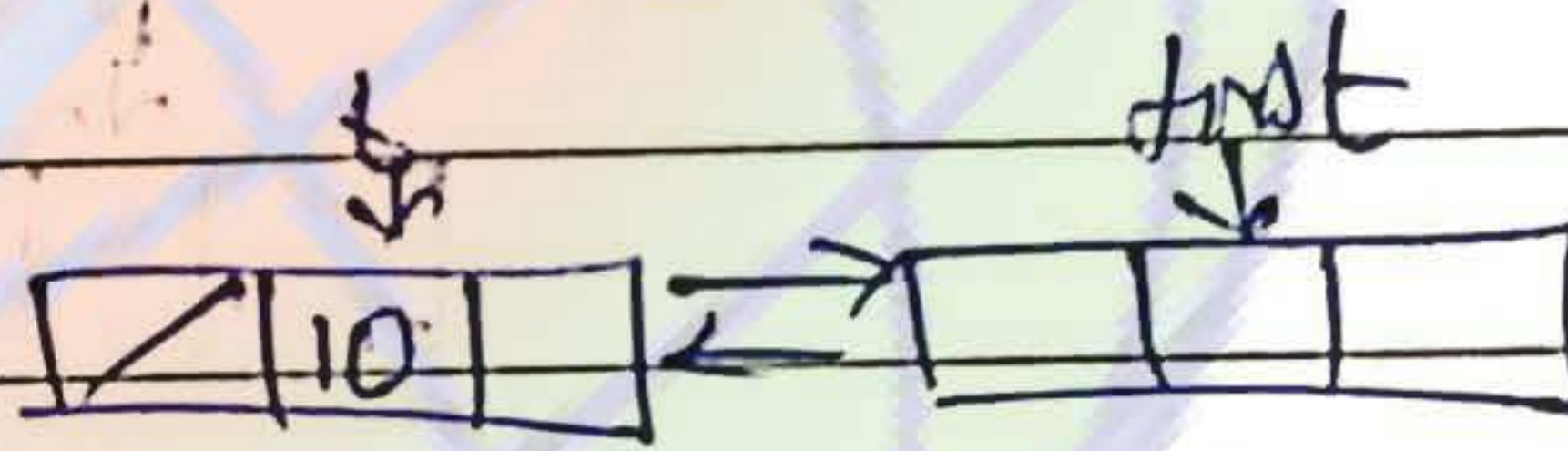
$t \rightarrow \text{prev} = \text{NULL}$;



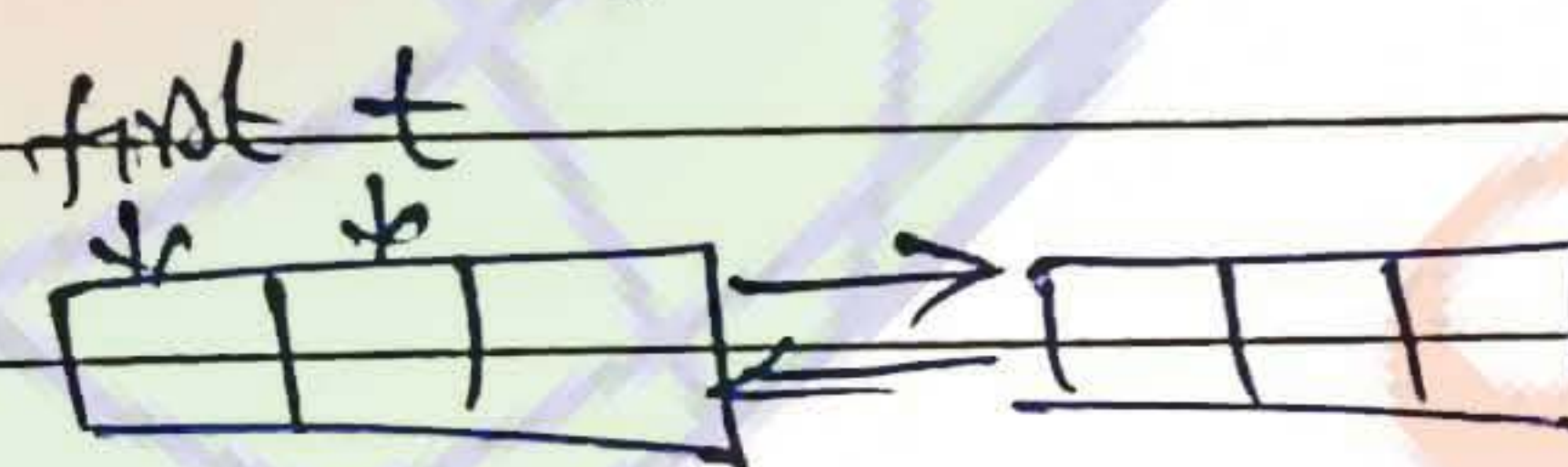
$t \rightarrow \text{next} = \text{first}$;



$\text{first} \rightarrow \text{prev} = t$;



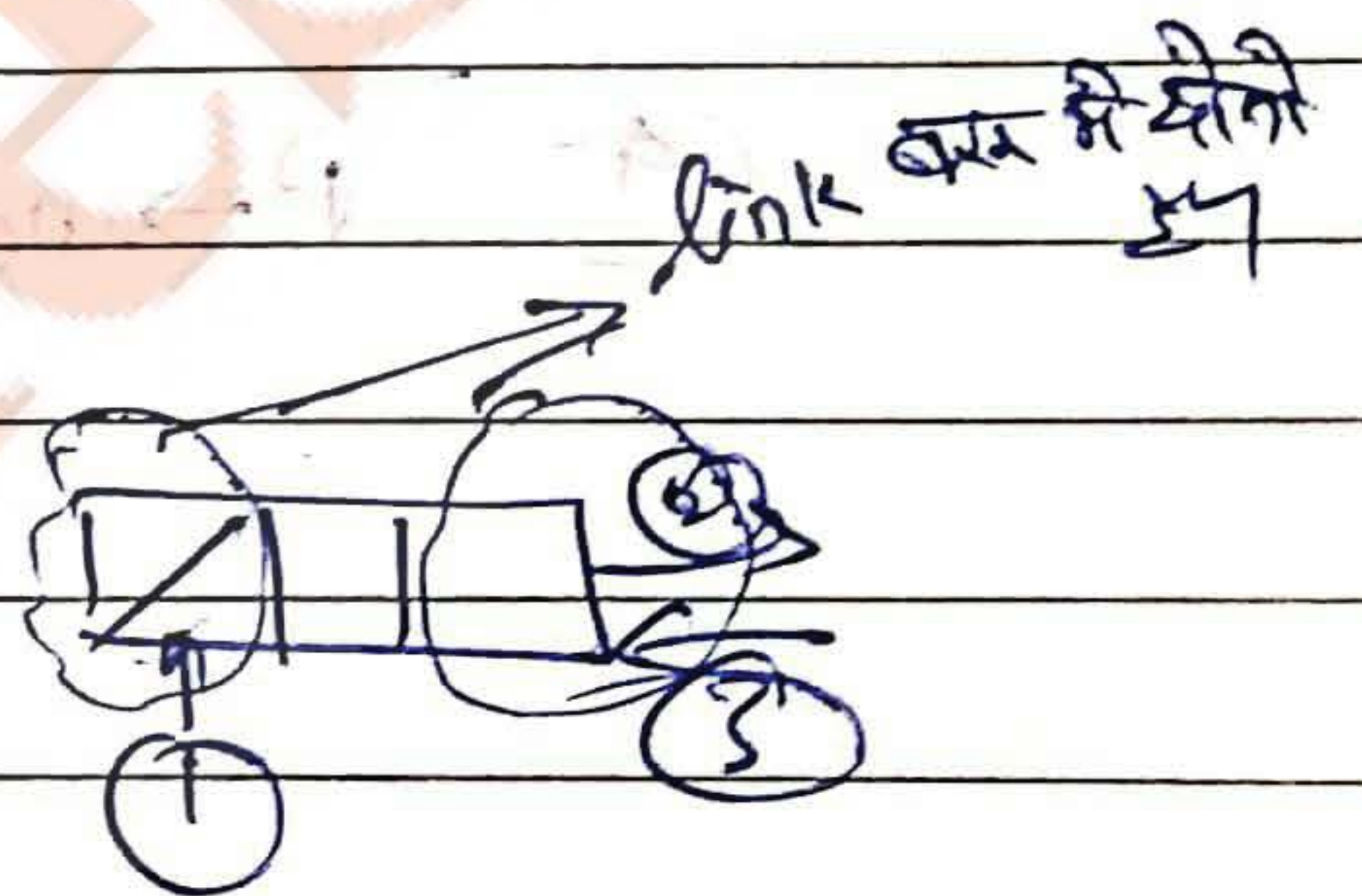
$\text{first} = t$;



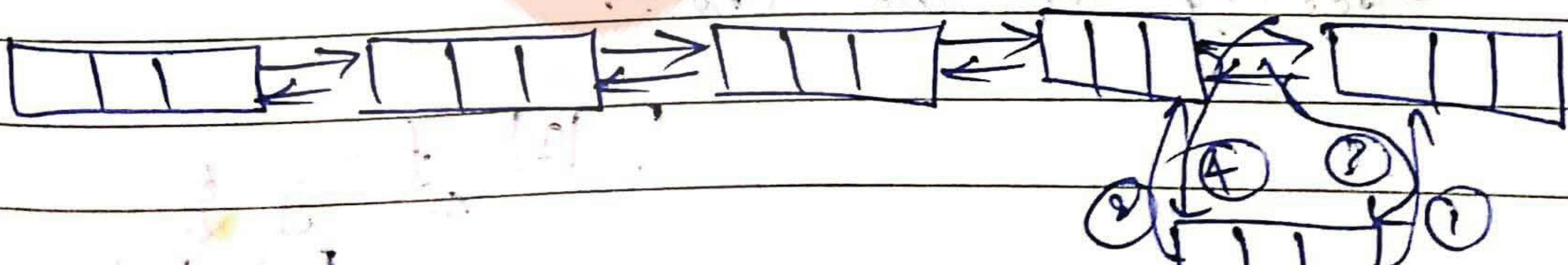
// time: $O(1)$

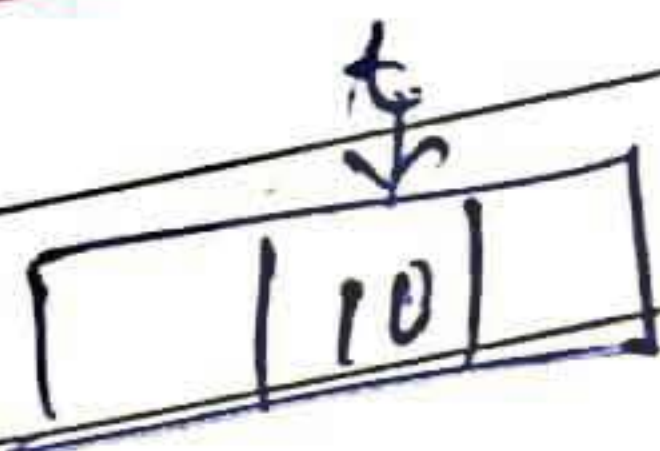
// one extra pointer

// links modified: 3



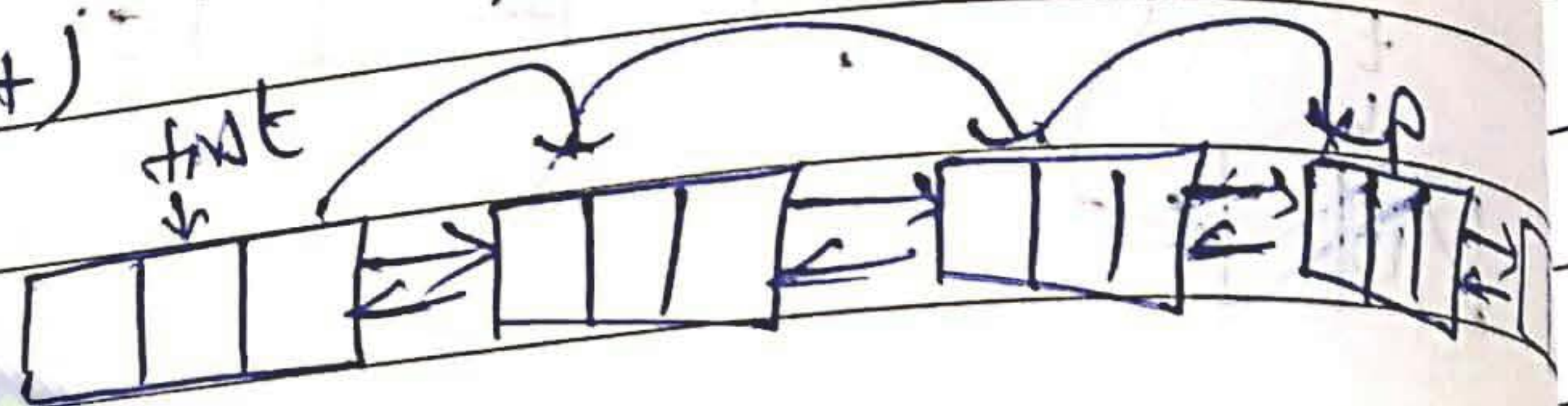
(b) Inserting a node at any position





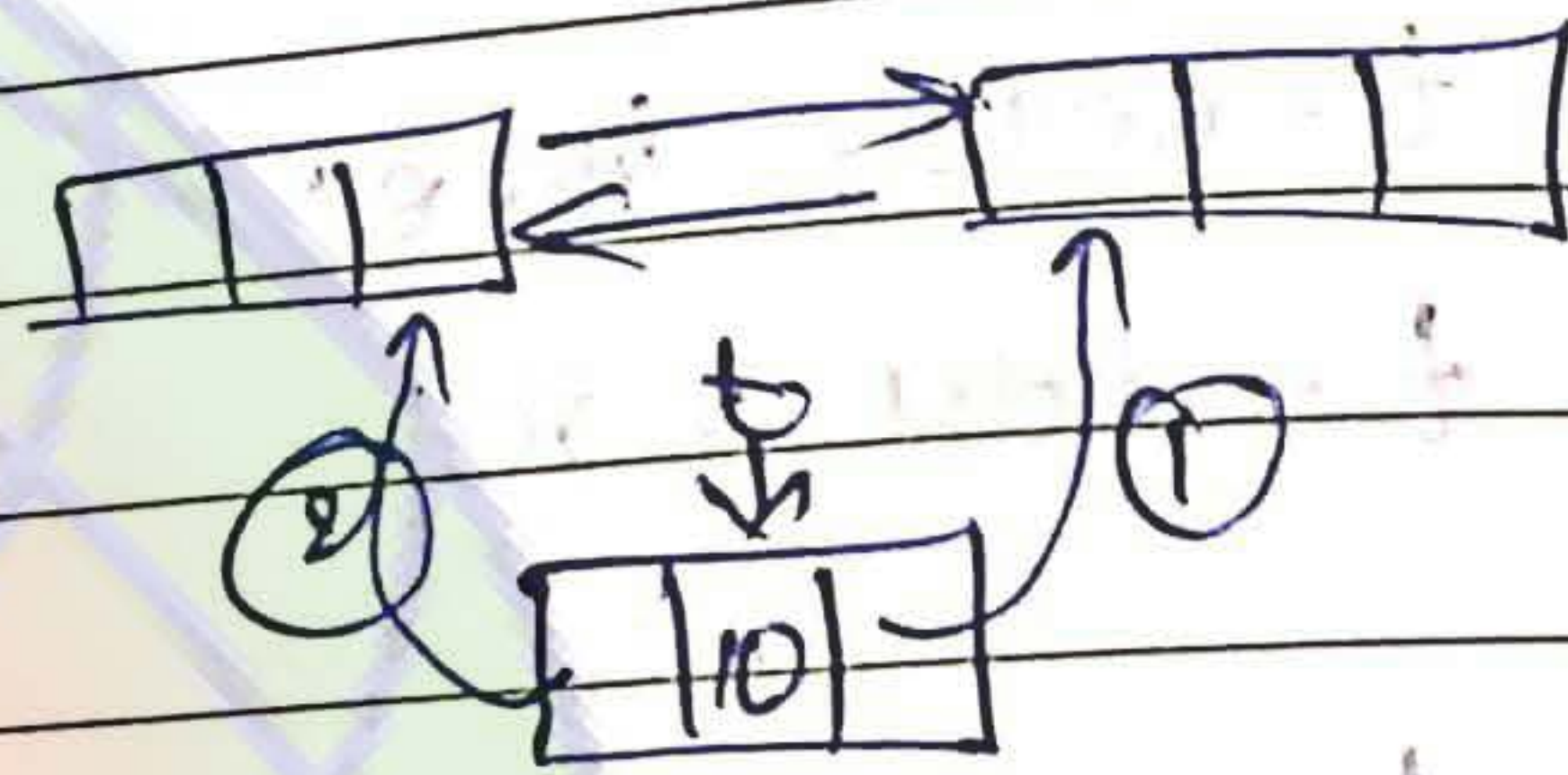
$t = \text{new Node};$
 $t \rightarrow \text{data} = 'x';$

$p = \text{first};$
 for: ($i=0; i < \text{pos}-1; i++$)
 $p = p \rightarrow \text{next};$

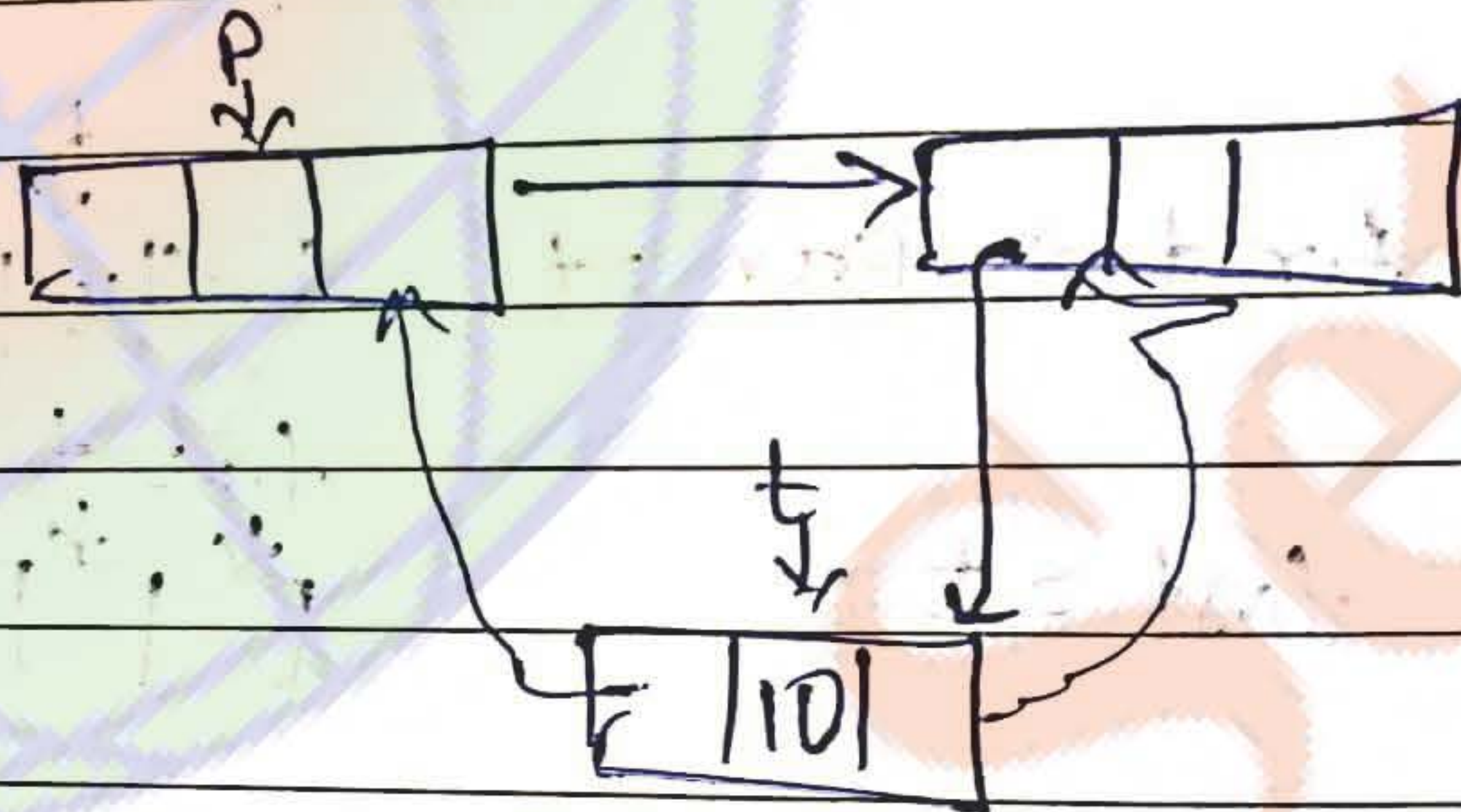


① $t \rightarrow \text{next} = p \rightarrow \text{next};$

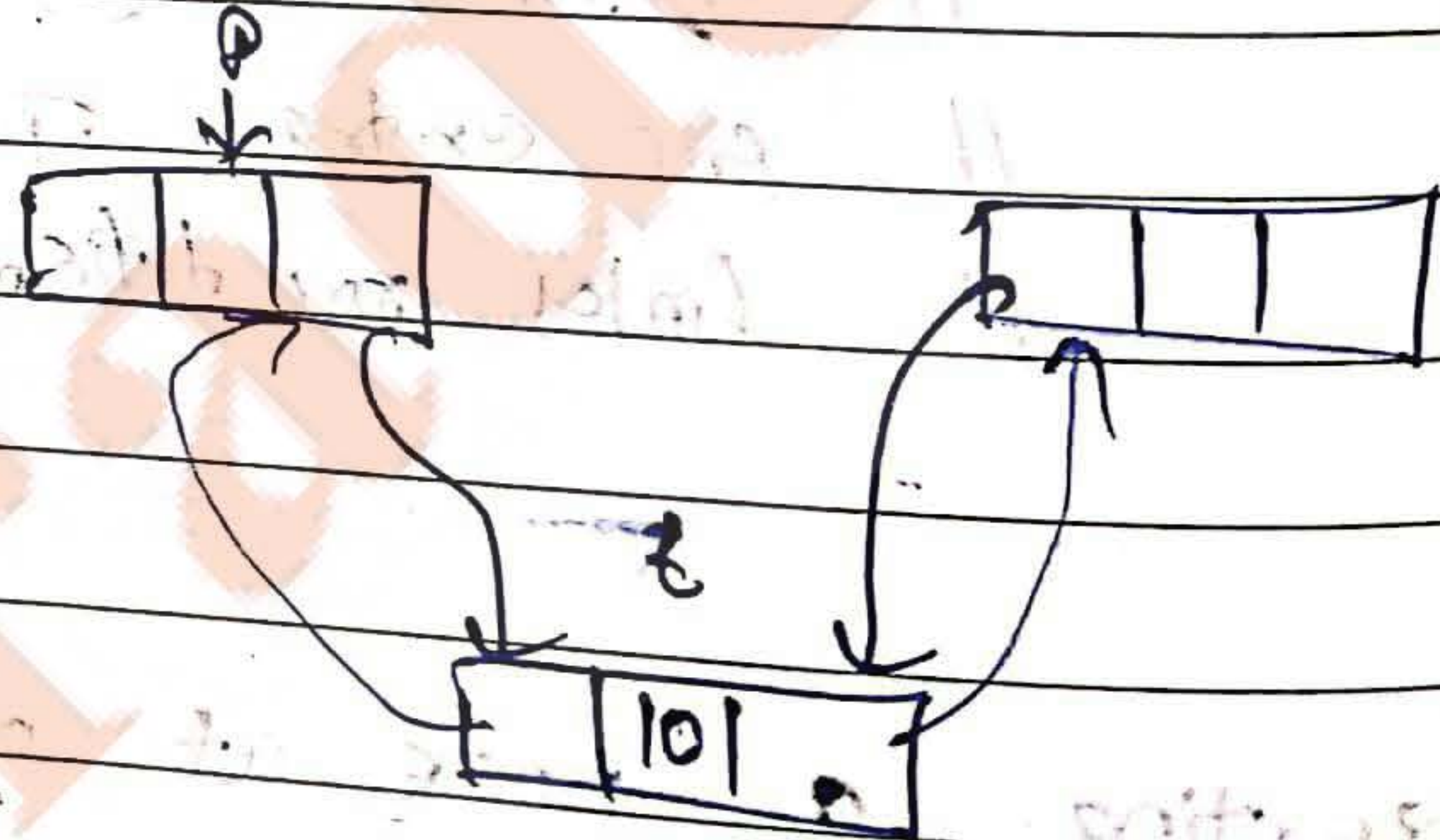
② $t \rightarrow \text{prev} = p;$



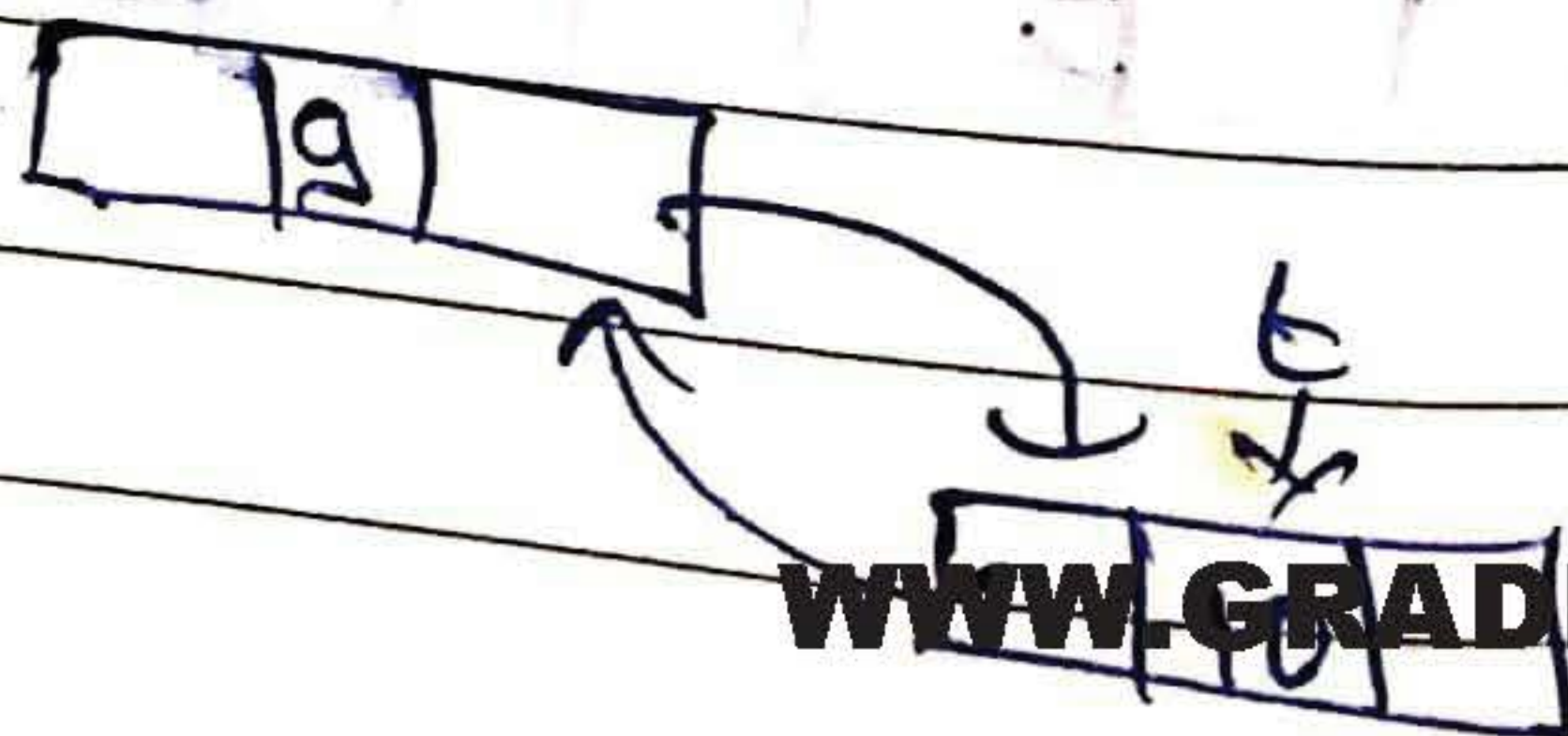
③ $p \rightarrow \text{next} \rightarrow \text{prev} = t;$



④ $p \rightarrow \text{next} = t;$



⑤ Inserting at the end:



Same as (b)

① if (p → next)

p → next → prev;

Same as b.

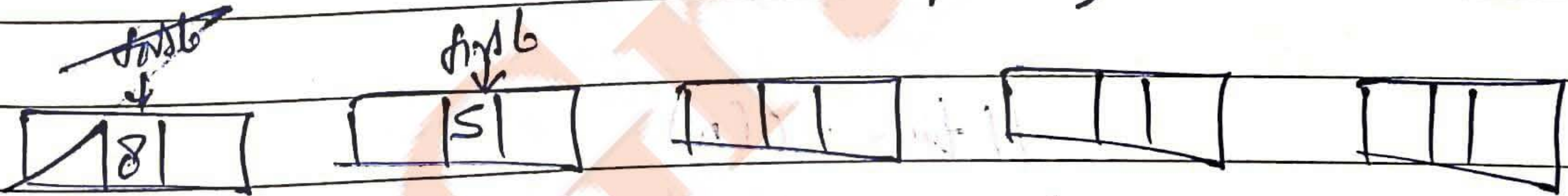
// time = $O(n)$

// pointers
require
entry = 2

// links modified = 4

② Deletion:-

(a) Deleting first node! (But at least ~~two~~ two nodes are required)



first → data;

first = first → next;

free (first → prev);

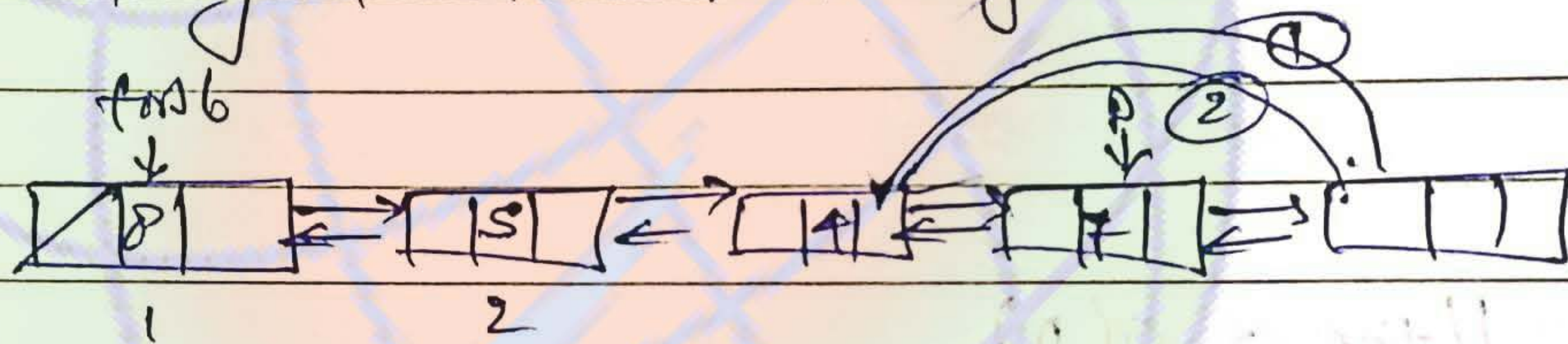
first → prev = NULL;

(b) Deleting first nodes

```

x = first -> data;
p = first;
first = first -> next;
free (p);
if (first)
    first -> prev = NULL;
    
```

(c) Deleting a node from given position:-



```

prev = first;
p = first;
for (i=0; i < pos-1; i++)
    p = p -> next;
    
```

- ① $p \rightarrow prev \rightarrow next = p \rightarrow next;$
- ② if ($p \rightarrow next$)
 $p \rightarrow next \rightarrow prev = p \rightarrow prev;$

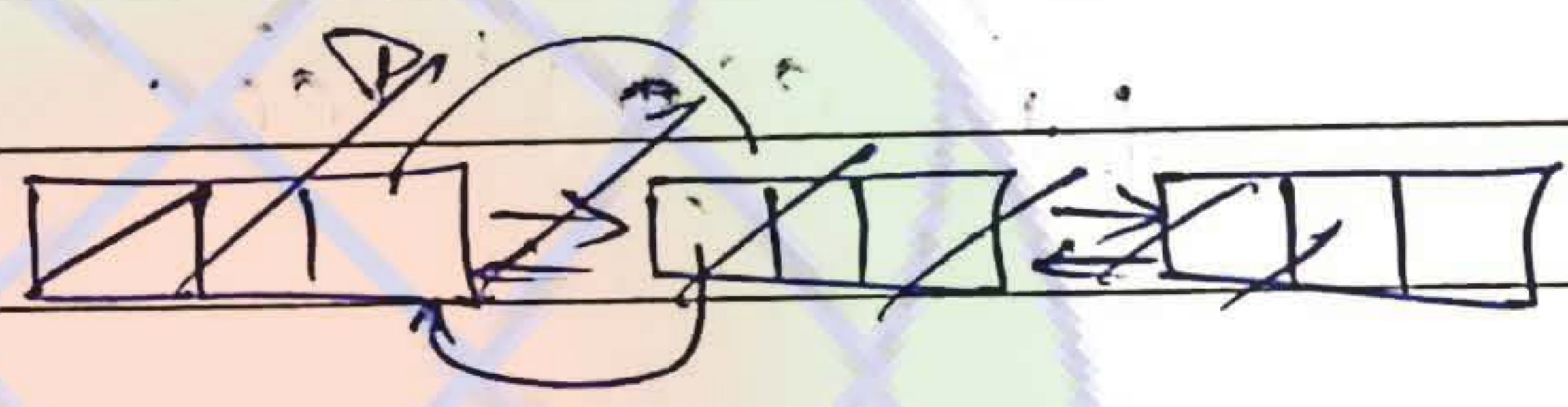
// time : $O(n)$

- // ~~points~~ No. of pointer required = 1
- // no of link modified = 2

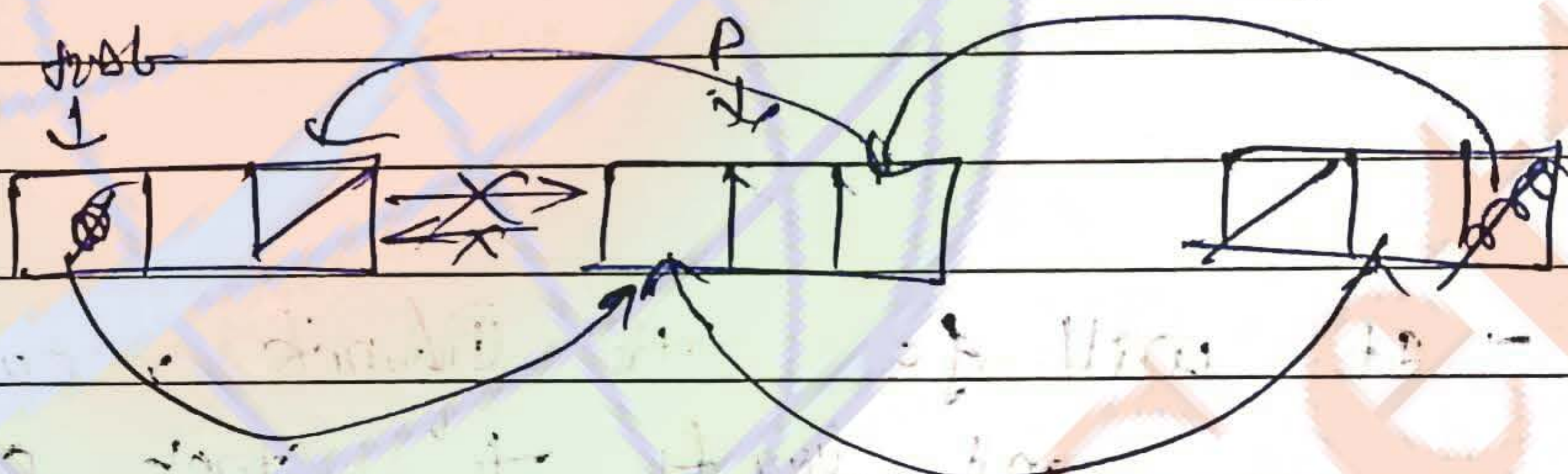
```

eg.) P = first;
while (P)
{
    q = P -> next;
    P -> next = P -> prev;
    P -> prev = q;
    P = q;
}
    
```

soln



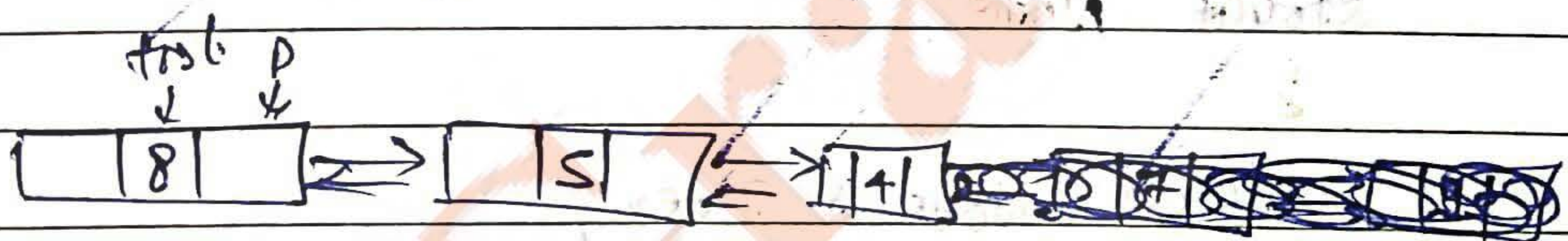
→ Link list is reversed



Interchanging the pointer, link list get reversed.

→ First remains on the same node, so it will pointing on the last node of reversed node.

Grade
Q.1



```

int Count (struct Node * p)
{
    if (P)
    {
        return 1 + count (P -> next) + count (P -> prev);
    }
    return 0;
}
    
```



```

int count(struct Node *P)
{
    if(P)
    {
        if(P->flag == 0)
        {
            P->flag = 1;
            return 1 + count(P->next) + count(P->prev);
        }
    }
    return 0;
}
    
```

★ Circular doubly linked list:-



Benefit: Circular & bi directional

Procedure of insert and delete will be same as procedure for insert & delete of doubly linked list

(9) Inserting nodes before Head

```

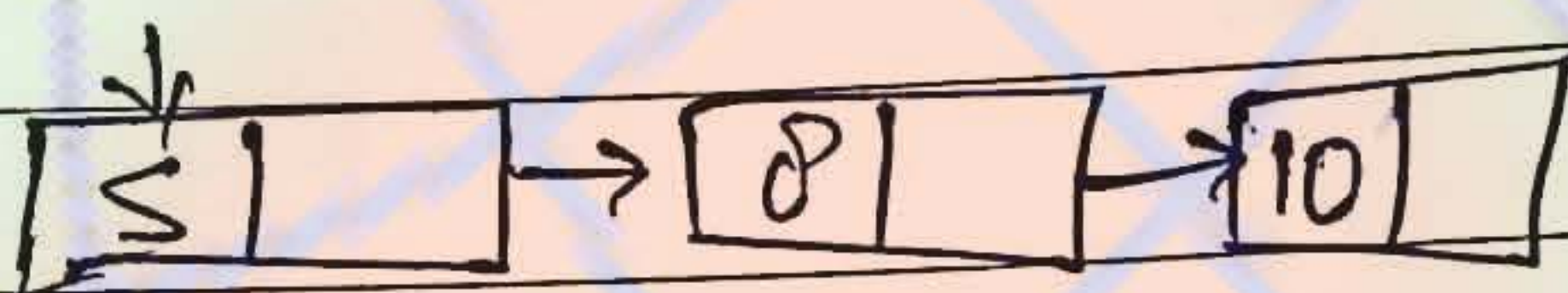
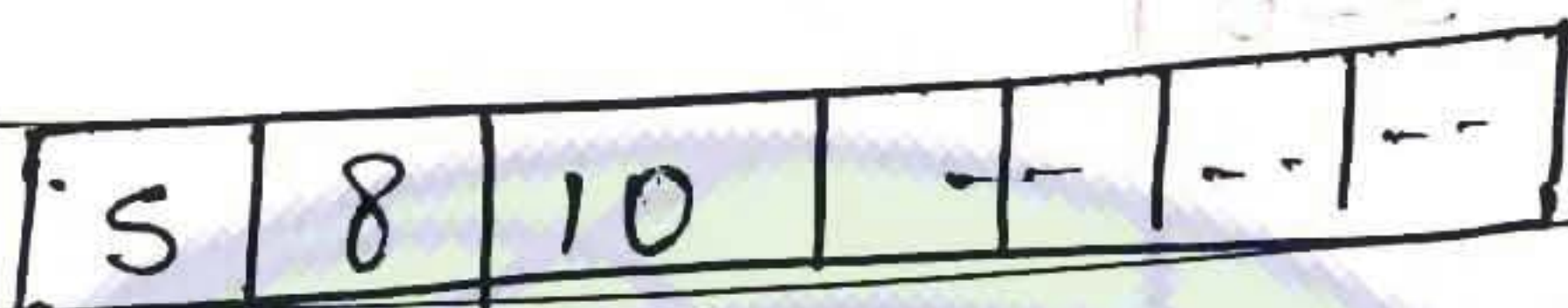
t = new node; // links modified = 4
t->data = x;
P = Head Head->prev;
t->next = Head;
t->prev = P;
P->next = t;
Head->prev = t;
    
```



Operations on List's (Array/Linked list)

~~Array/Linked list~~

5, 8, 10, 16, 12, 4, 9



// link list is better, due to its dynamic size, but it takes extra space for each element, to store address of next element.

1) Insert ① Insert

2) delete

3) search

4) Find

5) sort

6) Reverse

7) shift

8) split

9) length

10) ~~link~~ Append

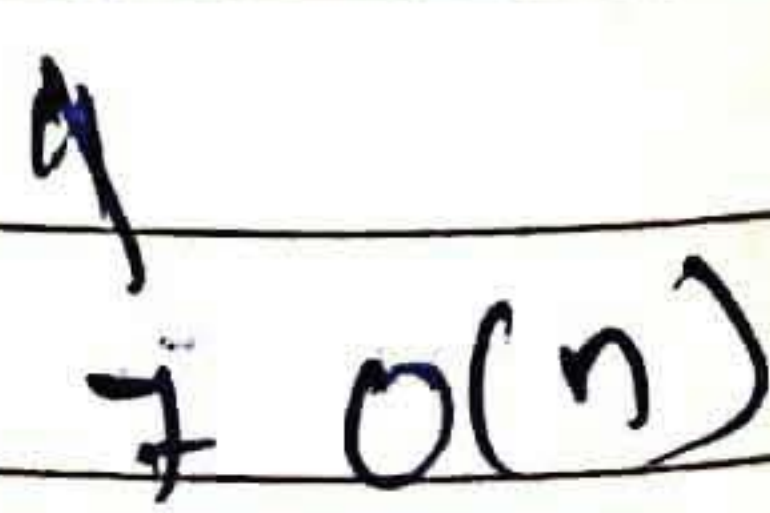
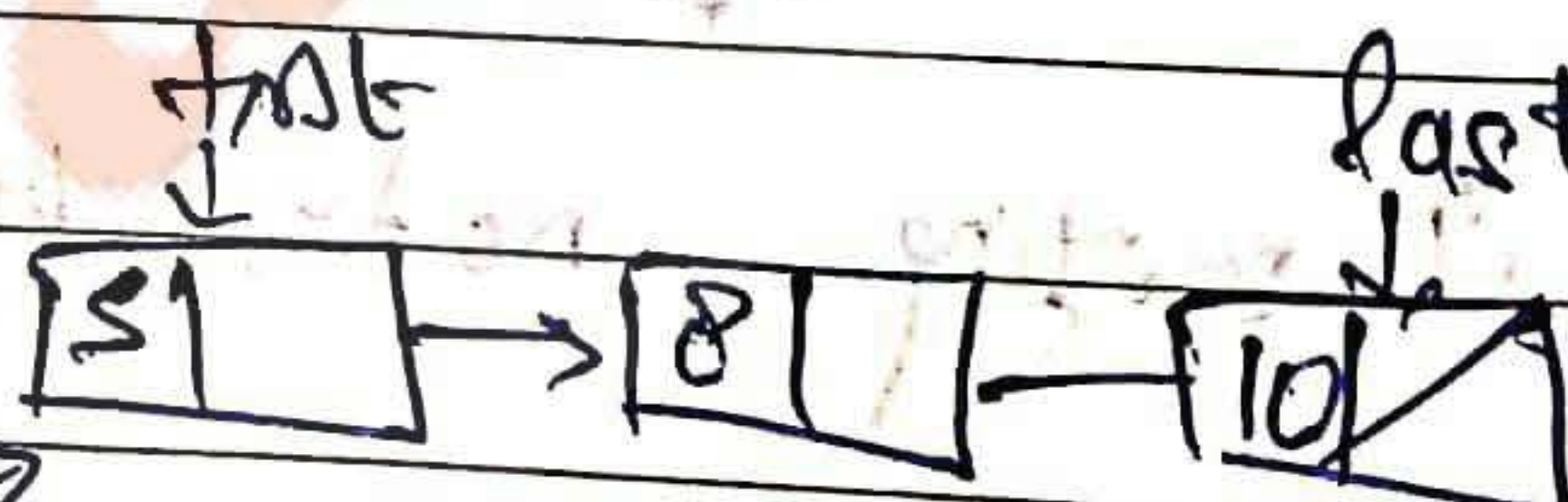
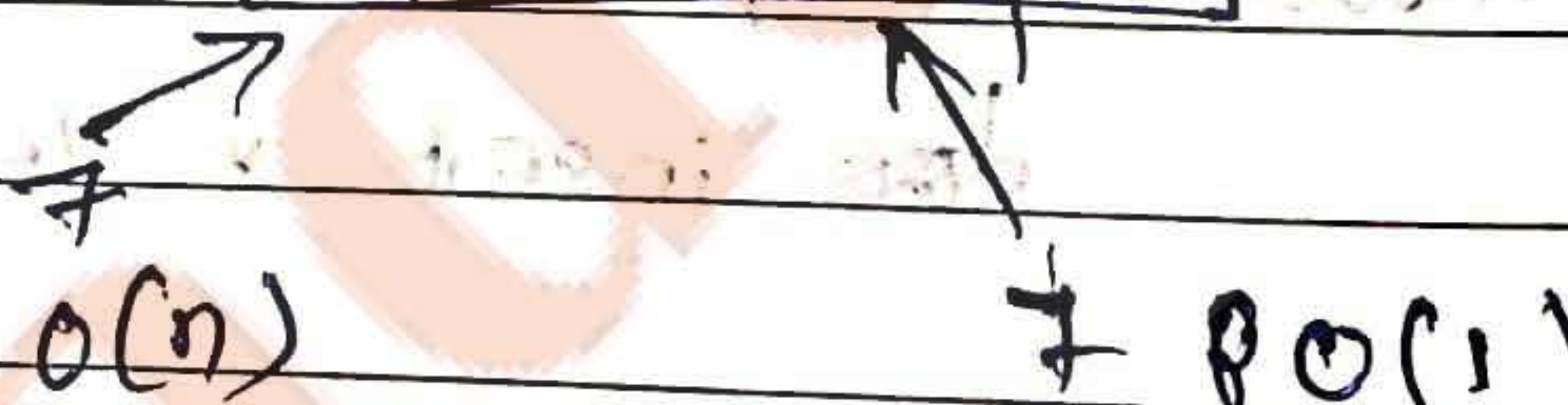
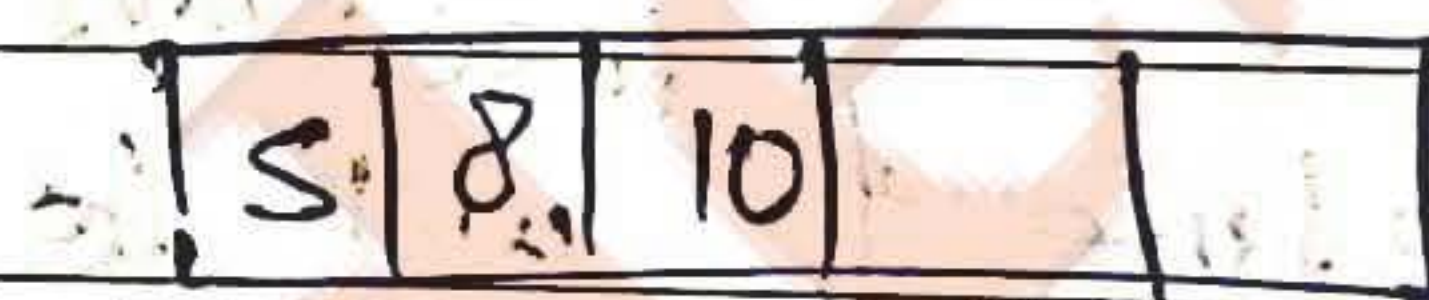
11) merge

set operations

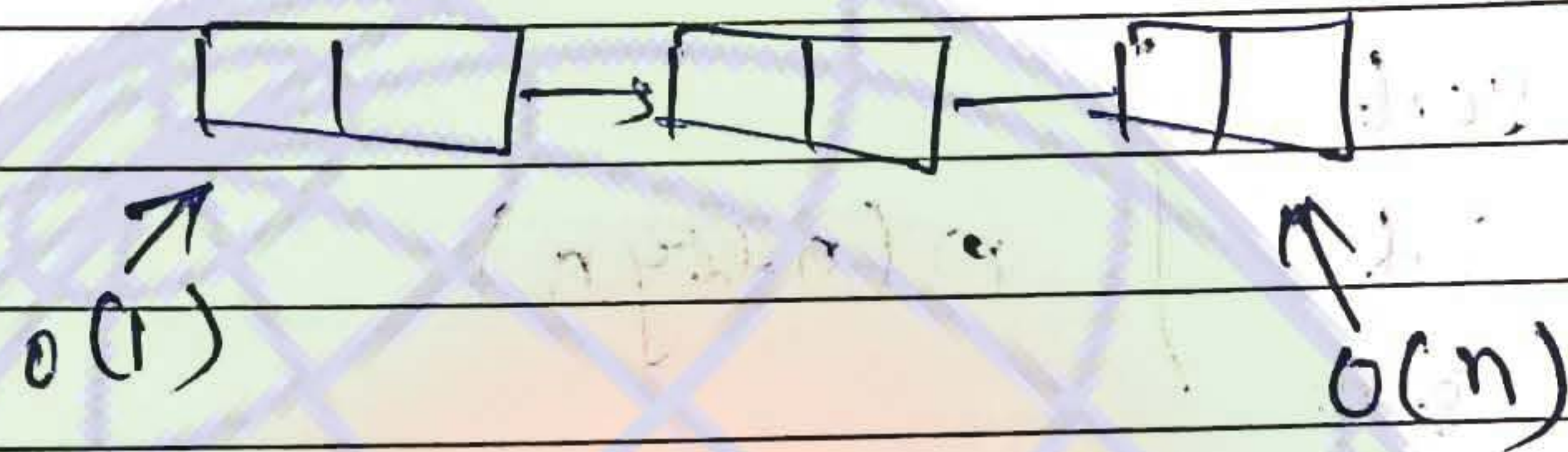
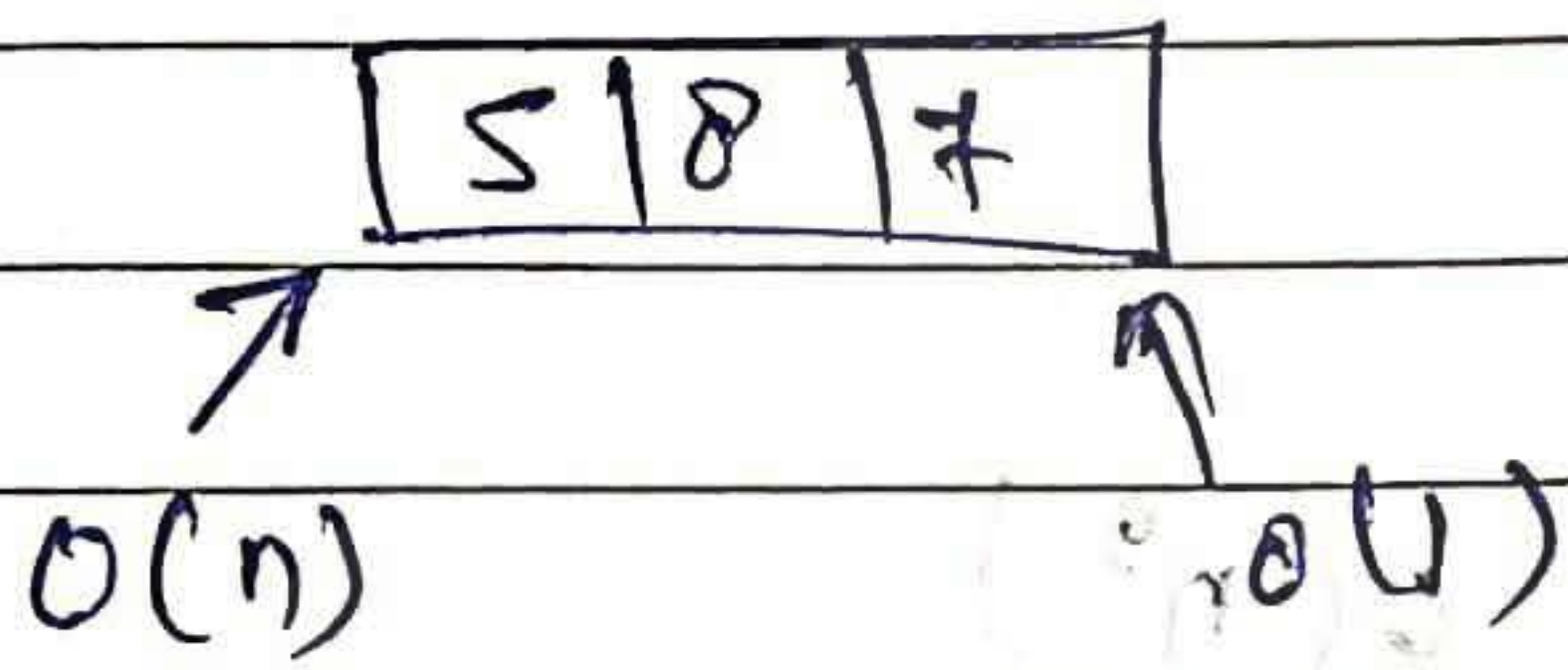
12) Union - n^2

14) Difference - n^2

13) Intersection - n^2 set membership $O(n)$



② Delete



Note:

③ Search

(a) Linear search ✓

(b) Binary search ✓

Array

$O(n)$

$O(\log n)$

linked list

$O(n)$

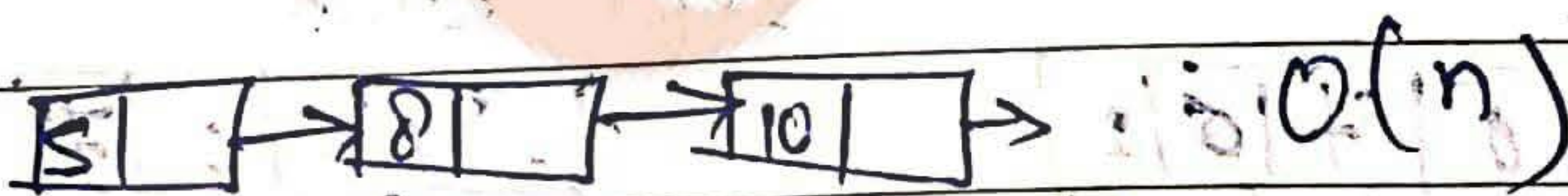
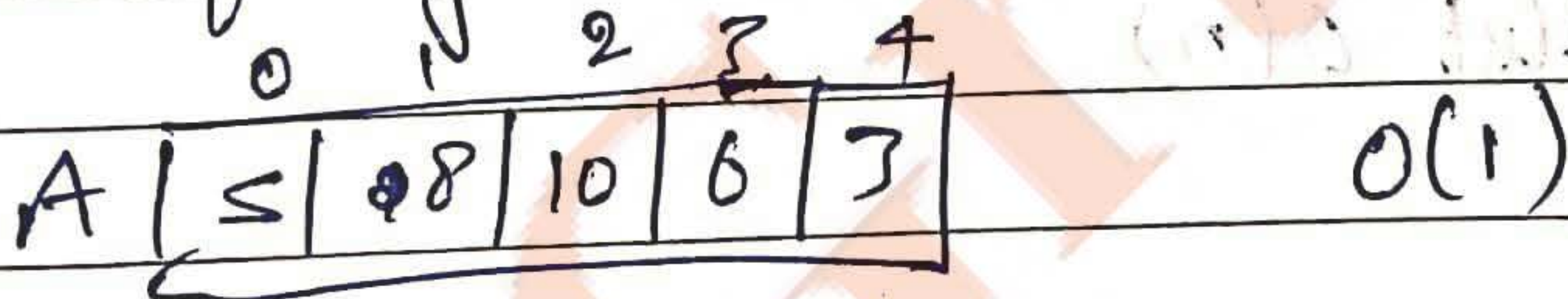
$O(n \log n)$

can be performed if the elements is sorted.

we can not directly reach the middle element, we have to traverse the nodes.

// Binary search is not efficient on linked list.

4) Find: finding an element at a given position.



50) short :-

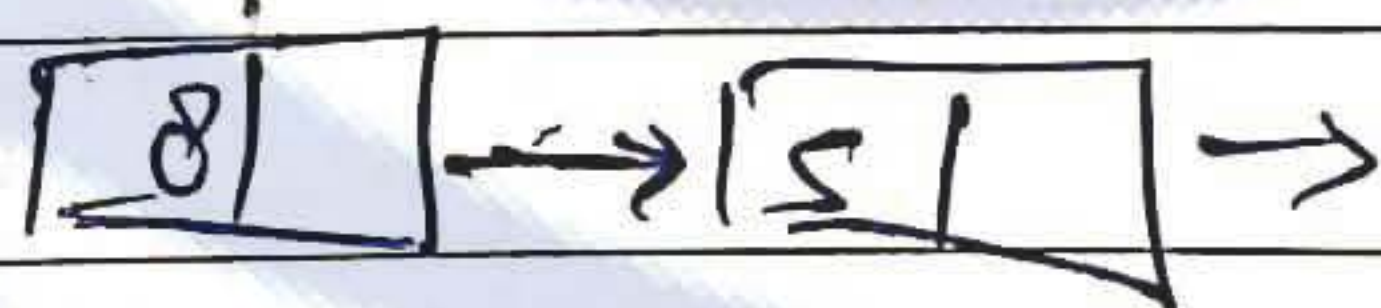
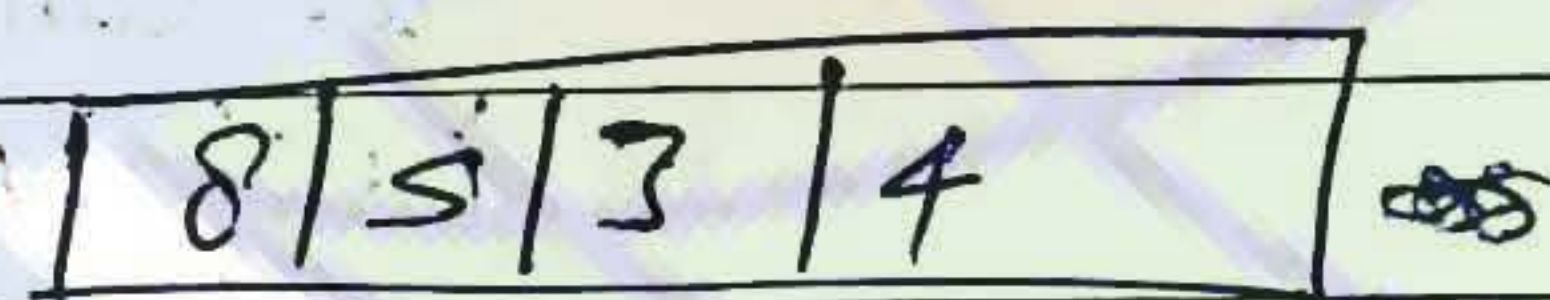
(a) Bubble sort } $O(n^2)$
 (b) Insertion sort }
 (c) Selection sort }

(d) Heap sort } $O(n \log n)$
 (e) Quick sort }
 (f) Merge sort }

* These sorts are on the basis of linked list.

→ These two are useful on linked list.

→ Insertion & merge sort work on nodes.



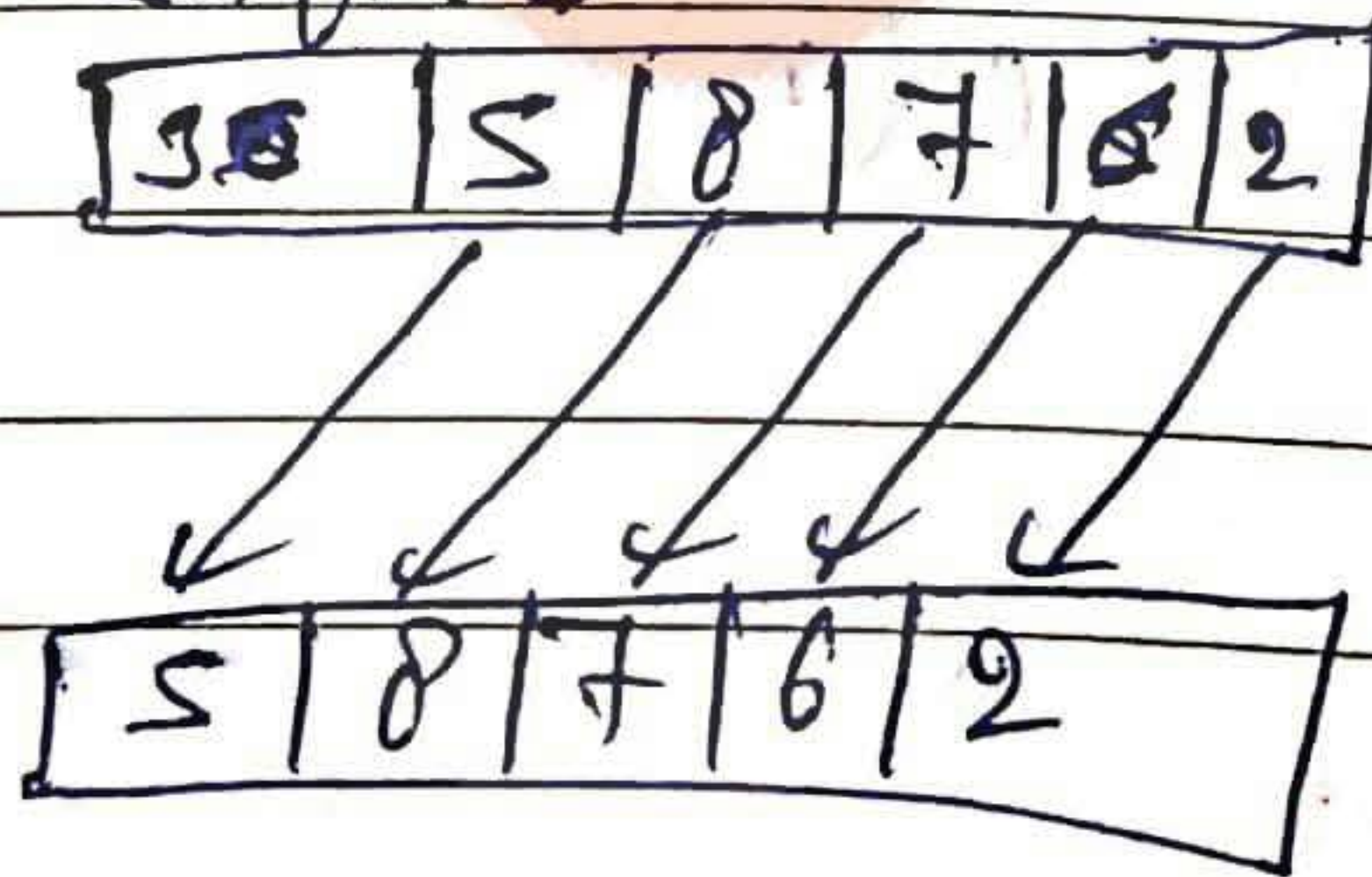
6) Reverse

array $O(n)$
 linked list $O(n)$

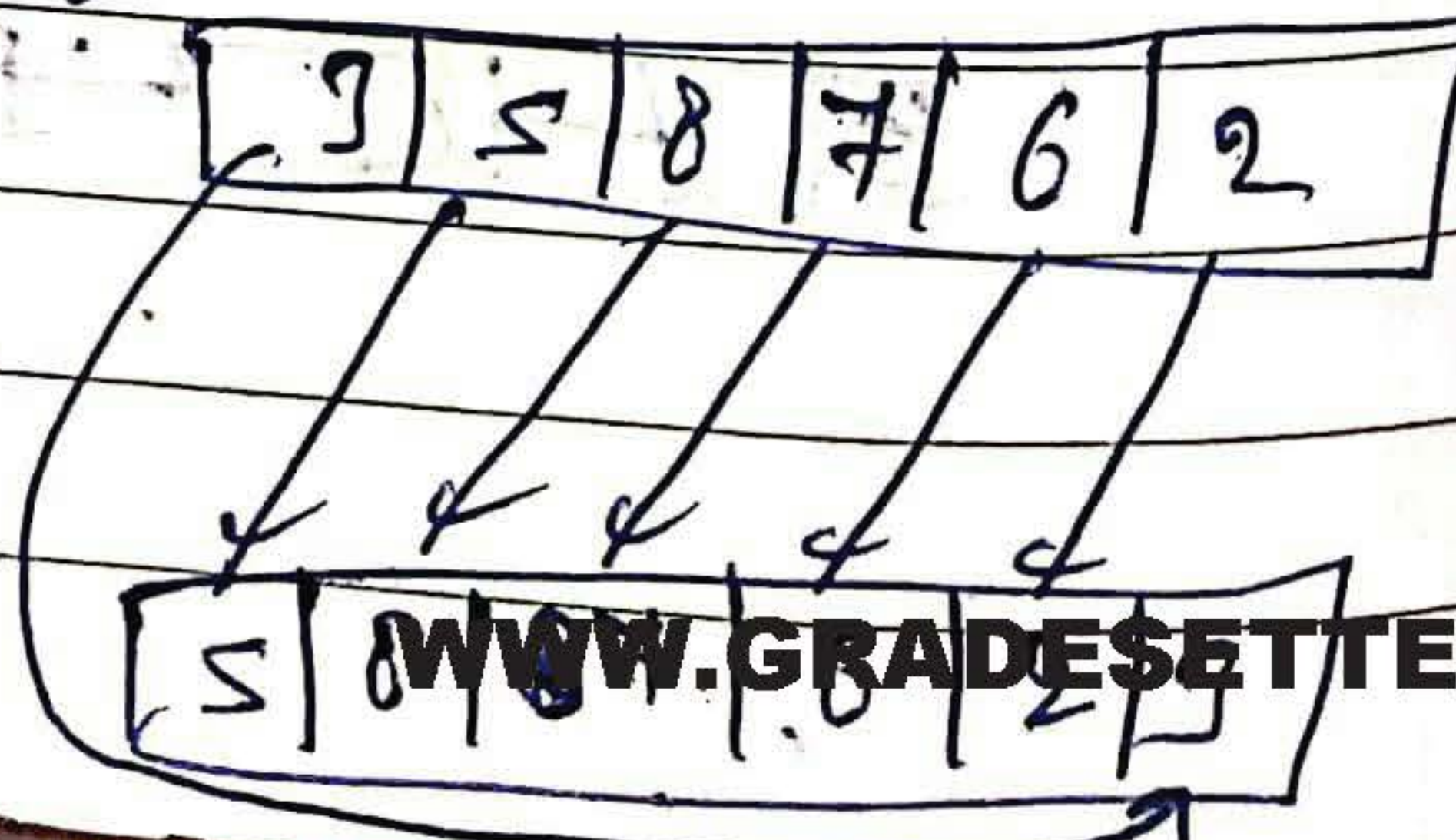
7)

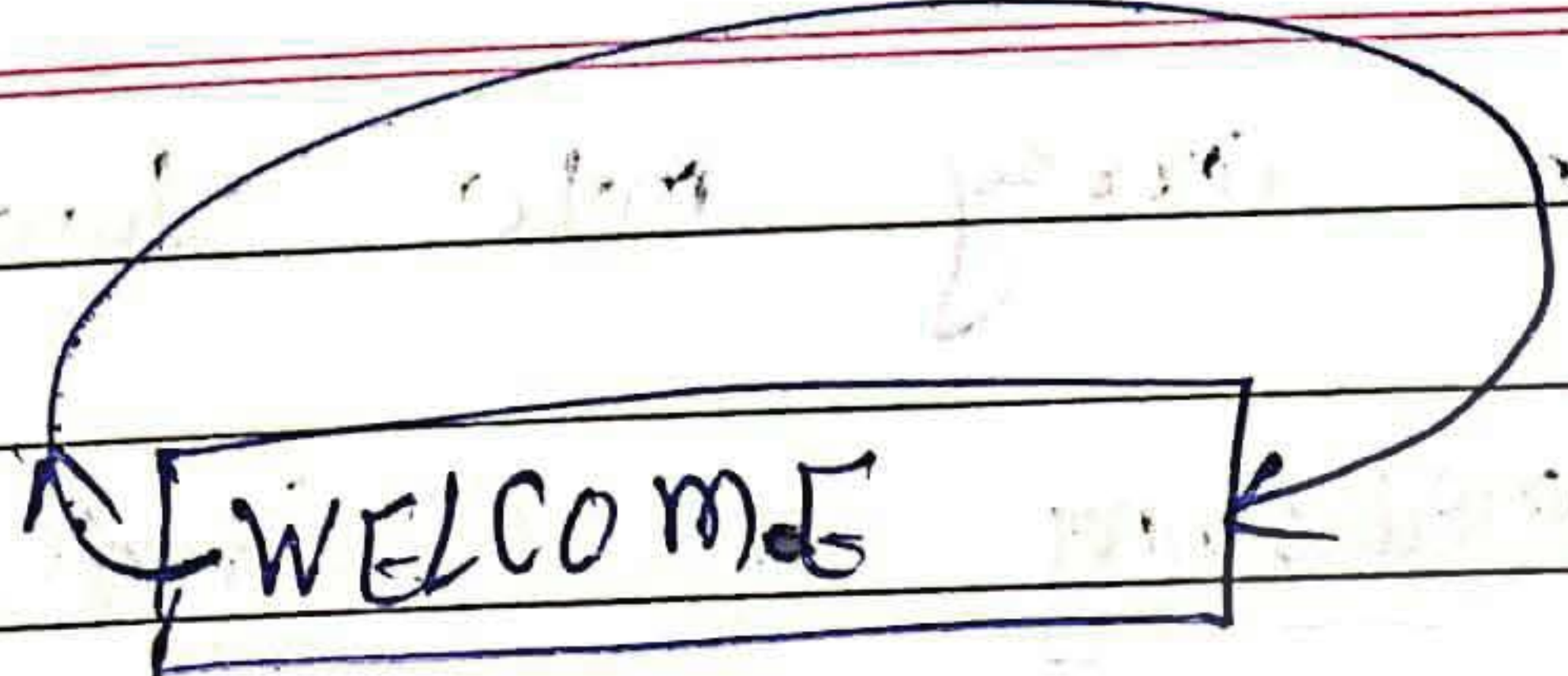
shift

left shift :-



left rotate

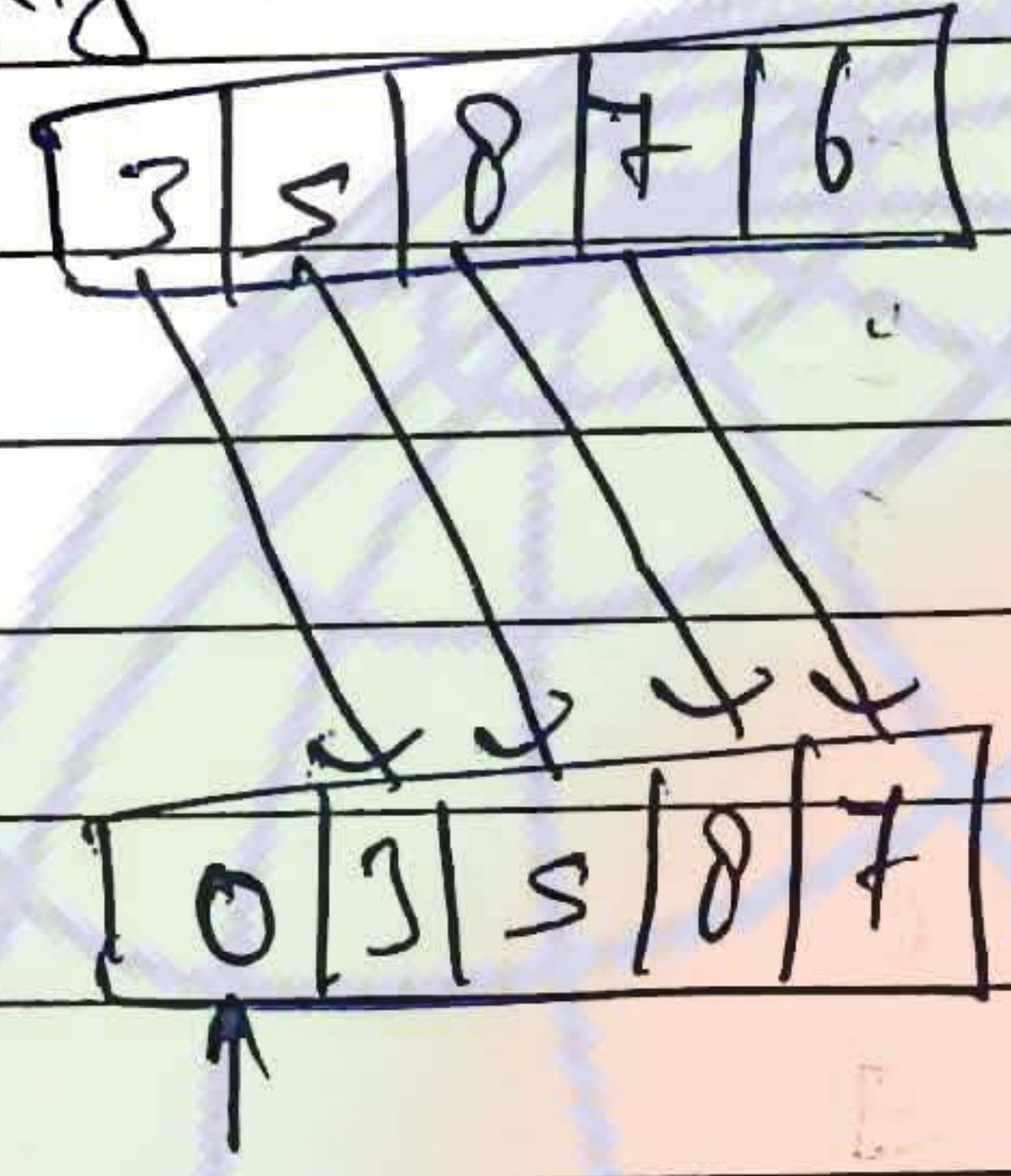




Rotation

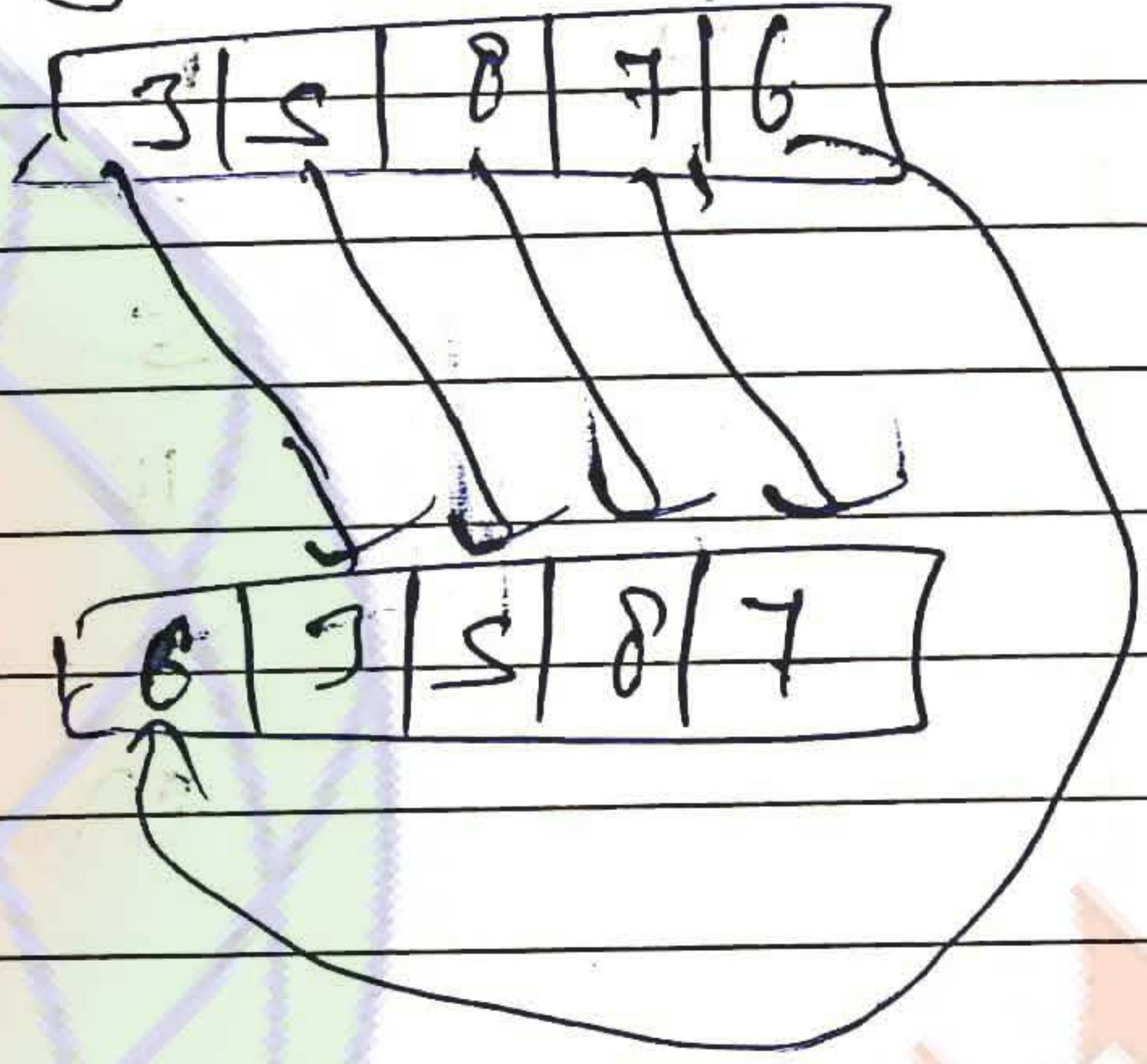


Right Shift



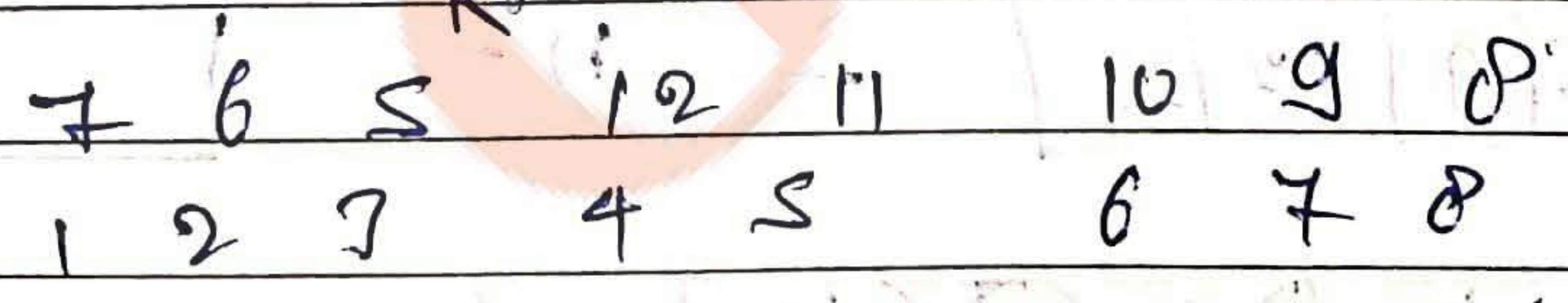
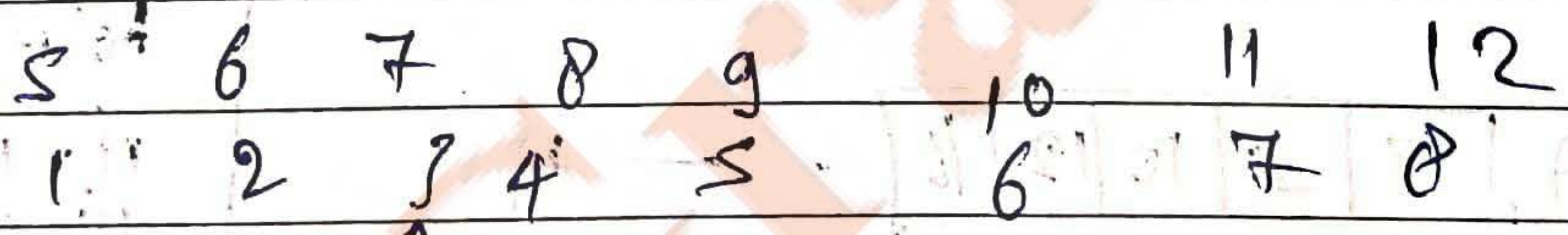
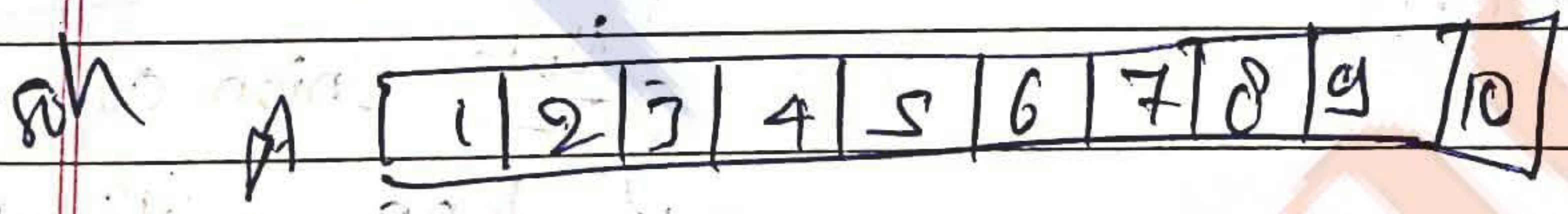
You have to put something, so put 0!

Right rotate

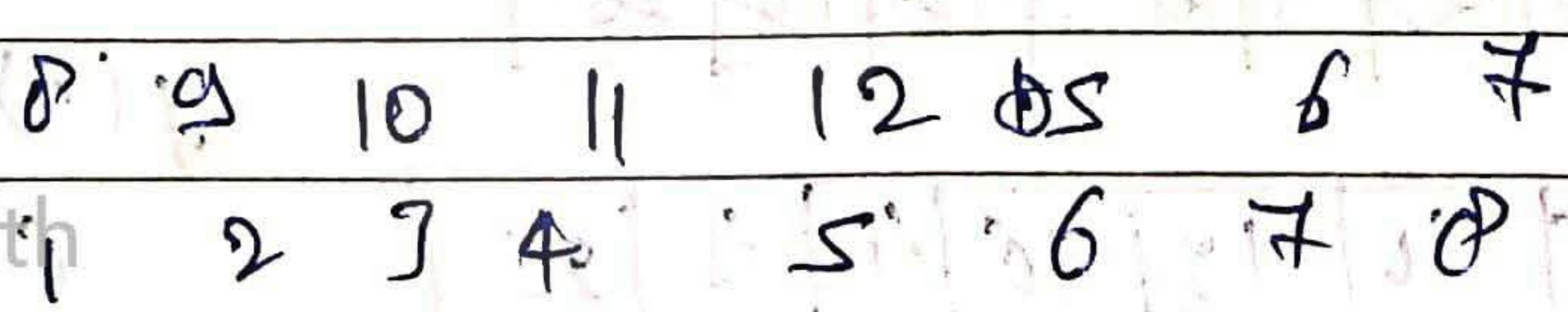


$A[1 \dots n]$

- reverse $[A, 1, k]$
- reverse $(A, k+1, n)$
- reverse $(A, 1, n)$



$n-k$ times right rotation



left rotation by 3 elements

(8) Split: - Splitting an array into two or more

(9) Length - is the measuring of the length

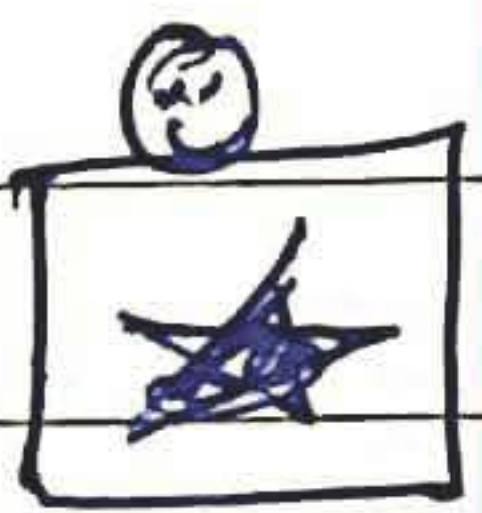
(10) Append - Adding more elements on the tail of the array.

11) Merge: Combining two sorted list into single sorted list.

A	B	C
2	3	2
5	6	3
10	9	5
	12	6
		9
m	n	10
		12

$$O(m+n) = O(n)$$

// For merging list ~~should~~ should be in sorted way.



Set Operation

12) Union

A [3 | 5 | 10 | 12 | 16] — n

B [4 | 5 | 9 | 12 | 20] — n²

~~A [3 | 5 | 9 | 10 | 12 | 16 | 20]~~

C [3 | 5 | 10 | 12 | 16 | 4 | 9 | 20]

Note: Union can be done with the help of merging if the elements is sorted
time: $O(n)$

$$f(n) = n^2 + n$$

13) Intersection

A [3 | 5 | 10 | 12 | 16] n

B [4 | 5 | 9 | 12 | 20] n^2

जहाँ दो दो राव लो common
हूँ then array में
insert करें

C [5 | 12]

$f(n) = n^2 + n$

$O(n^2)$

14) Difference: non common element

A []

B []

C []

time = $O(n^2)$

15) set

- element does belong to the set or not

\Rightarrow // time = $O(n)$

Union

Note: Using merging for set operation

If two sets A and B are sorted, then merging can be used for performing set operations.

It will take $O(n)$ times.

for union,

// while merging, don't copy duplicate value.

Intersection

for intersection, while merging take only equal elements.

Code for merging:-

$i=0$, $j=0$, $k=0$;

while ($i < m$ & $j < n$)

{

if ($A[i] < B[j]$)

{

}

else

{

$C[k++] = B[j++]$;

}

}

for ($i < m$; $i++$)

$C[k++] = A[i]$;

for ($j < n$; $j++$)

$C[k++] = B[j]$;

(b) case for Union, by merging.

$i=0$, $j=0$, $k=0$;

while ($i < m$ & $j < n$)

{

if ($A[i] < B[j]$)

{

$C[k++] = A[i++]$;

}

```
else if (A[i] > B[j])
```

```
{
```

```
    C[k++] = B[j++];
```

```
}
```

```
else
```

```
{
```

```
    C[k++] = A[i++];
```

```
    j++;
```

```
}
```

```
}
```

```
for ( ; i < m; i++)
```

```
    C[k++] = A[i];
```

```
for ( ; j < n; j++)
```

```
    C[k++] = B[j];
```

②

Intersection using merging.

i=0, j=0, k=0;

```
while (i < m && j < n)
```

```
{
```

```
    if (A[i] < B[j])
```

```
    {
```

```
        i++;
```

```
    else if (A[i] > B[j])
```

```
    {
```

```
        j++;
```

```
    }
```

```
    else
```

```
        C[k++] = A[i++];
```

```
        j++;
```

```
    }
```

Stack

① - Stack is a data structure which works on disciplines LIFO (last in first out)

- Elements are inserted and deleted from same end.

- Stack can be implemented using ~~array~~

(a) Array and ✓

(b) linked list ✓

② ADT (Abstract data type of stack) :-
hiding details, showing only required.

Data:

1-> space for storing elements

2-> Top-Pointer, to point on topmost element

Operation:

Push(x)

Pop()

Peek() - finding an element at given position

StackTop() - knowing what is the topmost element on stack

isFull() - } check if the stack is full or

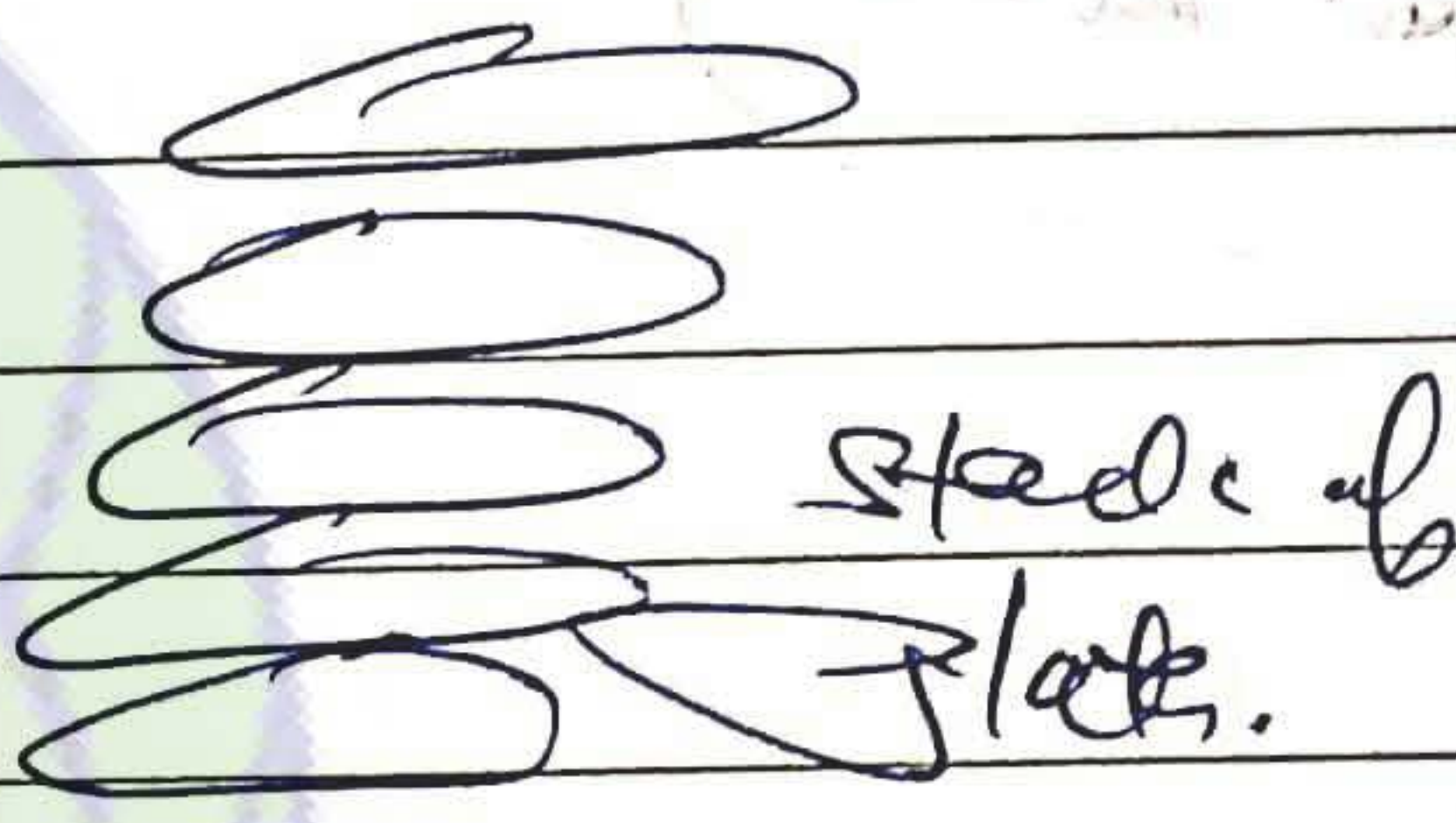
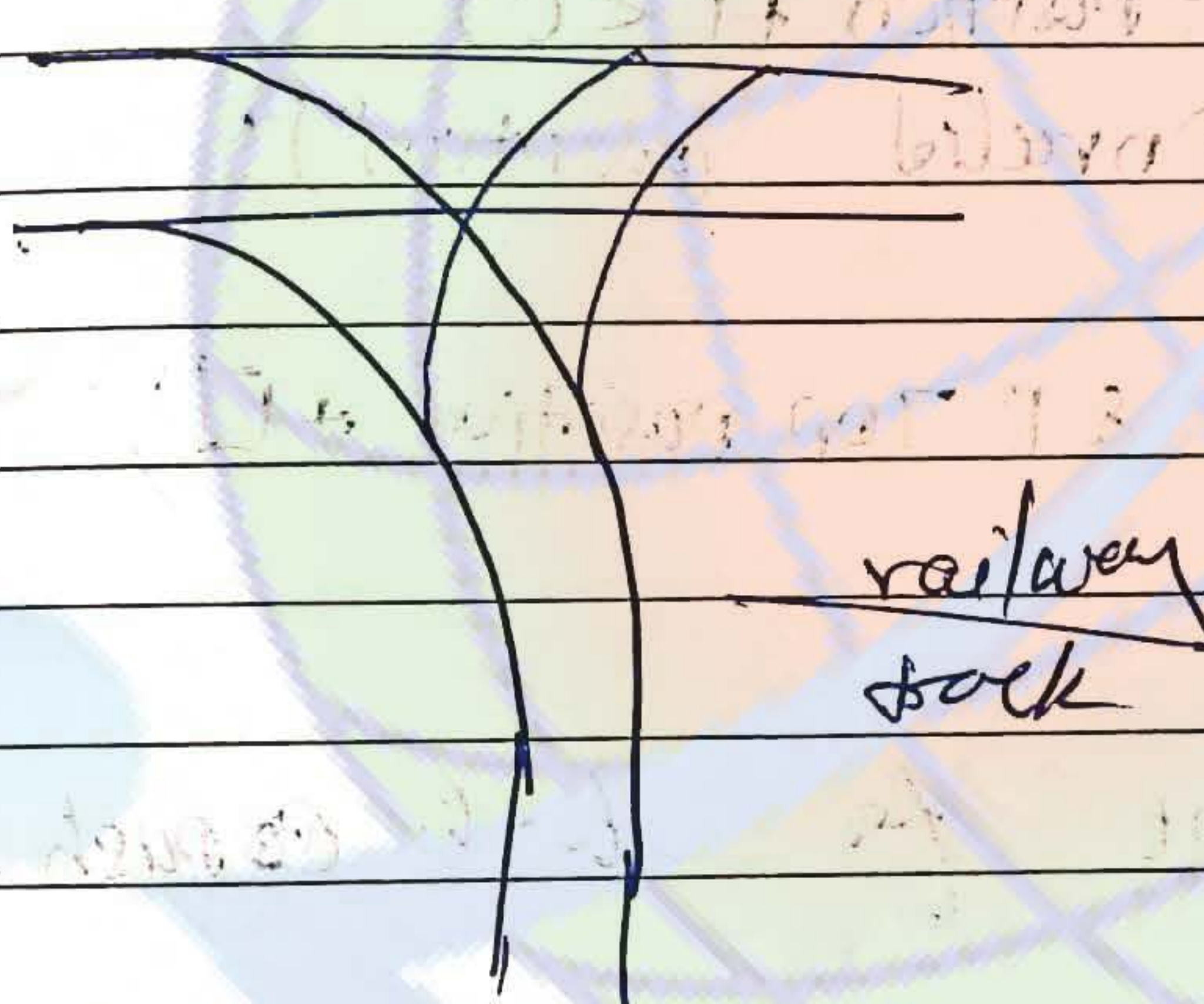
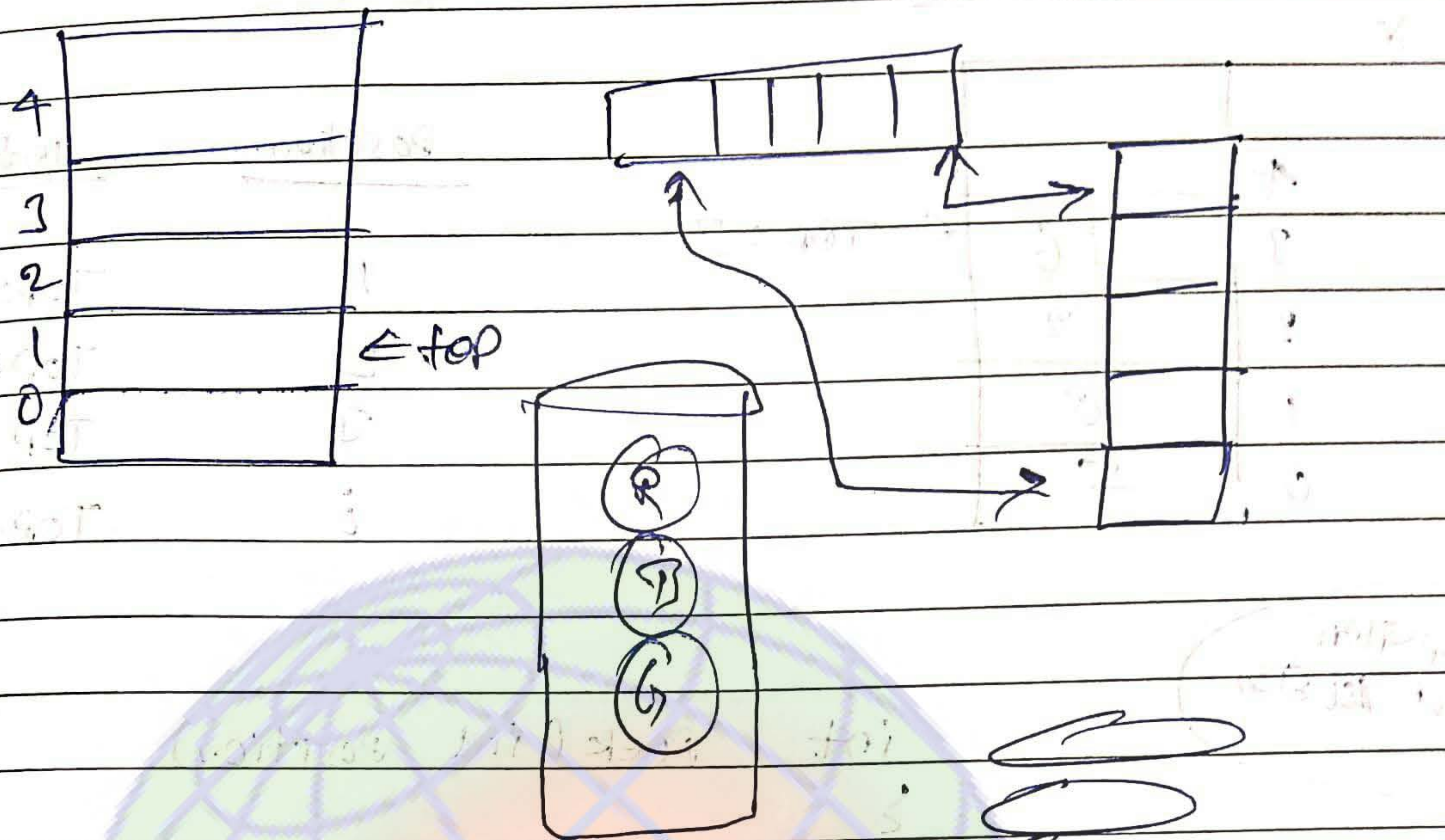
isEmpty() - } empty.

Note:

2 Data types - defines, with a ~~name~~ representation of data

Operations on data.

3) Implementing stack using Array



Initially Top = -1	Empty if (TOP == -1)	Full if (TOP == size - 1)
-----------------------	-------------------------	------------------------------

```

Push (int x)
{
    if (TOP == size - 1)
        Pf ("stack is Full");
    else
    {
        TOP++;
        s[TOP] = x;
    }
}

(int) Pop()
{
    int x = 0;
    if (TOP == -1)
        Pf ("stack is empty");
    else
    {
        x = s[TOP];
        TOP--;
    }
    return x;
}
    
```

size = 5

#		Position	Index
4		1	TOP = 3
3	16	2	TOP - 1 = 2
2	12	3	TOP - 2
1	8	i	TOP - i + 1
0	5		

← TOP = 3

Note: top of element

```
int peek (int position)
{
    if (TOP - position + 1 < 0)
        pf ("Invalid position");
    else
        return s [TOP - position + 1];
}
```

Note:

// Time : constant for both push & pop

- Full - is the state
- overflow - result of an operation

```
push (int x)
```

{

```
    if (TOP > -size - 1)
```

```
        pf ("stack is full");
```

```
    else
```

```
        TOP++
```

```
        s [TOP] = x;
```

}

① Using zeroth (0th) index of an array as a top pointer.



initially TOP = 0	Empty if (TOP == -1)	Full if (TOP == size - 1)
----------------------	-------------------------	------------------------------

size = 5

Push (int x)

{

if (s[TOP] == size - 1)

printf("stack is full");

else

s[TOP]++;

s[s[TOP]] = x;

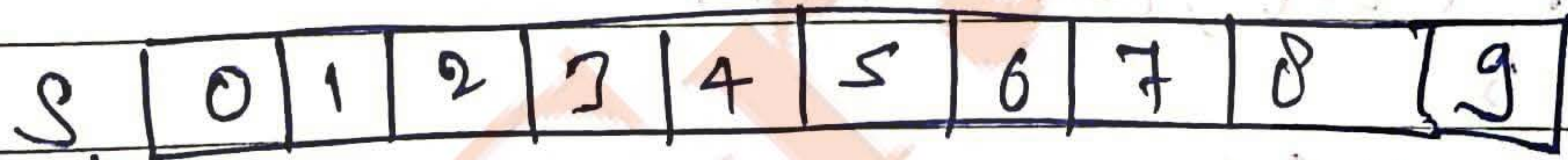
}

}

int = POP

② Implementing two stacks using single array.

size = 10

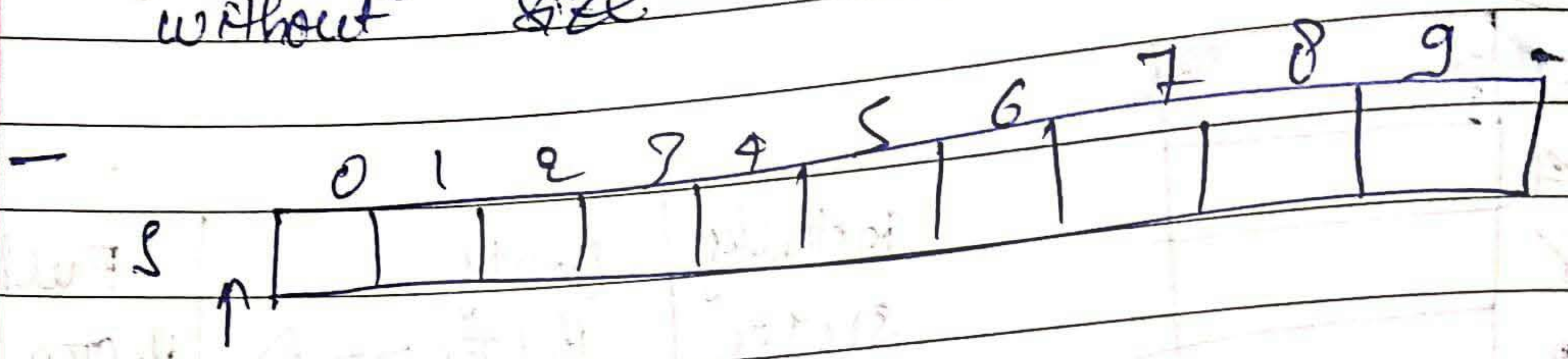


top = -1

Top = size

- single array is used for implementing two stacks. from either ends and the array is

uses by both the stack ~~with size~~
without size limit,



Stack 1	Stack 2
Empty: $\text{if} (\text{TOP} == -1)$	$\text{if} (\text{TOP} == \text{size})$
Full: $\text{if} (\text{TOP}_1 == \text{TOP}_2 - 1)$	$\text{if} (\text{TOP}_2 == \text{TOP}_1 - 1)$
	$\text{if} (\text{TOP}_1 == \text{TOP}_2 - 1)$

★ Implementing multiple stack using single array

Array S of size m
no. of stacks n

Array of TOPs $- T[n]$

Array of Boundaries $- B[n+1]$

for ($i=0; i < n; i++$)

$$T[i] = m/n * i - 1;$$

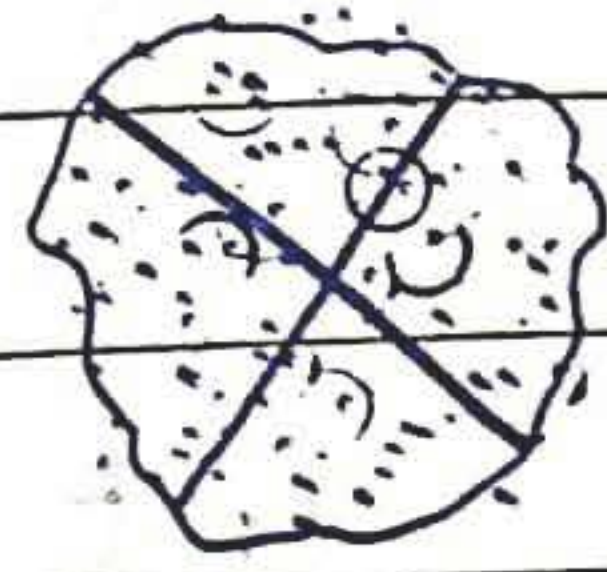
$$B[i] = m/n * i - 1;$$

$$B[n] = m - 1;$$

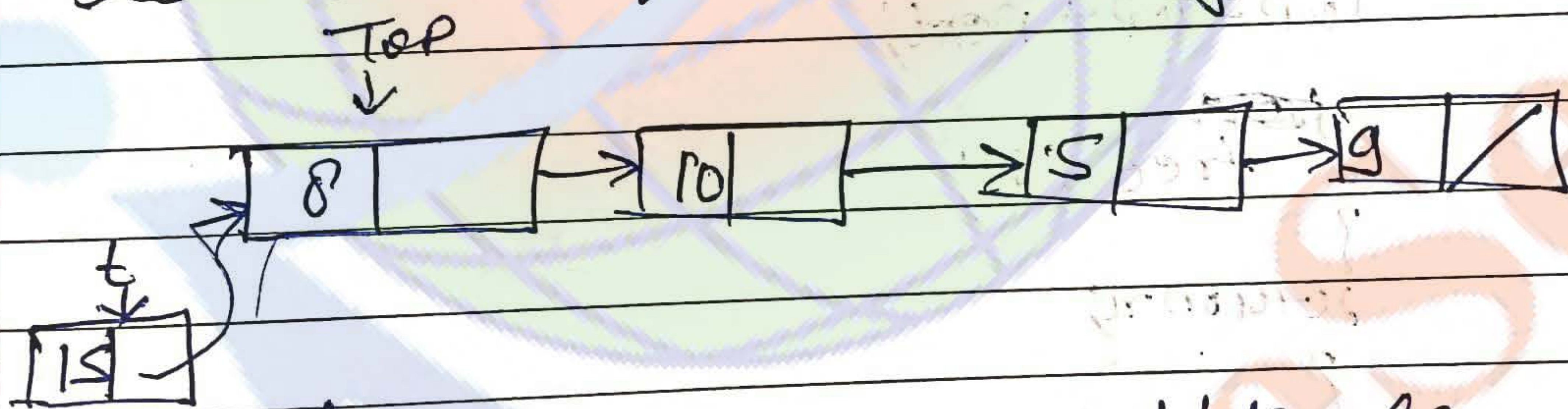
Empty and full stack i

empty: $if (T[i] == B[i])$

Full: $if (T[i] == B[i+1])$



* Implementation of stack using linked list:-



- always insert and delete from left hand side, it will take constant time.

Push (int x)

{

t = new Node;

if (t == NULL)

Print ("stack is full");

else

{

t -> data = x;

```
t -> next = TOP;
TOP = t;
```

```
int pop()
{
    int n = 0;
    if (TOP == NULL)
        printf("Stack is empty");
    else
    {
        n = TOP -> data;
        TOP = TOP -> next;
        free(n);
    }
    return n;
}
```

```
peek()
```

Note: Both push and pop takes constant time.

Intfix to Postfix Conversion!

① Intfix: operand operator operand

eg. $a + b$

prefix: operator operand operand

eg. $+ a b$

Postfix: operand operand operator

eg. $ab +$

Note
 → right to left
 & priority operator

operator	precedence	(lower)
$+$, $-$	0	↑ increase ↓ decrease higher
$*$, $/$	1	
\wedge	2	
$()$	3	

left to right

② infix $a + b * c$

Postfix $a + b * c$

Prefix: $(a + (b * c))$

$a + [b * c]$

$(a + (b * c))$

Prefix: $+ a * b c$

$(a + [b * c])$

Postfix: $= abc * +$

②

$$a + b + c + d * e$$

$$a + b + c + (d * e)$$

$$(a + b) + c + (d * e)$$

$$c(a + b) + c + (d * e)$$

$$c((a + b) + c) + (d * e)$$

prefix:-
+++ abc *de

post:-
ab+c+d e*+

③

$$(a + b) * (c - d) / e$$

post fix:-

$$\frac{(a + b) * (c - d)}{e}$$

prefix $\rightarrow / * + ab - cd$

$$\rightarrow \frac{(a + b) * (c - d)}{e} = \frac{ab + (cd -)}{e}$$

$$= (ab +)(cd -) * e /$$

④

$$a + b - c * d / e$$

post fix:-

$$a + b - cd * e /$$

prefix

$$a + b$$

$$\rightarrow ab / * cd e \leftarrow$$

$$\rightarrow ab + - cd * e /$$

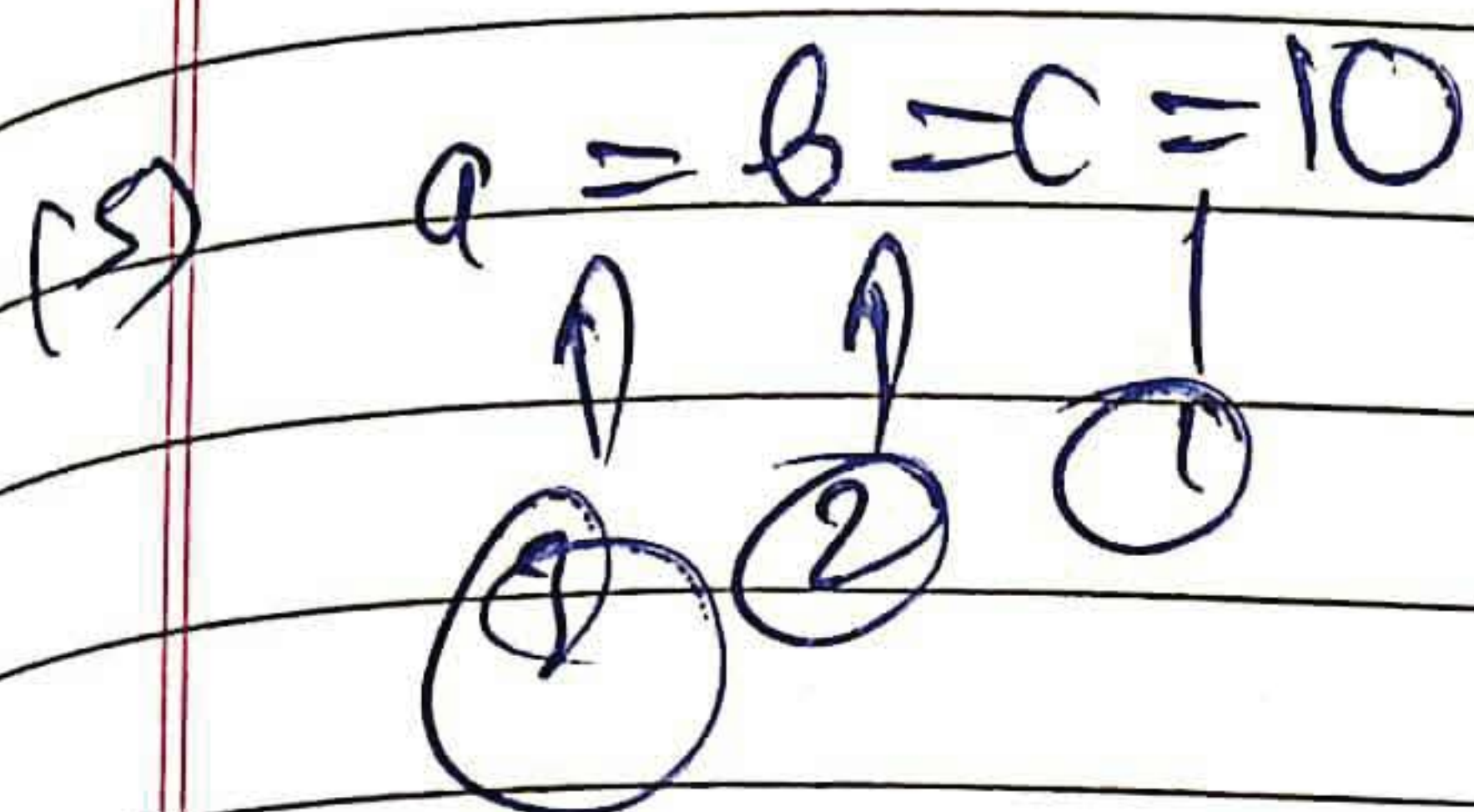
$$\rightarrow ab + cd * e / -$$

$$a + b - * cd / e$$

$$a + b - / * cd e$$

$$\rightarrow + ab - / * cd e$$

$$\rightarrow - + ab / * cd e$$



(Right to Left) ✓

$a + b + c$



(Left to Right)

$a(b)^c \rightarrow a \wedge b \wedge c$ (Right to Left) ✓

★ ~~Associativity~~ Associativity

→ If two or more operators are having same precedence in an expression, then they are evaluated based on associativity.

operators can have two types of associativity

- (a) ~~L to R~~ L to R and
- (b) R to L

eg. (=) Assignment operator

① R-L $a = b = c = 10$

Prefix $=a = b = c 10$

Postfix $abc 10 = = =$

② $a(b)^c \rightarrow a \wedge b \wedge c$

RL → prefix : $a \wedge a - b c$, post = $abc \wedge \wedge$

Note ① $a \times b - c \times d$
 $ab \times cd -$

② $a \times b \times c$
 abc

If operators are
continuous, then
it will affect

Note

④ Note Unary operators

⑤ Unary operator has highest precedence,
and their associativity is Right to Left



Precedence is
Same,
associativity R to L

eg ① $-a + \sqrt{b}$

Post
 $a - b\sqrt{c}$

Pre
 $-a + \sqrt{b}$

eg ② $\log(a+b)!$

Post

Pre
 $ab + ! \log$

$\log ! (+ab)$

③ $-3 \times a + b \log \sqrt{c}$

Proof

$-3 \times a + b \log \sqrt{c}$

$-3 \times a + b \log \sqrt{c}$

$-3 \times a + b \log \sqrt{c}$

$-3 \times a + b \log \sqrt{c} = -3a + \frac{b}{2} \log c$ $bc = b \times c$

Note

$ab + cd$

$ab \times cd$

$ab \div cd$

④ $\frac{a \times b + c - d}{e \times f}$

Proof

of associated in \mathbb{R} to \mathbb{Z}

$\frac{a \times b + c - d}{e \times f}$

$\frac{a \times b + c - d}{e \times f}$

$\frac{a \times b + c - d}{e \times f}$

$\frac{a \times b + c - d}{e \times f}$

$\frac{a \times b + c - d}{e \times f}$

Proof

Consider addition and subtraction have higher
 then $\times, /$
 as associated L to R

$$bc + d$$

$$bc + d -$$

~~abc~~

$$a \cdot bc + d - \cdot e / f$$

$$abc + d - \cdot e / f$$

★

① $a + b \cdot c - d / e$

~~a~~ $a + b \cdot c - d / e$

$$abc + d / e -$$

② $a + b + c / d + e - f \cdot g + (c / f) \cdot h$

1	()
2	-
3	/
4	$\cdot, /$
5	+ , -

⇒ S scans

(S will be expressed
 in reverse)

* Procedure for Infix to Postfix Conversion using Stack:-

- this procedure ~~can~~ will be scanning an expression only one time.

Procedure:-

- ① take a infix expression
- ② " " " " Stack
- ③ scan through infix expres taking one symbol at a time.
- ④ If a symbol is an operand, append into post fix
- ⑤ If a symbol is an operator, then
 - (a) If the precedence of operator is greater than the precedence of symbol in ~~the~~ stack, then push it into Stack
 - (b) else
POP out all greater or equal symbols from the stack.

Symbol	Stack	Postfix
a	-	a
+	+	a
b	+	ab
*	* +	ab
c	* +	abc
+	-	abc*+
d	-	abc*+d
/	/-	abc*+d
e	-	abc*+de
/	/-	abc*+de/-